



# Elementary Statistics Tables

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### Preface

Having published my Statistics tables in 1978, the obvious question is: why another book of Statistics tables so soon afterwards? The answer derives from reactions to the first book from a sample of some 500 lecturers and teachers covering a wide range both of educational establishments and of departments within those establishments. Approximately half found Statistics tables suitable for their needs; however the other half indicated that their courses covered rather less topics than included in the Tables, and therefore that a less comprehensive collection would be adequate. Further, some North American advisers suggested that more 'on the spot' descriptions, directions and illustrative examples would make such a book far more attractive and useful. Elementary statistics tables has been produced with these comments very much in mind.

The coverage of topics is probably still wider than in most introductory Statistics courses. But useful techniques are often omitted from such courses because of the lack of good tables or charts in the textbook being used, and it is one of the aims of this book to enable instructors to broaden the range of statistical methods included in their syllabuses. Even if some of the methods are completely omitted from the course textbook, instructors and students will find that these pages contain brief but adequate explanations and illustrations.

In deciding the topics to be included, I was guided to an extent by draft proposals for the Technician Education Council (TEC) awards, and Elementary statistics tables essentially covers the areas included in this scheme for which tables and/or charts are necessary. The standard distributions are of course included, i.e. binomial, Poisson, normal, t,  $\chi^2$  and F. Both individual and cumulative probabilities are given for binomial and Poisson distributions, the cumulative Poisson probabilities being derived from a newly designed chart on which the curves are virtually straight: this should enhance ease of reading and accuracy. A selection of useful nonparametric techniques is included, and advocates of these excellent and easy-to-apply methods will notice the inclusion of considerably improved tables for the Kruskal-Wallis and Friedman tests, and a new table for a Kolmogorov-Smirnov general test for normality. The book also contains random-number tables, including random numbers from normal and exponential distributions (useful for simple simulation experiments), binomial coefficients, control chart constants, various tables and charts concerned with correlation and rank correlation, and charts giving confidence intervals for a binomial p. The book ends with four pages of familiar mathematical tables and a table of useful constants, and a glossary of symbols used in the book will be found inside the back cover.

Considerable care and thought has been given to the design and layout of the tables. Special care has been taken to simplify a matter which many students find confusing: which table entries to use for one-sided and two-sided tests and for confidence intervals. Several tables, such as the percentage points for the normal,  $t, \chi^2$  and F distributions, may be used for several purposes. Throughout this book,  $\alpha_1$  and  $\alpha_2$  are used to denote significance levels for onesided (or 'one-tailed') and two-sided tests, respectively, and y indicates confidence levels for confidence intervals. (Where occasion demands, we even go so far as to use  $\alpha_1^R$  and  $\alpha_1^L$  to denote significance levels for right-hand and left-hand one-sided tests.) If a table can be used for all three purposes, all three cases are clearly indicated, with 5% and 1% critical values and 95% and 99% confidence levels being highlighted.

My thanks are due to many people who have contributed in various ways to the production of this book. I am especially grateful to Peter Worthington and Arthur Morley for their help and guidance throughout its development: Peter deserves special mention for his large contribution to the new tables for the Kruskal-Wallis and Friedman tests. Thanks also to Graham Littler and John Silk who very usefully reviewed some early proposals, and to Trevor Easingwood for discussions concerning the TEC proposals. At the time of writing, the proof-reading stage has not yet arrived; but thanks in advance to Tonie-Carol Brown who will be helping me with that unenviable task. Finally, I must express my gratitude to the staff of the Cripps Computing Centre at Nottingham University: all of the tables and charts have been newly computed for this publication, and the service which they have provided has been excellent.

Naturally, total responsibility for any errors is mine alone. It would be nice to think that there are none, but I would greatly appreciate anybody who sees anything that they know or suspect to be incorrect communicating the facts immediately to me.

HENRY NEAVE October 1979

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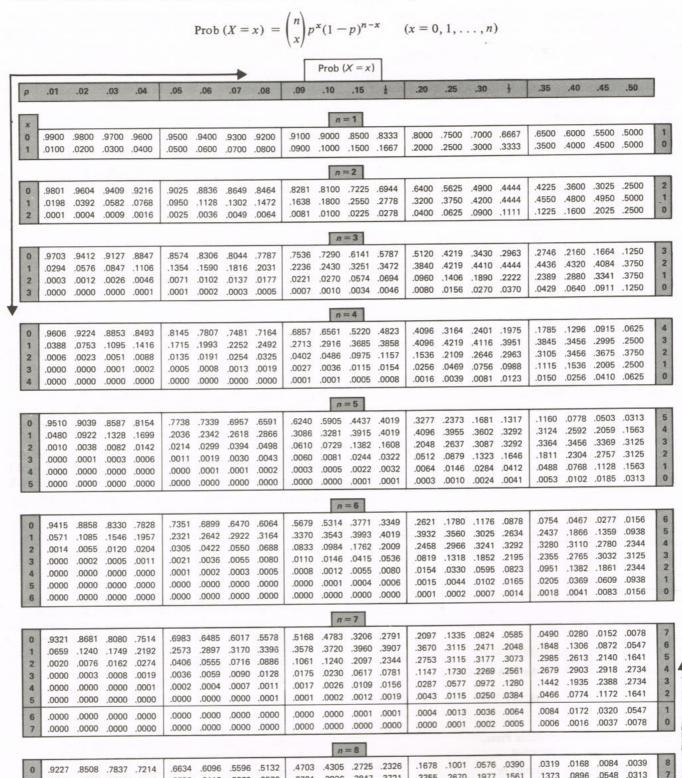
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## The binomial distribution: individual probabilities



If the probability is p that a certain event (often called a 'success') occurs in a trial of an experiment, the binomial distribution is concerned with the total number X of successes obtained in n independent trials of the experiment. Pages 4, 6, 8 and 10 give Prob (X = x) for all possible

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Prob (X = x)

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2605

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x and n up to 20, and 39 values of p. For values of  $p \leq \frac{1}{2}$ (along the top horizontal) refer to the x-values in the lefthand column; for values of  $p \ge \frac{1}{2}$  (along the bottom horizontal) refer to the x-values in the right-hand column.

3355

2936

1468

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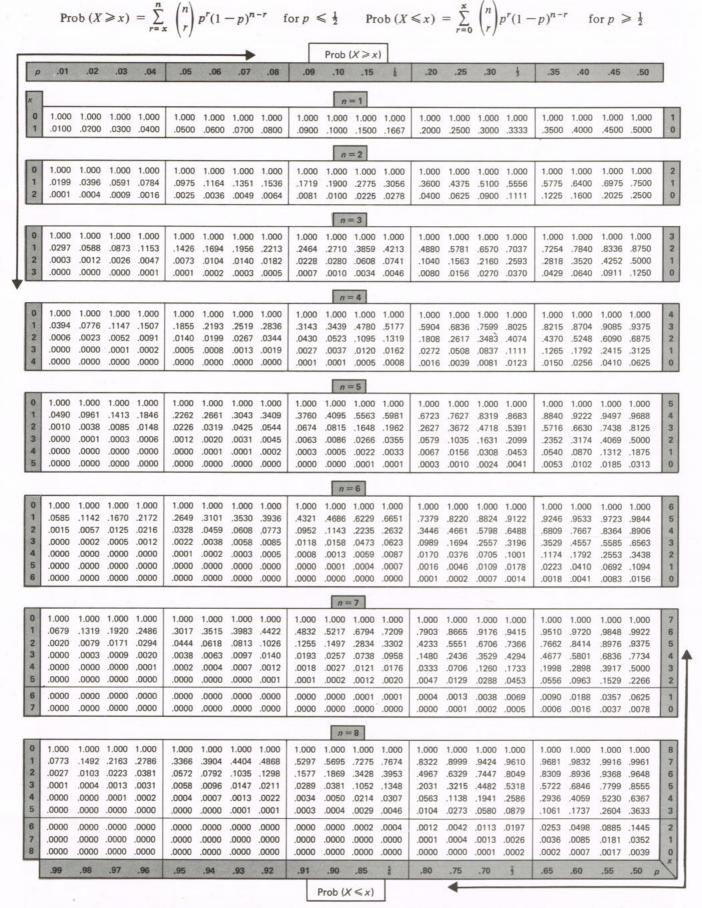
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### The binomial distribution: cumulative probabilities



Pages 5, 7, 9 and 11 give cumulative probabilities for the same range of binomial distributions as covered on pages 4, 6, 8 and 10. For values of  $p \le \frac{1}{2}$  (along the top horizontal) refer to the x values in the left-hand column, the table entries giving Prob  $(X \ge x)$ ; for values of  $p \ge \frac{1}{2}$  (along the bottom horizontal) refer to the x-values in the

right-hand column, the table entries giving Prob  $(X \le x)$  for these cases. Note that cumulative probabilities of the opposite type to those given may be calculated by Prob  $(X \le x) = 1 - \operatorname{Prob}(X \ge x + 1)$  and Prob  $(X \ge x) = 1 - \operatorname{Prob}(X \le x - 1)$ .

p	.01	.02	.03	.04	.05	.06	.07	.08	.09	.10	.15	1	.20	.25	.30	1	.35	.40	.45	.50
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2	.0034		.0262	.0433				.1285			.2597	No laser			.2668	.2341			.1110	.0703
3	.0001	.0006	.0019	.0042				.0261	.0348			.1302	.1762	.2336	.2668	.2731	.2716	.2508	.2119	.1641
4	.0000	.0000	.0001	.0003	.0006	.0012	.0021	.0034	.0052	.0074	.0283	.0391	.0661	.1168	.1715	.2048	.2194	.2508		.2461
5	.0000	.0000	.0000	.0000	.0000	.0001	.0002	.0003	.0005	.0008	.0050	.0078	.0165	.0389	.0735	.1024	.1181	.1672	.2128	.2461
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8	.0000	.0000	.0000	.0000	.0000			.0000	.0000			.0000			.0004	.0009	.0013	.0035	.0083	
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1	.0914	.1667	.2281	.2770	.3151	.3438		.3777	.3851		.3474	.3230	.2684		.1211	.0867	.0725	.0403	.0207	.0098
2	.0042	.0153	.0317	.0519				.1478	.1714		.2759	.1550	.3020	.2816	.2335	.1951	0.833 (9.35)	.2150		.1172
3	.0001	.0000	.0026	.0058		.0168	.0033	.0052	.0078	.0112		.0543	.0881	.1460	.2000	.2276	.2377		.2384	.2051
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8	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0004	.0014	.0030	3000000	.0106		.0439
9	.0000	.0000	.0000	.0000	.0000	.0000		.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0003	100000000000000000000000000000000000000	.0016	.0042	
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0	.8953	.8007	.7153	.6382	.5688	.5063	.4501	.3996	.3544	.3138	.1673	.1346	.0859	.0422	.0198	.0116	.0088	.0036	.0014	
1	.0995	.1798	.2433	.2925	.3293	.3555	.3727	.3823	.3855			.2961	1900000	.1549	.0932	.0636	.0518	.0266	.0125	.0054
2	.0050	.0183	.0376	.0609	100000000000000000000000000000000000000			.1662		.2131		.2961	15.772576		.1998	.1590	.1395	.0887	.0513	.0269
3	.0002	.0011	.0035	.0076			.0317	.0434	.0566		.1517	.0711	.2215		.2568	.2384	.2254	.2365		.1611
4	.0000	.0000	.0002	.0006	.0014		.0048	.0075	.0112	.0158	.0536		.0388		.1321	.1669	.1830	.2207		.2256
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7 8	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000		.0001	.0002	.0011	.0037	.0075	.0102	.0234		.0806
9	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0005	.0012	.0018	.0052	.0126	.0269
10	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	800000	.0007	.0021	
11	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0002	.0005
										n =	= 12									
0	.8864	.7847	.6938	.6127	.5404	.4759	.4186	.3677	.3225	.2824	.1422	.1122	5-20-00-00-00	.0317		.0077	7.38.35.00	.0022	.0008	.0002
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7 8	.0000	.0000	.0000		.0000	.0000	.0000	.0000	.0000		.0001		.0005	.0024				.0420	.0762	.1208
9	.0000	.0000	.0000		.0000	.0000	.0000	.0000	.0000		.0000	.0000	.0001		.0015		A San San	.0125	.0277	
10	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0002	.0005	.0008	.0025	.0068	.0161
11	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	25032	.0000	.0000		100 Sept. 100 Se	.0003	.0010	
12	.0000		.0000		.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0002
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0	.8775	.7690	.6730	.5882	.5133	.4474			96999999	.2542			100000000000000000000000000000000000000	.0238	.0097			.0013		
1	.1152	.2040		.3186		.3712		.3824	22/20/10/20	.3672			4200000	.1029	.0540		F 7/10 17 5 5/4	.0113	.0045	.0016
2	.0070	.0250		.0797	USA SASSASS	.1422					.2937		.2680	.2059	.1388		100000000000000000000000000000000000000	.0453	.0220	.0095
3	.0003	.0019		.0122	- Control (1974)	.0333		.0636	22 E S S V	.0997		.1069	.1535	.2097		.2296		.1845	.1350	.0873
4	.0000	.0001		.0013	1992090000	.0053		.0138	.0036			.0385	33,500,000	.1258				.2214	.1989	
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9	.0000	.0000			.0000		.0000	.0000	.0000			.0000	.0001	.0009	.0034	.0072		.0243	.0495	.0873
10	.0000	.0000			.0000		.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0006	.0014	.0022	.0065	.0162	.0349
11	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0002		.0012		.0095
	.0000	.0000			.0000		.0000	.0000	.0000		.0000		.0000	.0000	.0000		.0000		.0005	
12				17/21/21/21	1	0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001
13	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000		.0000	10000							

EXAMPLES: If ten dice are thrown, what is the probability of obtaining exactly two sixes? With n = 10 and  $p = \frac{1}{6}$ , Prob (X = 2) is found from the table to be 0.2907.

If a treatment has a 90% success-rate, what is the probability that all of twelve treated patients recover? With n = 12 and p = 0.9, the table gives Prob (X = 12) = 0.2824.

p	.01	.02	.03	.04	.05	.06	.07	.08	.09	.10	.15	ł	.20	.25	.30	4	.35	.40	.45	.50	
x											= 9	0									
0	1.000	1 000	1.000	1.000	1,000	1 000	1 000	1 000	1 000			1 000	1 000	1.000	1 000	1 000	1.000	1.000	1.000	1 000	
1		.1663	.2398	1.000	.3698	.4270	1.000	.5278	1.000	.6126	1.000	.8062	1.000	1.000	1.000	.9740	.9793	.9899	.9954	.9980	
2	.0034	.0131	.0282	.0478	A STATE OF THE STA	.0978	.1271	.1583	.1912	.2252	.4005	.4573	.5638	.6997	.8040	.8569	.8789	.9295	.9615	.9805	
3	.0001	.0006	.0020	.0045	.0084	.0138	.0209	.0298	.0405	.0530	.1409	.1783	.2618	.3993	.5372	.6228	.6627	.7682	.8505	.9102	
4	.0000	.0000	.0001	.0003	.0006	.0013	.0023	.0037	.0057	.0083	.0339	.0480	.0856	.1657	.2703	.3497	.3911	.5174	.6386	.7461	
5	.0000	.0000	.0000	.0000	.0000	.0001	.0002	.0003	.0005	.0009	.0056	.0090	.0196	.0489	.0988	.1448	.1717	.2666	.3786	.5000	
6	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0006	.0011	.0031	.0100	.0253	.0424	.0536	.0994	.1658	.2539	
7	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0003	.0013	.0043	.0083	.0112	.0250	,0498	.0898	
8	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0004	.0010	.0014	.0038	.0091	.0195	
9	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0001	.0003	.0008	.0020	
										n =	10										
0	1 000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000		1.000	1 000	1.000	1.000	1,000	1.000	1.000	1.000	1.000	1.000	1
1	.0956	.1829	.2626	.3352	0.135.913	.4614	.5160		.6106	.6513	.8031	.8385	.8926	.9437	.9718		.9865	.9940	.9975	.9990	
2		.0162	.0345	.0582	100000000		.1517	100000000000000000000000000000000000000	.2254	.2639		.5155		.7560	.8507		.9140	.9536	.9767		
3	.0001	.0009	.0028	.0062	650 NOVS	.0188	.0283	27.33.33	.0540		.1798	.2248	.3222	.4744	.6172		.7384	.8327	.9004	.9453	
4	.0000	.0000	.0001	.0004	.0010	.0020	.0036	.0058	.0088	.0128	.0500	.0697	.1209	.2241	.3504	.4407	.4862	.6177	.7340	.8281	
5	.0000	.0000	.0000	.0000	.0001	.0002	.0003	.0006	.0010	.0016	.0099	.0155	.0328	.0781	.1503	.2131	.2485	.3669	.4956	.6230	
6	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0001	.0014	.0024	.0064	.0197	.0473	.0766	.0949	.1662	.2616	.3770	
7	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0003	.0009	.0035	.0106	.0197	.0260	.0548	.1020		
8	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0004	.0016	.0034	.0048	.0123	.0274	.0547	
9	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0004	.0005	.0017		.0107	
0	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	,0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0003	.0010	
										n =	11										
0	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1
1	.1047	.1993	.2847	.3618	.4312	.4937	.5499	.6004	.6456	.6862	.8327	.8654	.9141	.9578	.9802	.9884	.9912	.9964	.9986	.9995	1
2	.0052	.0195	.0413	.0692	.1019	.1382	.1772	.2181	.2601	.3026	.5078	.5693	.6779	.8029	.8870	.9249	.9394	.9698	.9861	.9941	1
3	.0002	.0012	.0037	.0083	.0152	.0248	.0370	.0519	.0695	.0896	.2212	.2732	.3826	.5448	.6873	.7659	.7999	.8811		.9673	1
4		.0000	.0002	.0007	.0016	.0030	.0053	.0085	.0129		.0694	.0956	.1611	.2867		.5274	.5744	.7037	.8089	.8867	
5	.0000	.0000	.0000	,0000	.0001	.0003	.0005	.0010	.0017	.0028	.0159	.0245	.0504	.1146	.2103	.2890	.3317	.4672	.6029	.7256	
6	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0002	.0003	.0027	.0046	.0117	.0343	.0782	.1221	.1487	.2465	.3669	.5000	1
7	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0003	.0006	.0020	.0076	.0216	.0386	.0501	.0994	.1738	.2744	
8	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0002	.0012	.0043	.0088	.0122	.0293		.1133	-
9		.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000		.0000	.0000	.0000	.0001		.0014	.0020	.0059		.0327	
1		.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000		.0000	.0000	.0001		.0007	.0022	.0059	
600	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	10002	10000	
	0000000	07.5054					00.0500			n =			-								
0			1.000	1.000	1000000	1.000		1.000			1.000	1000000		1.000		1.000				1.000	12
1		.2153	.3062	.3873	WHISE.	.5241	.5814	.6323		.7176	.8578	.8878	.9313		.9862	.9923	.9943	.9978		.9998	11
2	.0062	.0231	.0486	.0809	.1184	.0316	.2033	.0652			.5565	.6187				.9460		.9804	.9917		10
4	.0002	.0015	.0003	.00107	600200000000000000000000000000000000000	.0043	.0075	3/33/3/	.0180	.0256		.1252		.6093	.5075		.6533	.9166	.9579	.9807	8
5	.0000	.0000	.0000	.0001	.0002	.0004		.0016	.0027	.0043	.0239	.0364			.2763		.4167	.5618		.8062	1
	30.0000	0.0000000	10-E0000X	111000000	13.0000	Variable.	THE SHEET	700000	2,555	52.37	1438333		-	-1.5830	1000	10000	200	1.23 =			
6	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0002	.0003	.0005	.0046	.0079	.0194	.0544	.1178	.0664	.0846	.3348	.4731		
8	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0007	.0002	.0039	.0028		.0188	.0255		.1117		1
9	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.00002	.0001	.0004	.0033	.0039				.0730	
10	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0002		.0008	.0028	.0079		
1	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	HISOSHW.	.0000	.0001	.0003	.0011	19300000	
2				.0000		.0000	.0000	1000	.0000	.0000		.0000			.0000				.0001		(
										n =	13										
0	1,000	1.000	1,000	1.000	1.000	1,000	1.000	1,000	1.000	-	1.000	1,000	1.000	1.000	1,000	1,000	1,000	1.000	1.000	1,000	13
1		.2310		.4118	.4867		.6107	STATE OF THE PARTY		.7458		.9065		.9762	.9903	.9949	.9963	.9987	.9996		13
2	.0072		.0564		.1354		.2298	33.000		.3787		.6635		.8733		.9615	.9704		.9951		1
3	.0003	.0020	.0062	.0135	.0245	.0392	.0578	3200	.1054	.1339	.3080	.3719	.4983	.6674	.7975	.8613	.8868	.9421	.9731	.9888	10
4	.0000	.0001	.0005	.0014	.0031	.0060	.0103	2000	.0242	.0342		.1581		.4157	.5794		.7217	.8314	.9071	.9539	1
5	.0000	.0000	.0000	.0001	.0003	.0007	.0013	.0024	.0041	.0065	.0342	.0512	.0991	.2060	.3457	.4480	.4995	.6470	.7721	.8666	8
6	.0000	.0000	.0000	.0000	.0000	.0001	.0001	.0003	.0005	.0009	.0075	.0127	.0300	.0802	.1654	.2413	.2841	.4256	.5732	.7095	1
7	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0001	.0013	.0024	.0070	.0243	.0624	.1035	.1295	.2288	.3563	.5000	6
8				.0000	.0000	.0000		.0000	.0000			.0003	.0012			.0347			.1788		1
9		.0000	.0000	.0000	.0000	.0000		.0000	.0000			.0000		.0010		.0088		.0321	.0698		-
0	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0007	.0016	.0025	.0078	.0203	.0461	3
1	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0002	.0003	.0013	.0041	.0112	2
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000		.0000	.0000	.0001		.0017	1
2				0000	0000	0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	1
2	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	,0000	.0000	.0000	10000	10000		.0000	10000		

EXAMPLES: If ten dice are thrown, what is the probability of obtaining at most two sixes? Now, Prob  $(X \le 2) = 1 - \text{Prob}(X \ge 3)$ . With n = 10 and  $p = \frac{1}{6}$ , the table gives Prob  $(X \ge 3)$  as 0.2248, so Prob  $(X \le 2) = 1 - 0.2248 = 10$ 

0.7752. If a treatment has a 90% success-rate, what is the probability that no more than ten patients recover out of twelve who are treated? With n=12 and p=0.9, the table gives Prob ( $X \le 10$ ) = 0.3410.

-	0.5	02	02	04	05	0.0	07	0.0	00		X = X	1	70	25	20	1	25	.40	AF	ED
P	.01	.02	.03	.04	.05	.06	.07	.08	.09	.10	.15	8	.20	.25	.30	3	.35	.40	.45	.50
×										n =	= 14									
0	.8687	.7536	.6528	.5647	.4877	.4205	.3620	.3112	.2670	.2288	.1028	.0779	.0440	.0178			.0024	.0008	.0002	.0001
1	.1229	.2153	.2827	.3294	.3593	.3758	.3815		.3698	.3559	.2539	.2181	.1539	.0832			100000000000000000000000000000000000000			.0009
3	.0081	.0286	.0568	.0892	.1229	.1559	.1867		.2377	.2570	.2912		.2501	.1802		.0779	.0634	.0317		.0056
4	.0003	.0023	.0070	.0149	.0259	.0398	.0562	.0745	.0940	.0349	.2056		.1720	.2402			.1366	.1549		.0222
5	.0000	.0000	.0000	.0001	.0004	.0009	.0018		.0051	.0078		.0499	.0860				55572	.2066	.1701	
3	.0000	.0000	.0000	.0000	.0000	.0001	.0002	.0004	.0008	.0013	.0093		.0322			7.5	.1759	.2066	.2088	1833
7	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0002	.0019	.0034	.0092	.0280				.1574	.1952	
3	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0003	.0006	.0020	.0082	.0232		.0510		.1398	.1833
9	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0003	.0018	.0066	.0134	.0183	.0408	.0762	.1222
)	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0003	.0014	.0033	.0049	.0136	.0312	.0611
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0002	.0006	.0010	.0033	.0093	.0222
2	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000		.0000	.0000	.0000	.0001	.0001	.0005	.0019	
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001		.0009
ä	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001
										n	= 15									
1	.8601	.7386	.6333	.5421	.4633	.3953	.3367	.2863	.2430	.2059	.0874	.0649	.0352	.0134	.0047	.0023	.0016	.0005	.0001	.0000
	.1303	.2261	.2938	.3388	.3658	.3785	.3801	.3734	.3605	.3432	.2312	.1947	.1319	.0668	.0305	.0171	.0126	.0047	.0016	.0005
2	.0092	.0323	.0636	.0988	.1348	.1691	.2003	.2273	.2496	.2669	.2856	.2726	.2309	.1559	.0916	.0599	.0476	.0219	.0090	.0032
	.0004	.0029	.0085	.0178	.0307	.0468	.0653	.0857	.1070	.1285	.2184	.2363	.2501	.2252	.1700	.1299	.1110	.0634		.0139
	.0000	.0002	.0008	.0022	.0049	.0090	.0148	.0223	.0317		.1156	.1418	1990000	.2252			A STATE OF S	.1268	.0780	.0417
	.0000	.0000	.0001	.0002	.0006	.0013	.0024	.0043	.0069	.0105		.0624	100000000000000000000000000000000000000	.1651	.2061	000220.2	50507	RISHARA	N 25575 N	AUXIONAL
	.0000	.0000	.0000	.0000	.0000	.0001	.0003	.0006	.0011		.0132	.0208	.0430	.0917	.1472		.1906	.2066	.1914	
죓	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001		.0005	.0053	.0035	.0393	.0348			.1181	.1647	
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000		.0001	.0002	.0007	.0034			2-3105-2	.0612		
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0007	.0030	.0067	.0096	.0245	.0515	.0916
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0006	.0015	.0024	.0074	.0191	.0417
蜀	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0003	.0004	.0016	.0052	.0139
	.0000	.0000	.0000	.0000	.0000	.0000	,0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0003		.0032
8	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0005
ā	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
										n =	= 16									
	.8515	.7238	.6143	.5204	.4401	.3716	.3131	.2634	.2211	.1853	.0743	.0541	.0281	.0100	.0033	.0015	.0010	.0003	.0001	.0000
	.1376	.2363	.3040	.3469	.3706	.3795	.3771	.3665	.3499	.3294	.2097	.1731	.1126	.0535	.0228	.0122	.0087	.0030	.0009	.0002
3	.0104	.0362	.0705	.1084	.1463	.1817	.2129	.2390	.2596	.2745	.2775	.2596	The second second	.1336	.0732	.0457	.0353	.0150		.0018
8	.0005	.0034	.0102	.0211	.0359	.0541	.0748	.0970	.1198	.1423	.2285	.2423	.2463	.2079	.1465	.1066	.0888	.0468		.0085
	.0000	.0002	.0010	.0029	.0061	.0112	.0183	.0274	.0385		.1311	.0756	35/15/1	.2252	.2040	.1732	1 CONTRACTOR   1 CONT	.1014	.0572	
						-				170000	000000	200000000			11235000	988880		100000000000000000000000000000000000000	10000000	2000
		.0000	.0000	.0000	.0001		.0005		.0017	.0028	.0045			.1101		.1905	.1982	.1983		.1222
	.0000	.0000	.0000	.0000		.0000	.0000	.0000	.0002		.0009	.0078	10000	.0197	.0487			.1417		
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0003	12.000	.0058	.0185		100000000000000000000000000000000000000	.0840	.1318	
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0002	.0014	.0056	.0119	.0167	.0392	.0755	.1222
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0002	.0013	.0032	.0049	.0142	.0337	.0667
	.0000	.0000	.0000	.0000	2000	.0000		.0000	.0000		.0000	.0000	.0000	.0000	.0002	.0007	.0011	.0040	.0115	.0278
ij	.0000	.0000	.0000	.0000	100000000000000000000000000000000000000	.0000		.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000			.0008	.0029	
	.0000	.0000	.0000	.0000	100000000000000000000000000000000000000	.0000		.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000		.0000	.0001	.0005	
	.0000	.0000	.0000	.0000	.0000	.0000	.0000		.0000	.0000	.0000	.0000	.0000	.0000	.0000		7113 53000000	.0000	.0001	
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
										n =	= 17									
	.8429	.7093	.5958	.4996	.4181	.3493	.2912	.2423	.2012	.1668	.0631	.0451	.0225	.0075	.0023	.0010	.0007	.0002	.0000	.0000
	.1447	.2461		.3539	.3741	.3790	.3726		.3383		.1893		5555555		.0169		.0060	.0019	.0005	
	.0117	.0402		.1180	.1575			.2492	.2677			.2452	Cloud Space	.1136	.0581		105000000000000000000000000000000000000	.0102	.0035	
	.0006	.0041	.0120	.0246	.0415		.0844	.1083	.1324		.2359	.2452	100000000000000000000000000000000000000	.1893			10 TO	.0341	.0144	
	.0000	.0003	.0013	.0036	.0076		.0222	.0330	.0458		.1457		75-5	.2209			100000000000000000000000000000000000000		.0875	
										Walter						The same of		100000	TAYS:	60.000
	.0000	.0000	.0000	.0000	.0001	.0003	.0007	.0013	.0023	.0039	.0236	.0357	100000000000000000000000000000000000000	.1276	.1784			.1839	.1841	
	.0000	.0000	.0000	.0000	100000000000000000000000000000000000000	.0000	.0000	.0002	.0004		.0005	.0028	2000000		.0644		.1134		.1883	
	.0000	.0000	.0000	.0000	.0000		.0000	.0000	.0000	.0000	.0003	.0006	100000000000000000000000000000000000000		.0276		The second second	.1070	.1540	
	.0000	.0000	.0000	.0000		.0000		.0000	.0000		.0000				.0095	.0193	.0263	.0571	.1008	.1484
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0005	.0026	.0061	.0090	.0242	.0525	.0944
	.0000	.0000	.0000	.0000	100000000000000000000000000000000000000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0006		.0024	.0081		.0472
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	7-20 10-20	.0000	.0001		.0005	.0021		.0182
	.0000	.0000	.0000	.0000	.0000			.0000	.0000	.0000	.0000	.0000	100000000000000000000000000000000000000	.0000	.0000		.0001	.0004		.0052
888	0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000		.0000	.0000	Watersta V	.0000	.0001	7.700-00000	.0010
88	.0000											100 200 200				0000	0000			
	.0000	.0000	.0000	.0000	.0000	.0000		.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000		.0000	.0000	.0000	.0001

							-			Prob (								(300)			
p	.01	.02	.03	.04	.05	.06	.07	.08	.09	.10	.15	100	.20	.25	.30	1	.35	.40	.45	.50	i
X										n =	14										
0		1.000	1.000		1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000		
1	.1313	.2464	.3472		.5123	.5795	.6380	.6888	.7330	.7712	.8972	.9221	.9560	.9822	.9932	.9966	.9976	.9992	.9998	.9999	
3	.0084	.0310	.0645		.1530	.2037	.2564	.3100	.1255		.6433	.7040	.8021	.8990	.9525	.9726	.9795	.9919	.9971	.9991	
4	.0000	.0001	.0006	.0019	.0042	.0080	.0036	.0214	.0315	.0441	.1465	.1937	.3018		.6448	.7388	.7795	.8757	.9368	.9713	
5	.0000	.0000	.0000	.0002	.0004	.0010	.0020	.0035	.0059	.0092	.0467	.0690	.1298		.4158	.5245	.5773	.7207	.8328	.9102	
6	.0000	.0000	.0000	.0000	.0000	.0001	.0002	.0004	.0008	.0015	.0115	.0191	.0439	.1117	.2195	.3102	.3595	.5141	.6627	.7880	1
7	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0002	.0022	.0041	.0116	.0383	.0933	.1495	.1836	.3075	.4539	.6047	
8	.0000	.0000	.0000		.0000	.0000	.0000	.0000	.0000	.0000	.0003	.0007	.0024		.0315			.1501		.3953	
9	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0004		.0083	.0174	.0243	.0583		.2120	
1000		2000			.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000		.0017		.0060	.0175		.0898	H
11	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0002	.0007	.0011	.0039	.0114		
13	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0000	.0001	.00022		
14	.0000	.0000	.0000		.0000	.0000		.0000	.0000	.0000	.0000			.0000			128.501	.0000	.0000		
										-	-										
						20000000				n =	= 15										100
0	1.000	1.000	1.000		1.000	1.000	1.000		1.000		1.000		1.000		1.000	1000	10000000	1.000	1.000		1
2	.1399	.2614	.3667		.5367	.6047	.6633	.7137	.7570	.7941	.9126	.9351	.9648	.9866	.9953	.9977	.9984	.9995		1.000	
3	.0004	.0030	.0094	.0203	.0362	.0571	.0829	.1130	.1469	.1841	.3958	.4678	.6020		.8732	.9206	.9383	.9729		.9963	
4	.0000	.0002	.0008	.0024	.0055	.0104	.0175	.0273	.0399	.0556		.2315	.3518		.7031	.7908	.8273	.9095	.9576	.9824	1
5	.0000	.0000	.0001	.0002	.0006	.0014	.0028	.0050	.0082	.0127	.0617	.0898	.1642	.3135	.4845	.5959	.6481	.7827	.8796	.9408	
6	.0000	.0000	.0000	.0000	.0001	.0001	.0003	.0007	.0013	.0022	.0168	.0274	.0611	.1484	.2784	.3816	.4357	.5968	.7392	.8491	
7	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0002	.0003	.0036	.0066	.0181	.0566	.1311	.2030	.2452	.3902	.5478	.6964	
8	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0006	.0013	.0042		.0500	.0882	.1132	.2131	.3465	.5000	
9	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0002	.0008	.0042	.0152	.0308	.0422	.0950	.1818	.3036	
1	.0000	.0000															-		200000000000000000000000000000000000000		
2	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0007	.0018	.0028	.0093	.0255	.0592	
3	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0003	.0011	.0037	
4	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0005	8
5	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	
										n =	16										
0	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	-
1	.1485	.2762	.3857	.4796	.5599	.6284	.6869	.7366	.7789	.8147	.9257	.9459	.9719	.9900	.9967	.9985	.9990	.9997	.9999	1.000	
2	.0109	.0399	.0818		.1892	.2489		.3701	.4289	.4853	.7161	.7728	.8593	.9365	.9739	.9863	.9902	.9967		.9997	1
3 4	.0005	.0037	.0113	The state of	.0429	.0673		.1311	.1694	.2108		.5132	.6482	.8029	.9006	.9406	.9549	.9817	.9934	.9979	
5	.0000	.00002	.0001	.0032	.0070	.0132	.0221	.0342	.0496	.0684	.2101	.2709	.4019	.5950	.7541	.8341	.8661	.9349	.9719	.9894	
6	.0000	.0000	.0000	.0000	.0001	.0002	.0005	.0010	.0019	.0033		.0378		.1897	.3402	.4531	.5100	.6712	.8024	.8949	
7	.0000	.0000	.0000	.0000	.0000	.00002	.0003		.0003	.0005	.0056	.0101			.1753		.3119		.6340		
8	.0000	.0000	.0000	.0000	.0000	.0000		.0000	.0000	.0001	.0011	.0021	.0070	.0271	.0744	.1265	.1594	.2839		.5982	
9	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0002	.0004	.0015	.0075	.0257	.0500	.0671	.1423	.2559	.4018	
0	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0002	.0016	.0071	.0159	.0229	.0583	.1241	.2272	
1	.0000	.0000	.0000	.0000	.0000	.0000		.0000	.0000	.0000	.0000	.0000	.0000	.0003	.0016	.0040	.0062	.0191	.0486	.1051	1333
2	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0003	.0008	.0013			.0384	
3	.0000	.0000	.0000	.0000	.0000	.0000		.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001		.0009		.0106	
5	.0000	.0000		.0000	.0000	.0000	.0000		.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000		.0000		.0003	100
6			.0000	0.00		.0000	.0000	ATTENDED OF	.0000		.0000	.0000		.0000	.0000	90000000	.0000		.0000		
											17										
٦	1.000	1.000	1 000	1.000	1.000	1.000	1.000	1.000	1.000	1 000				4 ***			4		4.655		
0	.1571	.2907	1.000	1.000	1.000	.6507	1.000		1.000	1.000	1.000	1.000		1.000	1.000		1.000	1.000	1.000		1
2	.0123			.1465		.2717	.3362		.4604	.5182		.8017		.9499	.9807	100000		.9998	.9994	.9999	3
3	.0006	.0044	.0134	.0286	.0503	.0782	.1118	775-5-5	.1927	.2382		.5565	.6904	.8363		.9558	.9673		.9959	.9988	1
4	.0000	.0003	.0014	.0040	.0088	.0164	.0273		.0603		.2444	.3113		.6470	.7981	.8696	.8972			.9936	1
5	.0000	.0000	.0001	.0004	.0012	.0026	.0051	.0089	.0145	.0221	.0987	.1396	.2418	.4261	.6113	.7186	.7652	.8740	.9404	.9755	1
6	.0000	.0000		.0000	.0001	.0003	.0007		.0027	.0047		.0504	.1057		.4032		.5803			.9283	1
7	.0000	.0000	.0000	.0000	.0000	.0000	.0001		.0004	.0008		.0147	.0377		.2248	9.750.0000	.3812			.8338	1
9	.0000	.0000	.0000	.0000	.0000	.0000	.0000		.0000	.0001	.0017	.0035		.0402	.1046	30000000		.3595	.5257	.6855	
0	.0000	.0000		.0000	.0000	.0000	.0000		.0000	.0000		.0007	.0026	.0124	.0403	VA.131.1913			.1834		
100	000000000000000000000000000000000000000	2000-000	The second	VIII. 1970.00	DOMESTICAL DESIGNATION OF THE PERSON OF THE	200000	1077219-008	VIII ORGANIA I	50.00000	234302224	8550 KO 17	500000000	F018710-51	7.75803803310	925000000	0000000	25/28/55/00	CALVERY	200 - 200 a		100
1 2	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0006	.0032	.0080				.1662	
3	.0000	.0000	.0000	.0000	.0000	.0000		.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0007	.0003				.0245	
4	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000		.0000				.0064	
5	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0003	.0012	
6	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	
7	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	
-								The second second	CONTRACTOR OF THE PARTY OF THE	100000000000000000000000000000000000000	100000000000000000000000000000000000000	_			The second second	-		-		_	1

Prob  $(X \leq x)$ 

	.01	.02	.03	.04	.05	.06	.07	.08	.09	.10	(X = x)	į.	.20	.25	.30	4	.35	.40	.45	.50
										n =		0								
-	.8345	.6951	.5780	.4796	.3972	.3283	.2708	.2229	.1831	.1501	.0536	.0376	.0180	.0056	.0016	.0007	.0004	.0001	.0000	.0000
	.1517	.2554	.3217	.3597	.3763	.3772	.3669	.3489	.3260	.3002	.1704	.1352	.0811	.0338	.0126	.0061	.0042	.0012	.0003	.0001
	.0130	.0443	.0846	.1274	.1683	.2047	.2348	.2579	.2741	.2835	.2556	.2299	.1723	.0958	.0458	.0259	.0190	.0069	.0022	.0006
	.0007	.0048	.0140	.0283	.0473	.0697	.0942	.1196	.1446	.1680	.2406	.2452	.2297	.1704	.1046	.0690	.0547	.0246	.0095	.0031
	.0000	.0004	.0016	.0044	.0093	.0167	.0266	.0390	.0536	.0700	.1592	.1839	.2153	.2130	.1681	.1294	.1104	.0614	.0291	.0117
	.0000	.0000	.0001	.0005	.0014	.0030	.0056	.0095	.0148	.0218	.0787	.1030	.1507	.1988	.2017	.1812				3.0.53
ı	.0000	.0000	.0000	.0000	.0002	.0004	.0009	.0018	.0032	.0052	.0301	.0446	.0816	.1436	.1873	.1963	.1941	.1655	.1181	.0708
1	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0003	.0002	.0022	.0042	.0120	.0376	.0811	.1157	.1327	.1734	.1864	.1669
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0004	.0009	.0033	.0139	.0386	.0643	.0794	.1284	.1694	.1855
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0002	.0008	.0042	.0149	.0289	.0385	.0771	.1248	.1669
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0010	.0046	.0105	.0151	.0374	.0742	.1214
ı	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0002	.0012	.0031	.0047	.0145	.0354	.0708
ı	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0002	.0007	.0012	.0045	.0134	.0327
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0002	.0009	.0031
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0006
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001
	.0000	.0000	,0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
										n =	19									
I	.8262	.6812	.5606	.4604	.3774	.3086	.2519	.2051	.1666	.1351	.0456	.0313	.0144	.0042	.0011	.0005	.0003	.0001	.0000	,0000
ı	.1586	.2642	.3294	.3645	.3774	.3743	.3602	.3389	.3131	.2852	.1529	.1189	.0685	.0268	.0093	.0043	.0029	8000.	.0002	.0000
1	.0144	.0485	.0917	.1367	.1787	.2150	.2440	.2652	.2787	.2852	.2428	.2141	.1540	.0803	.0358	.0193	.0138	.0046	.0013	.0003
ı	.0008	.0056	.0161	.0323	.0533	.0778	.1041	.1307	.1562	.1796	.2428	.2426	.2182	.1517	.0869	.0546	.0422	.0175	.0062	.0018
	.0000	.0005	.0020	.0054	.0112	.0199	.0313	.0455	.0618	.0798	.1714	.1941	.2182	.2023	.1916	.1639	.1468	.0933	.0203	.0222
H	.0000	.0000	.0000	.0001	.0002	.0006	.0012	.0024	.0042	.0069	.0374	.0544	.0955	.1574	.1916	.1912	.1844	.1451	.0949	.0518
ı	.0000	.0000	.0000	.0000	.0002	.0000	.0002	.0004	.0008	.0014	.0122	.0202	.0443	.0974	.1525	.1776	.1844	.1797	.1443	.0961
ı	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0001	.0002	.0032	.0061	.0166	.0487	.0981	.1332	.1489	.1797	.1771	.1442
1	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0007	.0015	.0051	.0198	.0514	.0814	.0980	.1464	.1771	.1762
ı	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0003	.0013	.0066	.0220	.0407	.0528	.0976	.1449	.1762
ı	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0003	.0018	.0077	.0166	.0233	.0532	.0970	.1442
ı	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0004	.0022	.0055	.0083	.0237	.0529	.0961
1	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0003	.0006	.0024	.0082	.0222
ı	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0001	.0005	.0022	.0074
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	,0000	.0001	.0005	.0018
ı	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0003
ı	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
	.0000	.0000	.0000	,0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
										n =	20									
	.8179	.6676	.5438	.4420	.3585	.2901	.2342	.1887	.1516	.1216	.0388	.0261	.0115	.0032	.0008	.0003	,0002	.0000	.0000	.0000
	.1652	.2725	.3364	.3683	.3774	.3703	.3526	.3282	3100000000	.2702		.1043	.0576	.0211	.0068	.0030	.0020	.0005	.0001	.0000
	.0159	.0528	.0988	.0364	.1887	.2246	.2521	.2711	.2818	.2852	.2293	.1982	.1369	.0669	.0278	.0143	.0100	.0031	.0008	.0002
	.0000	.0006	.0024	.0065	.0133	.0233	.0364	.0523	.0703	.0898	.1821	.2022	.2182	.1897	.1304	.0911	.0738	.0350	.0139	.0046
	.0000	.0000	.0002	.0009	.0022	.0048	.0088	.0145	.0222	.0319	.1028	.1294	.1746	.2023	.1789	.1457	.1272	.0746	.0365	.0148
	.0000	.0000	.0000	.0001	.0003	.0008	.0017	.0032	.0055	.0089	.0454	.0647	.1091	.1686	.1916	.1821	.1712	.1244	.0746	.0370
	.0000	.0000	.0000	.0000	.0000	.0001	.0002	.0005	.0011	.0020	.0160	.0259	.0545	.1124	.1643	.1821	.1844	.1659	.1221	.0739
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0002	.0004	.0046	.0084	.0222	.0609	.1144	.1480	.1614	.1797	.1623	.1201
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0011	.0022	.0074	.0271	.0654	.0987	.1158	.1597	.1771	.1602
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0002	.0001	.0005	.0030	.0120	.0247	.0336	.0710	.1185	.1602
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0005	.0008	.0039	.0092	.0136	.0355	.0727	.1201
1	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0002	.0010	.0028	.0045	.0146	.0366	.0739
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0002	.0007	.0012	.0049	.0150	.0370
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0003	.0013	.0049	.0148
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0003	.0013	.0046
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0002	.0011
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
4								_						_	_			- CONT.   1   1   1		.50

The four charts on pages 12 and 13 are for use in binomial sampling experiments, both to find confidence intervals for p and to produce critical regions for the sample fraction f=X/n (see bottom of page 4 for notation) when testing a null hypothesis  $H_0\colon p=p_0$ . The charts produce (a) confidence intervals having  $\gamma=90\%$ , 95%, 98% and 99% confidence levels; (b) one-sided critical regions (for alternative hypotheses  $H_1$  of the form  $p< p_0$  or  $p>p_0$ ) for tests with significance levels  $\alpha_1=5\%$ ,  $2\frac{1}{2}\%$ , 1% and  $\frac{1}{2}\%$ ; and (c) two-sided critical regions (for  $H_1$  of the form  $p\neq p_0$ )

for tests with significance levels  $\alpha_2=10\%$ , 5%, 2% and 1%. For confidence intervals, locate the sample fraction f on the horizontal axis, trace up to the two curves labelled with the appropriate sample size n, and read off the confidence limits on the vertical axis. For critical regions, locate the hypothesised value of p,  $p_0$ , on the vertical axis, trace across to the two curves labelled with the sample size n and read off critical values  $f_1$  and/or  $f_2$  on the horizontal axis. If  $f_1 < f_2$  the one-sided critical region for  $H_1: p < p_0$  is  $f \le f_1$ , or if  $H_1$  is  $p > p_0$  it is  $f \ge f_2$ . A two-sided critical

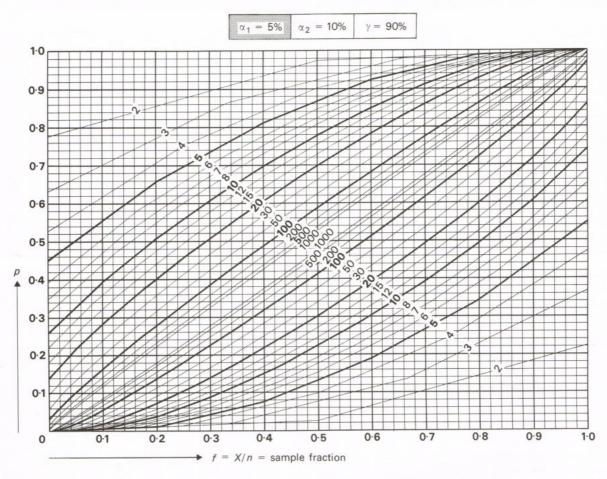
p	.01	.02	.03	.04	.05	.06	.07	.08	.09	.10	.15	1	.20	.25	.30	1	.35	.40	.45	.50	
	.01	.02	.00	,ury	,00	.00	.07	.00	1 .05	.10	.10	6	.20	.20	,30	3	.30	.40	.45	.50	3
X		2000 0000	17174-7-140-0						_	n =	= 18										_
0	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	ı
1	.1655	.3049	.4220	.5204	.6028	.6717	.7292	.7771	.8169	.8499	.9464	.9624	.9820	.9944	.9984	.9993	.9996	.9999	1.000	1.000	-80
3	.0138	.0052	.1003	.1607	.2265	.2945	.3622	.4281	.4909	.5497	.7759	.8272	.9009	.9605	.9858	.9932	.9954	.9987	.9997	.9999	- 80
4	.0000	.0004	.0018	.0050	.0109	.0201	.0333	.0506	.0723	.0982	.2798	.3521	.4990	.6943	.8354	.8983	.9217	.9672	.9880	.9993	- 80
5	.0000	.0000	.0002	.0006	.0015	.0034	.0067	.0116	.0186	.0282	.1206	.1682	.2836	.4813	.6673	.7689	.8114	.9058	.9589	.9846	- 80
6	.0000	.0000	.0000	.0001	.0002	.0005	.0010	.0021	.0038	.0064	.0419	.0653	.1329	.2825	.4656	.5878	.6450	.7912	.8923	.9519	t
7	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0003	.0006	.0012	.0118	.0206	.0513	.1390	.2783	.3915	.4509	.6257	.7742	.8811	I
3	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0002	.0027	.0053	.0163	.0569	.1407	.2233	.2717	.4366	.6085	.7597	П
9	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0005	.0011	.0043	.0193	.0596	.1076	.1391	.2632	.4222	.5927	ı
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	,0001	.0002	.0009	.0054	.0210	.0433	.0597	.1347	.2527	.4073	ı
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0002	.0012	.0061	.0144	.0212	.0576	.1280	.2403	ı
ä	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0002	.0014	.0039	.0062	.0203	.0537	.1189	Н
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0003	.0009	.0014	.0058	.0183	.0481	
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0000	.0013	.0049	.0154	
	.0000	.0000	.0000	.0000	.0000	.0000	0300000	1000000		CONFIGURA OF	7//										+
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0007	
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	
																					-
										n =	19										
	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	
	.1738	.3188	.4394	.5396	.6226	.6914	.7481	.7949	.8334	.8649	.9544	.9687	.9856	.9958	.9989	.9995	.9997	.9999	1.000	1.000	ı
	.0153	.0546	.1100	.1751	.2453	.3171	.3879	.4560	.5202	.5797	.8015	,8498	.9171	.9690	.9896	.9953	.9969	.9992	.9998	1.000	B
	.0009	.0061	.0183	.0384	.0665	.1021	.1439	.1908	.2415	.2946	.5587	.6357	.7631	.8887	.9538	.9760	.9830	.9945	.9985	.9996	П
	.0000	.0005	.0022	.0061	,0132	.0243	.0398	.0602	.0853	.1150	.3159	.3930	.5449	.7369	.8668	.9213	.9409	.9770	.9923	.9978	I
	CENTRAL				.0020	.0044	.0085	.0147	.0235	.0352	.1444	.1989	.3267	.5346	.7178	.8121	.8500	.9304	.9720	.9904	-
	.0000	.0000	.0000	.0001	.0002	.0006	.0014	.0029	.0051	.0086	.0537	.0824	.1631	.3322	.5261	.6481	.7032	.8371	.9223	.9682	I
	.0000	.0000	.0000	.0000	.0000	.0001	.0002	.0004	.0009	.0017	.0163	.0281	.0676	.1749	.3345	.4569	.5188	.6919	.8273	.9165	1
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0008	.0079	.0067	.0287	.1820	.2793	.1855	.5122	.6831	.8204	H
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0004	.0016	.0089	.0326	.0648	.0875	.1861	.3290	.5000	п
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0003	.0023	.0105	.0241	.0347	.0885	.1841	.3238	T
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0005	.0028	.0074	.0114	.0352	.0871	.1796	
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0006	.0019	.0031	.0116	.0342	.0835	B
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0004	.0007	.0031	.0109	.0318	В
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0001	.0006	.0028	.0096	Ш
8	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0005	.0022	I
н	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	,0004	П
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	н
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	,0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	Į.
										n =	20										
	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	Contract of the Contract of th		1.000	1.000	1.000	1 000	1.000	1 000	1 000	1.000	4 000	
	.1821	.3324	.4562	.5580	.6415	.7099	.7658	.8113	.8484	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	
	.0169	.0599	.1198	.1897	.2642	,3395	.4131	.4831	.5484	.6083	.8244	.8696	.9308	.9757	.9924	.9967	.9979	.9995	.9999	1.000	
	.0010	.0071	.0210	.0439	.0755	.1150	.1610	.2121	.2666	.3231	.5951	.6713	.7939	.9087	.9645	.9824	.9879	.9964	.9991	.9998	
	.0000	.0006	.0027	.0074	.0159	.0290	.0471	.0706	.0993	.1330	.3523	.4335	.5886	.7748	.8929	.9396	.9556	.9840	.9951	.9987	1
	.0000	.0000	.0003	.0010	.0026	.0056	.0107	.0183	.0290	.0432	.1702	.2313	.3704	.5852	.7625	.8485	.8818	.9490	.9811	.9941	
	.0000	.0000	.0000	.0001	.0003	.0009	.0019	.0038	.0068	.0113	.0673	.1018	.1958	.3828	.5836	.7028	.7546	.8744	.9447	.9793	Sec.
	.0000	.0000	.0000	.0000	.0000	.0001	.0003	.0006	.0013	.0024	.0219	.0371	.0867	.2142	.3920	.5207	.5834	.7500	.8701	.9423	1000
	.0000	.0000	,0000	.0000	.0000	.0000	.0000	.0001	.0002	.0004	.0059	.0113	.0321	.1018	.2277 -		.3990	.5841	.7480	.8684	100
и.	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0013	.0028	,0100	.0409	.1133	.1905	.2376	.4044	.5857	.7483	
۰									.0000				.0026	.0139	.0480	.0919	.1218	.2447	.4086	.5881	
	.0000	.0000	.0000	.0000	.0000	,0000	.0000	.0000	.0000	.0000	.0000	.0001	.0006	.0039	.0171	.0376	.0532	.1275	.2493	.4119	
88	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0009	.0051	.0130	.0196	.0565	.1308	.2517	1
88	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0002	.0003	.0037	.0060	.0210	.0580	.1316	
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0003	.0003	.0005	.0064	.0207	
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	100000000000000000000000000000000000000	.0003	.0015	.0059	f
	.0000		.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0003	.0059	
88			.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0002	
1	.0000		.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	ø
1	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000		.0000	.0000	I
-																				_	1000

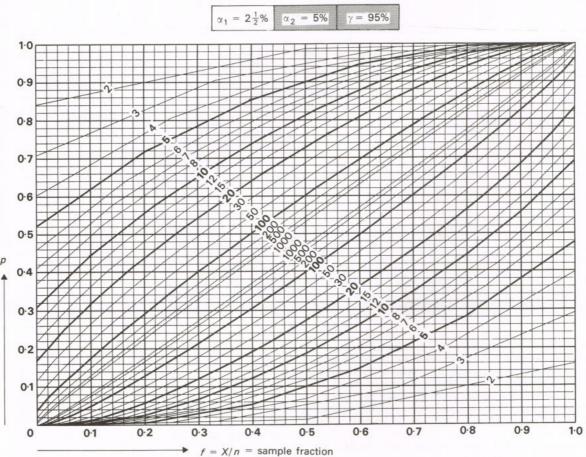
region appropriate for  $H_1\colon p\neq p_0$  is comprised of both of these one-sided regions. The 'curves' are in fact drawn as straight lines joining points corresponding to all n+1 possible values of f (this is seen most clearly for small n). Use of values of  $f_1$  and  $f_2$  which are in fact not realisable values of f result in conservative critical regions, i.e. actual  $\alpha_1$  or  $\alpha_2$  values which are less than the nominal values.

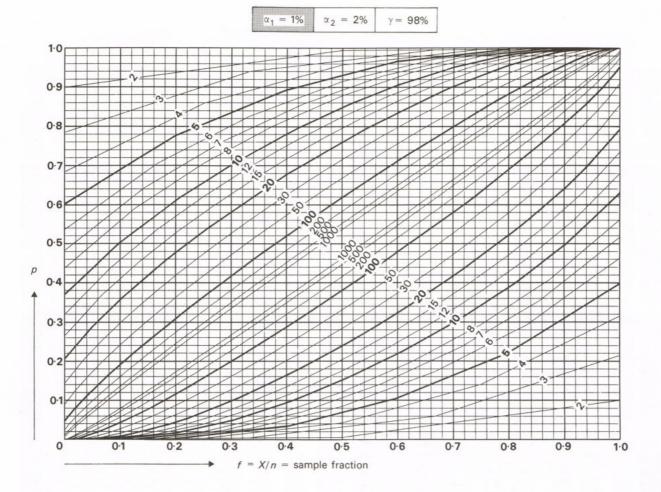
EXAMPLES: With eight successes out of twenty, i.e. n=20, X=8 and f=8/20=0.4, the  $\gamma=95\%$  confidence interval for p is (0.19:0.64), using the second chart on

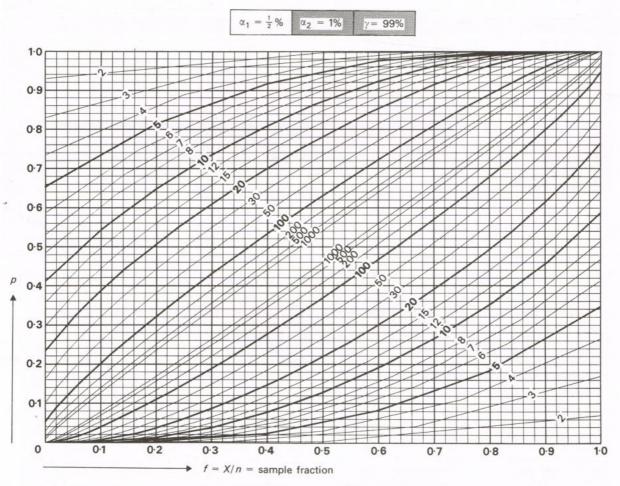
page 12. Using the same chart, suppose we wish to test  $H_0\colon p=0.6$ , again with n=20. We read off  $f_1=0.36$  and  $f_2=0.83$ . So  $f\leqslant 0.36$  (i.e.  $X\leqslant 7$ ) is the  $\alpha_1^L=2\frac{1}{2}\%$  critical region appropriate for  $H_1\colon p<0.6$ ,  $f\geqslant 0.83$  (i.e.  $X\geqslant 17$ ) is the  $\alpha_1^R=2\frac{1}{2}\%$  critical region appropriate for  $H_1\colon p>0.6$ , and these two regions combined constitute the  $\alpha_2=5\%$  critical region appropriate for  $H_1\colon p\neq 0.6$ .  $\alpha_1^L$  and  $\alpha_1^R$  denote significance levels for the one-sided tests where  $H_1$  says that p is to the Left or Right respectively of  $p_0$ . The true significance levels here are in all cases slightly less than the nominal figures of  $2\frac{1}{2}\%$  or 5%.

# Charts giving confidence intervals for p and critical values for the sample fraction









For description, see pages 10 and 11.

### The Poisson distribution: individual probabilities

Prob 
$$(X = x) = e^{-\mu} \cdot \frac{\mu^x}{x!}$$
  $(x = 0, 1, 2, ...)$ 

									Prob	(X = x)									
L	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09	0.10	0.12	0.14	0.16	0.18	0.20	0.25	0.30	0.35	4
ò	.9900	.9802	.9704	.9608	.9512	.9418	.9324	.9231	.9139	.9048	.8869	.8694	.8521	.8353	.8187	.7788	.7408	.7047	ı
П	.0099	.0196	.0291	.0384	.0476	.0565	.0653	.0738	.0823	.0905	.1064	.1217	.1363	.1503	.1637	.1947	.2222	.2466	1
	.0000	.0002	.0004	.0008	.0012	.0017	.0023	.0030	.0037	.0045	.0064	.0085	.0109	.0135	.0164	.0243	.0333	.0432	1
	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0001	.0001	.0002	.0003	.0004	.0006	.0008	.0011	.0020	.0033	.0050	1
5	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0001	.0003	.0004	1
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	1
4	0.40	0.45	0,50	0.55	0.60	0.65	0.70	0.75	0.80	0.85	0.90	0.95	1.00	1.10	1.20	1.30	1.40	1.50	4
	.6703	.6376	.6065	.5769	.5488	.5220	.4966	.4724	.4493	.4274	.4066	.3867	.3679	.3329	.3012	.2725	.2466	.2231	1
п	.2681	.2869	.3033	.3173	.3293	.3393	.3476	.3543	.3595	.3633	.3659	.3674	.3679	.3662	.3614	.3543	.3452	.3347	1
	.0536	.0646	.0758	.0873	.0988	.1103	.1217	.1329	.1438	.1544	.1647	.1745	.1839	.2014	.2169	.2303	.2417	.2510	١
	.0072	.0097	.0126	.0160	.0198	.0239	.0284	.0332	.0383	.0437	.0494	.0553	.0613	.0738	.0867	.0998	.1128	.1255	1
	.0007	.0011	.0016	.0022	.0030	.0039	.0050	.0062	.0077	.0093	.0111	.0131	.0153	.0203	.0260	.0324	.0395	.0471	1
	.0001	.0001	.0002	.0002	.0004	.0005	.0007	.0009	.0012	.0016	.0020	.0025	.0031	.0045	.0062	.0084	.0111	.0141	4
	.0000	.0000	.0000	.0000	.0000	.0001	.0001	.0001	.0002	.0002	.0003	.0004	.0005	.0008	.0012	.0018	.0026	.0035	1
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0001	.0001	.0002	.0003	.0005	.0008	1
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0001	.0001	-
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	,0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	_
M	1.60	1.70	1.80	1.90	2.00	2.10	2.20	2.30	2.40	2.50	2.60	2.70	2.80	2.90	3.00	3.10	3.20	3.30	μ
T	.2019	.1827	.1653	.1496	.1353	.1225	.1108	.1003	.0907	.0821	.0743	.0672	.0608	.0550	.0498	.0450	.0408	.0369	1
	.3230	.3106	.2975	.2842	.2707	.2572	.2438	.2306	.2177	.2052	.1931	.1815	.1703	.1596	.1494	.1397	.1304	.1217	1
	.2584	.2640	.2678	.2700	.2707	.2700	.2681	.2652	.2613	.2565	.2510	.2450	.2384	.2314	.2240	.2165	.2087	.2008	1
	.1378	.1496	.1607	.1710	.1804	.1890	.1966	.2033	.2090	.2138	.2176	.2205	.2225	.2237	.2240	.2237	.2226	.2209	1
	.0551	.0636	.0723	.0812	.0902	.0992	.1082	.1169	.1254	.1336	.1414	.1488	.1557	.1622	.1680	.1733	.1781	.1823	1
5	.0176	.0216	.0260	.0309	.0361	.0417	.0476	.0538	.0602	.0668	.0735	.0804	.0872	.0940	.1008	.1075	.1140	.1203	
	.0047	.0061	.0078	.0098	.0120	.0146	.0174	.0206	.0241	.0278	.0319	.0362	.0407	.0455	.0504	.0555	.0608	.0662	1
	.0011	.0015	.0020	.0027	.0034	.0044	.0055	.0068	.0083	.0099	.0118	.0139	.0163	.0188	.0216	.0246	.0278	.0312	1
	.0002	.0003	.0005	.0006	.0009	.0011	.0015	.0019	.0025	.0031	.0038	.0047	.0057	.0068	.0081	.0095	.0111	.0129	1
	.0000	.0001	.0001	.0001	.0002	.0003	.0004	.0005	.0007	.0009	.0011	.0014	.0018	.0022	.0027	.0033	.0040	.0047	1
)	.0000	.0000	.0000	.0000	.0000	.0001	.0001	.0001	.0002	.0002	.0003	.0004	.0005	.0006	.0008	.0010	.0013	.0016	
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0001	.0001	.0002	.0002	.0003	.0004	.0005	1
2	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0001	.0001	.0001	1
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	
	3.40	3.50	3.60	3.70	3.80	3.90	4.00	4.10	4.20	4.30	4,40	4.50	4.60	4.70	4.80	4.90	5.00	5.10	11
Ť	.0334	.0302	.0273	.0247	.0224	.0202	.0183	.0166	.0150	.0136	.0123	.0111	.0101	.0091	.0082	.0074	.0067	.0061	٦
	.1135	.1057	.0273	.0247	.0850	.0789	.0733	.0679	.0630	.0583	.0540	.0500	.0462	.0427	.0395	.0365	.0337	.0311	1
	.1929	.1850	.1771	.1692	.1615	.1539	.1465	.1393	.1323	.1254	.1188	.1125	.1063	.1005	.0948	.0894	.0842	.0793	1
	.2186	.2158	.2125	.2087	.2046	.2001	.1954	.1904	.1852	.1798	.1743	.1687	.1631	.1574	.1517	.1460	.1404	.1348	
	.1858	.1888	.1912	.1931	.1944	.1951	.1954	.1951	.1944	.1933	.1917	.1898	.1875	.1849	.1820	.1789	.1755	.1719	
	.1264	.1322	.1377	.1429	.1477	.1522	.1563	.1600	.1633	.1662	.1687	.1708	.1725	.1738	.1747	.1753	.1755	.1753	
	.0716	.0771	.0826	.0881	.0936	.0989	.1042	.1093	.1143	.1191	.1237	.1281	.1323	.1362	.1398	.1432	.1462	.1490	1
	.0348	.0385	.0425	.0466	.0508	.0551	.0595	.0640	.0686	.0732	.0778	.0824	.0869	.0914	.0959	.1002	.1044	.1086	1
	.0148	.0169	.0191	.0215	.0241	.0269	.0298	.0328	.0360	.0393	.0428	.0463	.0500	.0537	.0575	.0614	.0653	.0692	1
	.0056	.0066	.0076	.0089	.0102	.0116	.0132	.0150	.0168	.0188	.0209	.0232	.0255	.0281	.0307	.0334	.0363	.0392	1
)	.0019	.0023	.0028	.0033	.0039	.0045	.0053	.0061	.0071	.0081	.0092	.0104	.0118	.0132	.0147	.0164	.0181	.0200	
	.0006	.0007	.0009	.0011	.0013	.0016	.0019	.0023	.0027	.0032	.0037	.0043	.0049	.0056	.0064	.0073	.0082	.0093	
	.0002	.0002	.0003	.0003	.0004	.0005	.0006	.0008	.0009	.0011	.0013	.0016	.0019	.0022	.0026	.0030	.0034	.0039	
	.0000	.0001	.0001	.0001	.0001	.0002	.0002	.0002	.0003	.0004	.0005	,0006	.0007	.0008	.0009	.0011	.0013	.0015	
	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0001	.0001	.0001	.0001	.0002	.0002	.0003	.0003	.0004	.0005	.0006	
,	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0001	.0001	.0001	.0001	.0002	.0002	
STATE OF		2222	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0001	1
	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	- 1

Prob (X = x)

The main uses of the Poisson distribution are as an approximation to binomial distributions having large n and small p (for notation see page 4) and as a description of the occurrence of random events over time (or other continua). Individual probabilities are given on pages 14-16 for a wide range of values of the mean  $\mu$ , and cumulative probabilities are obtained from the Poisson probability chart on page 17.

EXAMPLES: A production process is supposed to have a 1% rate of defectives. In a random sample of size eighty, what is the probability of there being (a) exactly two defectives, and (b) at least two defectives? The number X of defectives has a binomial distribution with n=80 and p=0.01; its mean  $\mu$  is  $np=80\times0.01=0.8$ . This distribution is well approximated by the Poisson distribution having the same mean,  $\mu=0.8$ . So immediately we find (a) Prob (X=2) = 0.1438. For (b) Prob (X=2) we can

use the chart on page 17 directly. However this probability can also be found by noting that  $\operatorname{Prob}(X \ge 2) = 1 - \operatorname{Prob}(X \le 1) = 1 - \{\operatorname{Prob}(X = 0) + \operatorname{Prob}(X = 1)\} = 1 - \{0.4993 + 0.3595\} = 0.1912$ , using the above table.

A binomial distribution with large n and a p-value close to 1 may also be dealt with by means of a Poisson approximation if the problem is re-expressed in terms of a small p-value. For example if a treatment has a 90% (p=0.9) success-rate, what is the probability that exactly 95 out of 100 treated patients recover? This is the same as asking what is the probability that exactly 5 patients out of 100 fail to recover when the failure-rate is 10% or 0.1. That is we want Prob (X=5) in the binomial distribution with n=100 and p=0.1 which can be approximated by the Poisson distribution with mean  $\mu=np=100\times0.1=10.0$ . From page 15, this probability is found to be 0.0378.

									Prob	(X = x)	7								
X"	5.20	5.30	5.40	5.50	5.60	5.70	5.80	5.90	6.00	6.10	6.20	6.30	6.40	6.50	6.60	6.70	6.80	6.90	1/x
0	.0055	.0050	.0045	.0041	.0037	.0033	.0030	.0027	.0025	.0022	.0020	.0018	.0017	.0015	.0014	.0012	.0011	.0010	0
1 2	.0287	.0265	.0244	.0225	.0207	.0191	.0176	.0162	.0149	.0137	.0126	.0116	.0106	.0098	.0090	.0082	.0076	.0070	1
3	.1293	.1239	.1185	.1133	.1082	.1033	.0985	.0938	.0892	.0848	.0806	.0765	.0726	.0688	.0652	.0617	.0584	.0552	3
4	.1681	.1641	.1600	.1558	.1515	.1472	.1428	.1383	.1339	.1294	.1249	.1205	.1162	.1118	.1076	.1034	.0992	.0952	4
5	.1748	.1740	.1728	.1714	.1697	.1678	.1656	.1632	.1606	.1579	.1549	.1519	.1487	.1454	.1420	.1385	.1349	.1314	5
6	.1515	.1537	.1555	.1571	.1584	.1594	.1601	.1605	.1606	.1605	.1601	.1595	.1586	.1575	.1562	.1546	.1529	.1511	7
8	.0731	.0771	.0810	.0849	.0887	.0925	.0962	.0998	.1033	.1066	.1099	.1130	.1160	.1188	.1215	.1240	.1263	.1284	8
9	.0423	.0454	.0486	.0519	.0552	.0586	.0620	.0654	.0688	.0723	.0757	.0791	.0825	,0858	.0891	.0923	.0954	.0985	9
	.0220	.0241	.0262	.0285	.0309	.0334	.0359	.0386	.0413	.0441	.0469	.0498	.0528	.0558	.0588	.0618	.0649	.0679	10
11	.0104	.0116	.0129	.0143	.0157	.0173	.0190	.0207	.0225	.0244	.0265	.0285	.0307	.0330	.0353	.0377	.0401	.0426	112
13	.0018	.0021	.0024	.0028	.0032	.0036	.0041	.0046	.0052	.0058	.0065	.0073	.0081	.0089	.0099	.0108	.0119	.0130	13
14	.0007	.0008	.0009	.0011	.0013	.0015	.0017	.0019	.0022	.0025	.0029	.0033	.0037	.0041	.0046	.0052	.0058	.0064	14
16	.0001	.0001	.0001	.0001	.0003	.0002	.0002	.0003	.0003	.0004	.0005	.0005	.0006	.0007	.0008	.0010	.0011	.0013	16
17	.0000	.0000	,0000	.0000	.0002	.0002	.0002	.0003	.0003	.0004	.0003	.0003	.0002	.0007	.0003	.0004	.0004	.0005	17
18	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0001	.0001	.0001	.0001	.0001	.0002	.0002	18
19	.0000	.0000	.0000.	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0001	.0001	19
20	.0000	.0000	.0000	.0000	.0000	.0000	.0000	0000,	,0000	.0000	.0000.	.0000	.0000	.0000	.0000	.0000	.0000	.0000	-
X	7.00	7.10	7.20	7,30	7,40	7.50	7.60	7,70	7.80	7.90	8.00	8.10	8.20	8.30	8.40	8.50	8.60	8.70	11/x
0	.0009	.0008	.0007	.0007	.0006	.0006	.0005	.0005	.0004	.0004	.0003	.0003	.0003	.0002	.0002	.0002	.0002	.0002	0
1	.0064	.0059	.0054	.0049	.0045	.0041	.0038	.0035	.0032	.0029	.0027	.0025	.0023	.0021	.0019	.0017	.0016	.0014	1
2	.0223	.0208	.0194	.0180	.0167	.0156	.0145	.0134	.0125	.0116	.0107	.0100	.0092	.0086	.0079	.0074	.0068	.0063	3
4	.0912	.0874	.0836	.0799	.0764	.0729	.0696	.0663	.0632	.0602	.0573	.0544	.0517	.0491	.0466	.0443	.0420	.0398	4
5	.1277	.1241	.1204	.1167	.1130	.1094	.1057	.1021	.0986	.0951	.0916	.0882	.0849	.0816	.0784	.0752	.0722	.0692	5
6	.1490	.1468	.1445	.1420	.1394	.1367	.1339	.1311	.1282	.1252	.1221	.1191	.1160	.1128	.1097	.1066	.1034	.1003	6
7 8	.1490	.1321	.1486	.1481	.1474	.1465	.1454	.1442	.1428	.1413	.1396	.1378	.1358	.1338	.1317	.1294	.1271	.1247	7
9	.1014	.1042	.1070	.1096	.1121	.1144	.1167	.1187	.1207	.1224	.1241	.1256	.1269	.1280	.1290	.1299	.1306	.1311	9
10	.0710	.0740	.0770	.0800	.0829	.0858	.0887	.0914	.0941	.0967	.0993	,1017	.1040	.1063	.1084	.1104	.1123	.1140	10
11 12	.0452	.0478	.0504	.0531	.0558	.0585	.0613	.0640	.0667	.0695	.0722	.0749	.0776	.0802	.0828	.0853	.0878	.0902	11
13	.0142	.0154	.0168	.0181	.0196	.0211	.0227	.0243	.0260	.0278	.0296	.0315	.0334	.0354	.0374	.0395	.0416	.0438	13
14	.0071	.0078	.0086	.0095	.0104	.0113	.0123	.0134	.0145	.0157	.0169	.0182	.0196	.0210	.0225	.0240	.0256	.0272	14
15	.0033	.0037	.0041	.0046	.0051	.0057	.0062	.0069	.0075	.0083	.0090	.0098	.0107	.0116	.0126	.0136	.0147	.0158	15
16	.0014	.0016	.0019	.0021	.0024	.0026	.0030	.0033	.0037	.0041	.0045	.0050	.0055	.0060	.0066	.0072	.0079	.0086	16
18	.0002	.0003	.0003	.0004	.0004	.0005	.0006	.0006	.0007	.0008	.0009	.0011	.0012	.0014	.0015	.0017	.0019	.0021	18
19 20	.0001	.0001	.0001	.0001	.0002	.0002	.0002	.0003	.0003	.0003	.0004	.0005	.0005	.0006	.0007	.0008	.0009	.0010	19
21	.0000	.0000	.0000	.0001	.0001	.0001	.0001	.0001	.0001	.0001	.0002	.0002	.0002	.0002	.0003	.0003	.0004	.0004	20
22	,0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0002	.0002	22
23	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	23
L	8.80	8.90	9.00	9.10	9.20	9.30	9.40	9.50	9.60	9.70	9.80	9.90	10.00	10.50	11.00	11.50	12.00	12.50	11/
X O	.0002	.0001	.0001	.0001	.0001	.0001	.0001	.0001	.0001	.0001	.0001	.0001	.0000	.0000	.0000	.0000	.0000	.0000	×
1	.0013	.0012	.0011	.0010	.0009	.0009	.0008	.0007	.0007	.0006	.0005	.0005	.0005	.0003	.0002	.0001	.0001	.0000	1
2	.0058	.0054	.0050	.0046	.0043	.0040	.0037	.0034	.0031	.0029	.0027	.0025	.0023	.0015	.0010	.0007	.0004	.0003	2
3 4	.0171	.0160	.0150	.0140	.0131	.0123	.0115	.0107	.0100	.0093	.0087	.0081	.0076	.0053	.0037	.0026	.0018	.0012	3
5	.0663	.0635	.0607	.0581	.0555	.0530	.0506	.0483	.0460	.0439	.0418	.0398	.0378	.0293	.0224	.0170	.0127	.0095	5
6	.0972	.0941	.0911	.0881	.0851	.0822	.0793	.0764	.0736	.0709	.0682	.0656	.0631	.0513	.0411	.0325	.0255	.0197	6
7	.1222	.1197	.1171	.1145	.1118	.1091	.1064	.1037	.1010	.0982	.0955	.0928	.0901	.0769	.0646	.0535	.0437	.0353	7 8
8	.1315	.1317	.1318	.1302	.1286	.1269	.1251	.1232	.1212	.1191	.1170	.1148	.1126	.1009	.0888	.0769	.0874	.0551	9
10	.1157	.1172	.1186	.1198	.1210	.1219	.1228	.1235	.1241	.1245	.1249	.1250	.1251	.1236	.1194	.1129	.1048	.0956	10
11	.0925	.0948	.0970	.0991	.1012	.1031	.1049	.1067	.1083	.1098	.1112	.1125	.1137	.1180	.1194	.1181	.1144	.1087	11
12	.0679	.0703	.0728	.0752	.0776	.0799	.0822	.0844	.0866	.0888	.0908	.0928	.0948	.1032	.1094	.1131	.1144	.1132	12
14	.0289	.0306	.0324	.0342	.0361	.0380	.0399	.0419	.0439	.0459	.0479	.0500	.0521	.0625	.0728	.0822	.0905	.0972	14
15	.0169	.0182	.0194	,0208	.0221	.0235	.0250	.0265	.0281	.0297	.0313	.0330	.0347	.0438	.0534	.0630	.0724	.0810	15
16	.0093	.0101	.0109	.0118	.0127	.0137	.0147	.0157	.0168	.0180	.0192	.0204	.0217	.0287	.0367	.0453	.0543	.0633	16
17	.0048	.0053	.0058	.0063	.0069	.0075	.0081	.0088	.0095	.0103	.0111	.0119	.0128	.0177	.0237	.0306	.0383	.0465	17 18
19	.0024	.0026	.0029	.0032	.0035	.0039	.0042	.0023	.0026	.0055	.0060	.0034	.0071	.0104	.0084	.0119	.0255	.0323	19
20	.0005	.0005	.0006	.0007	.0008	.0009	.0010	.0011	.0012	.0014	.0015	.0017	.0019	.0030	.0046	.0068	.0097	.0133	20
21	.0002	.0002	.0003	.0003	.0003	.0004	.0004	.0005	.0006	.0006	.0007	.0008	.0009	.0015	.0024	.0037	.0055	.0079	21
22	.0001	.0001	.0001	.0001	.0001	.0002	.0002	.0002	.0002	.0003	.0003	.0004	.0004	.0007	.0012	.0020	.0030	.0045	22
24	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	,0000	.0001	.0002	.0002	.0003	.0003	.0005	.0008	.0024	24
25	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0001	.0002	.0004	.0006	25
26	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0002	.0003	26
27	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0001	27
29	.0000	.0000	.0000	.0000	.0000	,0000,	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	29
-											_								_

Prob (X = x)

Prob (X = x)

								1	100 11										
1	13.00	13.50	14.00	14.50	15.00	16.00	17.00	18.00	19.00	20.00	21.00	22.00	23.00	24.00	25.00	30.00	40.00	50.00	11/x
×	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	,0000	.0000	0
1	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	,0000	.0000	1
2	.0002	.0001	.0001	.0001	.0000	.0000	.0000	.0000	.0000	.0000	,0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	2
3	.0008	.0006	.0004	.0003	.0002	.0001	.0000	.0000	.0000	.0000		.0000	.0000	.0000	.0000	.0000	.0000	.0000	3
4	.0027	.0019	.0013	.0009	.0006	.0003	.0001	.0001	.0000	.0000		.0000	.0000	.0000	.0000	.0000	.0000	.0000	5
5	.0070	.0051	.0037	.0027	.0019	.0010	.0005	.0002	.0001	.0001	500 9 100 D 100 D 100 D 1	.0000	.0000	.0000	.0000	.0000	.0000	.0000	1000000
6	.0152	.0115	.0087	.0065	.0048	.0026	.0014	.0007	.0004	.0002		.0000	.0000	.0000	.0000	.0000	,0000	.0000	6
7	.0281	.0222	.0174	.0135	.0104	.0060	.0034	.0019	.0010	.000		.0001	.0001	.0000	.0000	.0000	.0000	.0000	8
8	.0457	.0375	.0304	.0244	.0194	.0120	.0072	.0042	.0024	.0013		.0004	.0002	.0001	.0001	,0000	.0000	.0000	9
9	.0661	.0563	.0473	.0394	.0324	.0213	.0135	.0083	.0050	.0029		.0009	.0003	.0003	.0004	.0000	.0000	.0000	10
10	.0859	.0760	.0663				-				10.00010				200000000000000000000000000000000000000				20000
11	.1015	.0932	.0844	.0753	.0663	.0496	.0355	.0245	.0164	.0106		.0041	.0024	.0014	8000.	.0000	.0000	.0000	11
12	.1099	.1049	.0984	.0910	.0829	.0661	.0504	.0368	.0259	.0176		.0075	.0047	.0029	.0017	.0001	.0000	.0000	13
13	.1099	.1089	.1060	.1014	.0956	.0814	.0658	.0509	.0378	.027		.0127	.0083	.0053	.0033	.0002	.0000	.0000	14
14	.1021	.1050	.1060	.1051	.1024	.0930	.0800	.0655	.0514	.0387		.0292	.0209	.0146	.0099	,0010	.0000	.0000	15
15	.0885	.0945	.0989	.1016	.1024									3-91-3-6-5	1000100000		Topological Co.		100000
16	.0719	.0798	.0866	.0920	.0960	.0992	.0963	.0884	.0772	.0646		.0401	.0301	.0219	.0155	.0019	,0000	.0000	16
17	.0550	.0633	.0713	.0785	.0847	.0934	.0963	.0936	.0863	.0760		.0520	.0407	.0309	.0227	.0034	.0000	.0000	18
18	.0397	.0475	.0554	.0632	.0706	.0830	.0909	.0936	.0911	.0844		.0635	.0520	.0520	.0316	,0089	.0001	.0000	19
19	.0272	.0337	.0409	.0483	.0557	.0699	.0814	.0887	.0911	.0888		.0735	.0724	.0624	.0519	.0134	.0001	.0000	20
20	.0177	.0228	.0286	.0350	775-05-05-0	1000000				-		-		.0713		.0192	.0004	.0000	21
21	.0109	.0146	.0191	.0242	.0299	.0426	.0560	.0684	.0783	.0846		.0847	.0793	.0778	.0618	.0192	.0004	.0000	22
22	.0065	.0090	.0121	.0159	.0204	.0310	.0433	.0560	.0676	.0769		.0847	.0829	.0812	.0763	.0201	.0007	.0000	23
23	.0037	.0053	.0074	.0100	.0133	.0216	.0320	.0328	.0442	.055		.0743	.0794	.0812	.0795	.0426	.0019	.0000	24
25	.0020	.0030	.0043	.0035	.0050	.0092	.0154	.0237	.0336	.0446		.0654	.0731	.0779	.0795	.0511	.0031	.0000	25
26	.0005	.0008	.0013	.0020	.0029	.0057	.0101	.0164	.0246	.0343		.0553	.0646	.0719	.0765	.0590	.0047	.0001	26
27	.0003	.0004	.0007	.0020	.0025	.0034	.0063	.0109	.0173	.0254		.0451	.0551	.0639	.0708	.0655	.0070	.0001	27
28	.0002	.0004	.0003	.0005	.0009	.0019	.0038	.0070	.0117	,0181		.0354	.0452	.0548	.0632	.0702	.0100	.0002	28
29	.0001	.0001	.0002	.0003	.0004	.0011	.0023	.0044	.0077	.0125		.0269	.0359	.0453	.0545	.0726	.0138	.0004	29
30	.0000	.0000	.0001	.0001	.0002	.0006	.0013	.0026	.0049	.008	.0133	.0197	.0275	.0363	.0454	.0726	.0185	.0007	30
31	.0000	.0000	.0000	.0001	.0001	.0003	.0007	.0015	.0030	.0054	.0090	.0140	.0204	.0281	.0366	.0703	.0238	.0011	31
32	.0000	.0000	.0000	.0000	.0001	.0001	.0004	.0009	.0018	.0034	.0059	.0096	.0147	.0211	.0286	.0659	.0298	.0017	32
33	.0000	.0000	.0000	.0000	.0000	.0001	.0002	.0005	.0010	.0020	.0038	.0064	.0102	.0153	.0217	.0599	.0361	.0026	33
34	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0002	.0006	.0012	.0023	.0041	.0069	.0108	.0159	.0529	.0425	.0038	34
35	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0003	.000	.0014	.0026	.0045	.0074	.0114	.0453	.0485	.0054	35
36	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0002	.0004	.0008	.0016	.0029	.0049	.0079	.0378	.0539	.0075	36
37	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.000	.0005	.0009	.0018	.0032	.0053	.0306	.0583	.0102	37
38	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.000	.0003	.0005	.0011	.0020	.0035	.0242	.0614	.0134	38
39	.0000	.0000	.0000	.0000	,0000	.0000	.0000	.0000	.0000	.000		.0003	.0006	.0012	.0023	.0186	.0629	.0172	39
40	.0000	.0000	.0000	,0000	.0000	.0000	.0000	.0000	,0000	,000	,0001	.0002	.0004	.0007	.0014	.0139	.0629	.0215	40
41	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	,0002	.0004	.0009	.0102	,0614	.0262	41
42	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000		.0000	.0001	.0003	.0005	.0073	,0585	.0312	42
43	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000		.0000	.0001	.0001	.0003	.0051	.0544	.0363	43
44	.0000	,0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000		.0000	.0000	.0001	.0002	.0035	.0495	.0412	44
45	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	,000		.0000	.0000	.0000	.0001	.0023			1000000
46	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000		.0000	.0000	.0000	.0001	.0015	.0382	.0498	46
47	,0000	.0000	.0000	.0000	.0000	.0000	.0000	,0000	,0000	,0000		.0000	.0000	.0000	.0000	.0010	.0325	.0530	48
48	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000		.0000	.0000	.0000	.0000	.0006	.0271	.0563	49
49	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000		.0000	.0000	.0000	.0000	.0004	.0177	.0563	50
50	.0000	,0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	,000	,0000	,0000	.0000	.0000	1	-		.0552	51
															.0000	.0001	.0139	UDDZ	1 31

The Poisson probability chart on page 17 gives cumulative probabilities of the form  $\operatorname{Prob}(X\geqslant x)$  where X has a Poisson distribution with mean  $\mu$  in the range  $0.01\leqslant \mu\leqslant 100$ . To find such a probability, locate the appropriate value of  $\mu$  on the right-hand vertical axis, trace back along the horizontal to the line or curve labelled with the desired value of x, and read off the probability on the horizontal axis. The horizontal scale is designed to give most accuracy in the tails of the distribution, i.e. where the probabilities are close to 0 or 1, and the vertical scale has been devised to make the curves almost linear.

EXAMPLES: A production process is supposed to have a 1% rate of defectives. In a random sample of size eighty, what is the probability of there being at least two defectives? This question has already been answered on p. 14 using individual probabilities. Here we may read off the probability directly, following the above directions with  $\mu=0.8$  and x=2, giving Prob  $(X\geqslant 2)=0.19$ . Obviously, accuracy may be somewhat limited when using the chart.

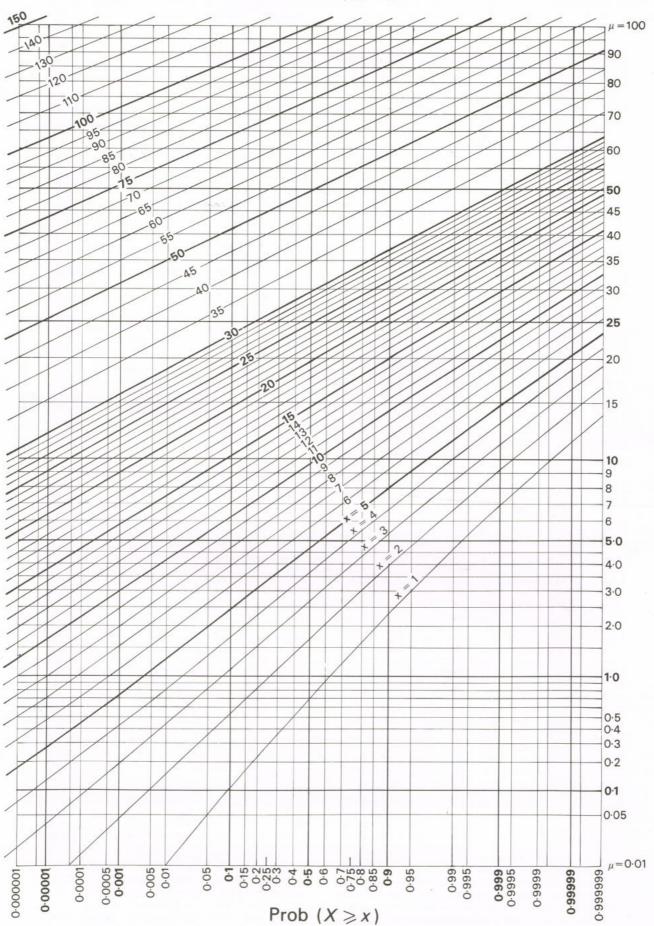
Probabilities of events such as  $X \le 2$  can also be easily found. For Prob  $(X \le 2) = 1 - \text{Prob}(X \ge 3)$ , and Prob  $(X \ge 3)$  is seen to be just less than 0.05, say 0.048, giving Prob  $(X \le 2) = 1 - 0.048 = 0.952$ .

As a final example, suppose the number X of serious road accidents per week in a certain region has a Poisson distribution with mean  $\mu=2.0$ . What is the probability of there being no more than three accidents in a particular week? This again can be calculated using either individual probabilities or the chart. From page 14, the probabilities of 0, 1, 2 or 3 accidents are respectively 0.1353, 0.2707, 0.2707 and 0.1804, and adding these we have  $\text{Prob}(X \leq 3) = 0.8571$ . Using the chart, since  $\text{Prob}(X \leq 3) = 1 - \text{Prob}(X \geq 4)$ , we obtain  $\text{Prob}(X \leq 3) = 1 - 0.14 = 0.86$ .

.0000	.0004	.0221	.0000	
.0000	.0002	.0177	.0563	50
.0000	.0001	.0139	.0552	51
.0000	.0001	.0107	.0531	52
.0000	.0000	.0081	.0501	53
.0000	.0000	.0060	.0464	54
.0000	.0000	.0043	.0422	55
.0000	.0000	.0031	.0376	56
.0000	.0000	.0022	.0330	57
.0000	.0000	.0015	.0285	58
.0000	.0000	.0010	.0241	59
.0000	.0000	.0007	.0201	60
.0000	.0000	.0004	.0165	61
.0000	.0000	.0003	.0133	62
.0000	.0000	.0002	.0105	63
.0000	.0000	.0001	.0082	64
.0000	.0000	.0001	.0063	65
.0000	.0000	.0000	.0048	66
.0000	.0000	.0000	.0036	67
.0000	.0000	.0000	.0026	68
.0000	.0000	.0000	,0019	69
.0000	.0000	.0000	.0014	70
.0000	.0000	.0000	.0010	71
.0000	.0000	.0000	.0007	72
.0000	.0000	.0000	.0005	73
.0000	,0000	.0000	.0003	74
.0000	.0000	.0000	.0002	75
.0000	.0000	.0000	.0001	76
.0000	.0000	.0000	.0001	77
.0000	.0000	.0000	.0001	78
.0000	.0000	.0000	.0000	79

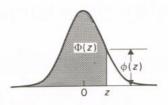
## Poisson probability chart (cumulative probabilities)

Prob 
$$(X \geqslant x) = \sum_{r=x}^{\infty} e^{-\mu} \cdot \frac{\mu^r}{r!}$$



# Probabilities and ordinates in the normal distribution

$$\phi(z) = \frac{1}{\sqrt{2\pi}} e^{-\frac{1}{2}z^2}; \quad \Phi(z) = \text{Prob}(Z \le z) = \int_{-\infty}^{z} \phi(t) dt$$



φ(z)	z	0	1	2	3	4	5	6	7	8	9									
0.08 608	- 6.0	0.09987	09928	0°872	0°820	0 <sup>9</sup> 771	0 <sup>9</sup> 724	0°681	0° 640	09601	0°565									
0.0 <sup>7</sup> 110	-5.9	0.08 182	08 171	08 161	08 151	0 <sup>8</sup> 143	0 <sup>8</sup> 134	0 <sup>8</sup> 126	0 <sup>8</sup> 119	08 112	08 105									
0.0 <sup>7</sup> 198	-5.8	0.08332	08312	08 294	08277	08 261	08 246	08 231	0 <sup>8</sup> 218	08 205	0 <sup>8</sup> 193 0 <sup>8</sup> 352									
0.07351	-5.7	0.08599	0 <sup>8</sup> 565	0 <sup>8</sup> 533 0 <sup>8</sup> 955	0 <sup>8</sup> 502 0 <sup>8</sup> 901	0 <sup>8</sup> 473 0 <sup>8</sup> 850	08 446 08 802	08421 08757	08396 08714	08374 08673	08635						en es osa			
0.07618	-5.6 -5.5	0.0 <sup>7</sup> 107 0.0 <sup>7</sup> 190	0 <sup>7</sup> 101 0 <sup>7</sup> 179	0°955	07160	0° 850	0 802	07135	07127	07120	07114				persc					
0.06 108		345747			07282	07266	07252	0 <sup>7</sup> 238	0 <sup>7</sup> 225	07213	07201				ndica )8182					
0.06186	-5.4 -5.3	0.0 <sup>7</sup> 333 0.0 <sup>7</sup> 579	0 <sup>7</sup> 315 0 <sup>7</sup> 548	0 <sup>7</sup> 298 0 <sup>7</sup> 519	07491	07465	07440	07416	07394	07372	07352				83 =				001	04,
0.0 <sup>6</sup> 317 0.0 <sup>6</sup> 536	-5.2	0.0 579	07944	07895	07848	07803	07760	0 <sup>7</sup> 720	0 <sup>7</sup> 682	07646	07612	ar	ia o	.0-4	03 -	0.00	0 40	٥.		
0.0 897	- 5.1	0.06 170	0 <sup>6</sup> 161	0 <sup>6</sup> 153	0 <sup>6</sup> 145	0 <sup>6</sup> 137	0 <sup>6</sup> 130	0 <sup>6</sup> 123	0 <sup>6</sup> 117	0 <sup>6</sup> 111	0 <sup>6</sup> 105									
0.05 149	-5.0	0.06287	0 <sup>6</sup> 272	0 <sup>6</sup> 258	0 <sup>6</sup> 245	0 <sup>6</sup> 233	0 <sup>6</sup> 221	0 <sup>6</sup> 210	0 <sup>6</sup> 199	0 <sup>6</sup> 189	0 <sup>6</sup> 179									
0.05 244	-4.9	0.06479	0 <sup>6</sup> 455	0 <sup>6</sup> 433	06411	0 <sup>6</sup> 391	0 <sup>6</sup> 371	06352	06335	06318	06302									
0.05396	- 4.8	0.0 <sup>6</sup> 793	0 <sup>6</sup> 755	06718	06 683	0 <sup>6</sup> 649	0 <sup>6</sup> 617	0 <sup>6</sup> 587	0°558	0 <sup>6</sup> 530	0 <sup>6</sup> 504									
0.05 637	- 4.7	0.05 130	05 124	0 <sup>5</sup> 118	05112	0 <sup>5</sup> 107	05102	06968	0 <sup>6</sup> 921 0 <sup>5</sup> 151	0 <sup>6</sup> 876 0 <sup>5</sup> 143	0 <sup>6</sup> 834 0 <sup>5</sup> 137									
0.04 101	- 4.6	0.05211	05 201	0 <sup>5</sup> 192 0 <sup>5</sup> 309	0 <sup>5</sup> 183	0 <sup>5</sup> 174 0 <sup>5</sup> 281	0 <sup>5</sup> 166 0 <sup>5</sup> 268	0 <sup>5</sup> 158 0 <sup>5</sup> 256	05 244	05232	05222		De	ono	rtiona	l nai	rte h	ave n	ot h	neen
0.0 <sup>4</sup> 160	- 4.5	0.05340	0 <sup>5</sup> 324	200	100 200	100.000000				0 <sup>5</sup> 373	0 <sup>5</sup> 356	oi			this					
0.0 <sup>4</sup> 249	- 4.4	0.05541	05517	05 494	0 <sup>5</sup> 471 0 <sup>5</sup> 746	0 <sup>5</sup> 450 0 <sup>5</sup> 712	05429 05681	0 <sup>5</sup> 410 0 <sup>5</sup> 650	05391 05621	0° 573	0° 567				ot be					
0.04385	- 4.3 - 4.2	0.0 <sup>5</sup> 854 0.0 <sup>4</sup> 133	0 <sup>5</sup> 816 0 <sup>4</sup> 128	0 <sup>5</sup> 780 0 <sup>4</sup> 122	04117	04112	04 107	0 <sup>4</sup> 102	05977	05934	05893									
0.0 <sup>4</sup> 589 0.0 <sup>4</sup> 893	-4.1	0.0 133	04 198	04 189	04 181	0 <sup>4</sup> 174	04 166	04 159	0 <sup>4</sup> 152	0 <sup>4</sup> 146	04 139									
0.0 033	-4.0	0.04317	04304	04291	04 279	04 267	0 <sup>4</sup> 256	04245	04235	04225	04216									
0.03 199	3.9	0.04481	0 <sup>4</sup> 461	04443	0 <sup>4</sup> 425	0 <sup>4</sup> 407	04391	0 <sup>4</sup> 375	0 <sup>4</sup> 359	0 <sup>4</sup> 345	04 330									
0.0 199	-3.8	0.04723	0 <sup>4</sup> 695	04667	04641	04615	0 <sup>4</sup> 591	0 <sup>4</sup> 567	0 <sup>4</sup> 544	0 <sup>4</sup> 522	0 <sup>4</sup> 501									
0.03 425	- 3.7	0.0 <sup>3</sup> 108	0 <sup>3</sup> 104	04996	04957	04920	0 <sup>4</sup> 884	04850	0 <sup>4</sup> 816	0 <sup>4</sup> 784	0 <sup>4</sup> 753									
0.03612	-3.6	0.0 <sup>3</sup> 159	0 <sup>3</sup> 153	0 <sup>3</sup> 147	0 <sup>3</sup> 142	0 <sup>3</sup> 136	03131	0 <sup>3</sup> 126	03 121	0 <sup>3</sup> 117 0 <sup>3</sup> 172	0 <sup>3</sup> 112 0 <sup>3</sup> 165	_		_	0.99	.Zustava				
0.03873	- 3.5	0.0 <sup>3</sup> 233	0 <sup>3</sup> 224	0 <sup>3</sup> 216	0 <sup>3</sup> 208	0 <sup>3</sup> 200	0 <sup>3</sup> 193	0 <sup>3</sup> 185	0 <sup>3</sup> 178	75.000						BTRA		DTC		-
0.00123	- 3.4	0.0 <sup>3</sup> 337	0 <sup>3</sup> 325	0 <sup>3</sup> 313	0 <sup>3</sup> 302	03 291	0 <sup>3</sup> 280	03270	03260	0 <sup>3</sup> 251 0 <sup>3</sup> 362	0 <sup>3</sup> 242 0 <sup>3</sup> 349			PH	OPORT	IONA	AL PA	nis		
0.00172	- 3.3	0.03483	0 <sup>3</sup> 466	0 <sup>3</sup> 450	03434	0 <sup>3</sup> 419 0 <sup>3</sup> 598	0 <sup>3</sup> 404 0 <sup>3</sup> 577	0 <sup>3</sup> 390 0 <sup>3</sup> 557	0 <sup>3</sup> 376 0 <sup>3</sup> 538	0°362	0° 349	1	2	3	4	5	6	7	8	9
0.00238	-3.2 -3.1	0.0 <sup>3</sup> 687 0.0 <sup>3</sup> 968	0 <sup>3</sup> 664 0 <sup>3</sup> 935	0 <sup>3</sup> 641 0 <sup>3</sup> 904	0 <sup>3</sup> 619 0 <sup>3</sup> 874	0° 598	0 877	0° 337	0 <sup>3</sup> 762	0 <sup>3</sup> 736	0 <sup>3</sup> 711									
0.00327	-3.0	0.00135	00131	00126	00122	00118	00114	00111	00107	00104	00100	0	1	1	2	2	2	3	3	3
	-2.9	0.00187	00181	00175	00169	00164	00159	00154	00149	00144	00139	1	1	2	2	3	3	4	4	5
0.00595	-2.8	0.00187	00181	00240	00233	00226	00219	00212	00205	00199	00193	1	1	2	3	3	4	5	6	6
0.0104	-2.7	0.00347	00336	00326	00317	00307	00298	00289	00280	00272	00264	1	2	3	4	5	5	6	7	8
0.0136	-2.6	0.00466	00453	00440	00427	00415	00402	00391	00379	00368	00357	1 2	2	5	5	6	7 9	8	12	14
0.0175	- 2.5	0.00621	00604	00587	00570	00554	00539	00523	00508	00494	00480				_			14	16	18
0.0224	-2.4	0.00820	00798	00776	00755	00734	00714	00695	00676	00657	00639 0084	0	0	6	8	10	12	2	2	2
0.0283	-2.3	0.0107	0104	0102	0099	0096 0125	0094	0091	0089	0087	0110	0	1	1	1	2	2	2	3	3
0.0355	-2.2 -2.1	0.0139	0136 0174	0132	0129 0166	0162	0158	0154	0150	0146	0143	0	1	1	2	2	2	3	3	4
0.0440	-2.1	0.0179	0222	0217	0212	0207	0202	0197	0192	0188	0183	0	1	1	2	2	3	3	4	4
		0.0287	0281	0274	0268	0262	0256	0250	0244	0239	0233	1	1	2	2	3	4	4	5	5
0.0656	-1.9 -1.8	0.0287	0351	0344	0336	0329	0322	0314	0307	0301	0294	1	1	2	3	4	4	5	6	6
0.0940	-1.7	0.0446	0436	0427	0418	0409	0401	0392	0384	0375	0367	1	2	3	3	4	5	6 7	7	8
0.1109	-1.6	0.0548	0537	0526	0516	0505	0495	0485	0475	0465	0455	1	2	3	4 5	6	6	8	10	11
0.1295	-1.5	0.0668	0655	0643	0630	0618	0606	0594	0582	0571	0559	1				_		7/	77775	1000
0.1497	-1.4	0.0808	0793	0778	0764	0749	0735	0721	0708	0694	0681	1	3	4	6	7	10	10	11	13
0.1714	- 1.3	0.0968	0951	0934	0918	0901	0885	0869	0853	0838	0823 0985	2 2	3	5	6	9	11	13	15	16
0.1942	- 1.2	0.1151	1131	1112	1093	1075	1056 1251	1038 1230	1020 1210	1003 1190	1170	2	4	6	8	10	12	14	16	19
0.2179	-1.1	0.1357	1335 1562	1314 1539	1292 1515	1271 1492	1469	1446	1423	1401	1379	2	5	7	9	12	14	16	18	21
0.2420	- 1.0		0.000.00				+	S 450-3334	20000000	1635	1611	3	5	8	10	13	15	18	20	23
0.2661	-0.9	0.1841	1814	1788 2061	1762 2033	1736 2005	1711 1977	1685 1949	1660 1922	1894	1867	3	6	8	11	14	17	19	22	25
0.2897	-0.8 -0.7	0.2119	2090 2389	2358	2327	2296	2266	2236	2206	2177	2148	3	6	9	12	15	18	21	24	27
0.3123	-0.6	ACCOMMONS.	2709	2676	2643	2611	2578	2546	2514	2483	2451	3	6	10	13	16	19	23	26	29
0.3521	- 0.5	0.3085	3050	3015	2981	2946	2912	2877	2843	2810	2776	3	7	10	14	17	21	24	27	31
0.3683	-0.4	0.3446	3409	3372	3336	3300	3264	3228	3192	3156	3121	4	7	11	14	18	22	25	29	32
0.3814	- 0.3		3783	3745	3707	3669	3632	3594	3557	3520	3483	4	8	11	15	19	22	26 27	30	34
0.3910	-0.2	0.4207	4168	4129	4090	4052	4013	3974	3936	3897	3859 4247	4	8	12	15 16	19	24	28	32	36
0.3970	-0.1		4562	4522	4483	4443	4404	4364 4761	4325 4721	4286 4681	4641	4	8	12	16	20	24	28	32	36
0.3989	-0.0		4960	4920	4880	4840	4801			10000	9	1	2	3	4	5	6	7	8	9
ø(z)	Z	0	1	2	3	4	5	6	7	8	-	-	-	9		2000				-
														P	ROPOF	UBTR		ARTS		

The left-hand column gives the ordinate  $\phi(z) = \mathrm{e}^{-\frac{1}{2}z^2}/\sqrt{2\pi}$  of the standard normal distribution (i.e. the normal distribution having mean 0 and standard deviation 1), z being listed in the second column. The rest of the table gives  $\Phi(z) = \int_{-\infty}^z \phi(t) dt = \operatorname{Prob}\left(Z \leqslant z\right)$ , where Z is a random variable having the standard normal distribution. Locate z, expressed to its first decimal place in the second column, and its second decimal place along the top or bottom

horizontal: the corresponding table entry is  $\Phi(z)$ . Proportional parts are given for the third decimal place of z in part of the table. These proportional parts should be subtracted if z < 0 and added if z > 0.

EXAMPLES:  $\Phi(-1.2) = \text{Prob}(Z \le -1.2) = 0.1151;$  $\Phi(-1.23) = 0.1093; \Phi(-1.234) = 0.1086.$ 

φ(z)	Z	0	1	2	3	4	5	6	7	8	9	1
0.3989	0.0	0.5000	5040	5080	5120	5160	5199	5239	5279	5319	5359	4
0.3970	0.1	0.5398	5438	5478	5517	5557	5596	5636	5675	5714	5753	4
0.3910	0.2	0.5793	5832	5871	5910	5948	5987	6026	6064	6103	6141	4
0.3814	0.3	0.6179	6217	6255	6293	6331	6368	6406	6443	6480	6517	4
0.3683	0.4	0.6554	6591	6628	6664	6700	6736	6772	6808	6844	6879	4
0.3521	0.5	0.6915	6950	6985	7019	7054	7088	7123	7157	7190	7224	3
0.3332	0.6	0.7257	7291	7324	7357	7389	7422	7454	7486	7517	7549	3
0.3123	0.7	0.7580 0.7881	7611	7642	7673	7704	7734	7764	7794	7823	7852	3
0.2897 0.2661	0.8		7910 8186	7939	7967	7995 8264	8023	8051	8078	8106	8133	3
0.2420	1.0	0.8159 0.8413	8438	8212 8461	8238 8485	8508	8289 8531	8315 8554	8340 8577	8365 8599	8389 8621	2
			E-Allessa			70010000		-33133	Sine			-
0.2179 0.1942	1.1	0.8643 0.8849	8665 8869	8686 8888	8708 8907	8729 8925	8749 8944	8770 8962	8790 8980	8810 8997	8830 9015	2 2
0.1714	1.3	0.9032	9049	9066	9082	9099	9115	9131	9147	9162	9177	2
0.1497	1.4	0.9192	9207	9222	9236	9251	9265	9279	9292	9306	9319	1
0.1295	1.5	0.9332	9345	9357	9370	9382	9394	9406	9418	9429	9441	1
0.1109	1.6	0.9452	9463	9474	9484	9495	9505	9515	9525	9535	9545	1
0.0940	1.7	0.9554	9564	9573	9582	9591	9505	9608	9616	9625	9633	1
0.0790	1.8	0.9641	9649	9656	9664	9671	9678	9686	9693	9699	9706	1
0.0656	1.9	0.9713	9719	9726	9732	9738	9744	9750	9756	9761	9767	1
0.0540	2.0	0.9772	9778	9783	9788	9793	9798	9803	9808	9812	9817	0
0.0440	2.1	0.9821	9826	9830	9834	9838	9842	9846	9850	9854	9857	0
0.0355	2.2	0.9861	9864	9868	9871	9875	9878	9881	9884	9887	9890	0
0.0283	2.3	0.9893	9896	9898	9901	9904	9906	9909	9911	9913	9916	0
0.0224	2.4	0.99180	99202	99224	99245	99266	99286	99305	99324	99343	99361	2
0.0175	2.5	0.99379	99396	99413	99430	99446	99461	99477	99492	99506	99520	2
0.0136	2.6	0.99534	99547	99560	99573	99585	99598	99609	99621	99632	99643	1
0.0104	2.7	0.99653	99664	99674	99683	99693	99702	99711	99720	99728	99736	1
0.00792	2.8	0.99744	99752	99760	99767	99774	99781	99788	99795	99801	99807	1
0.00595	2.9	0.99813	99819	99825	99831	99836	99841	99846	99851	99856	99861	1
0.00443	3.0	0.99865	99869	99874	99878	99882	99886	99889	99893	99896	99900	0
0.00327	3.1	0.9 <sup>3</sup> 032	9 <sup>3</sup> 065	9 <sup>3</sup> 096	9 <sup>3</sup> 126	9 <sup>3</sup> 155	9 <sup>3</sup> 184	9 <sup>3</sup> 211	9 <sup>3</sup> 238	9 <sup>3</sup> 264	9 <sup>3</sup> 289	1
0.00238	3.2	0.9 <sup>3</sup> 313	9 <sup>3</sup> 336	9 <sup>3</sup> 359	9 <sup>3</sup> 381	9 <sup>3</sup> 402	93423	9 <sup>3</sup> 443	9 <sup>3</sup> 462	9 <sup>3</sup> 481	9 <sup>3</sup> 499	
0.00172	3.3	0.93517	9 <sup>3</sup> 534	9 <sup>3</sup> 550	9 <sup>3</sup> 566	9 <sup>3</sup> 581	9 <sup>3</sup> 596	9 <sup>3</sup> 610	9 <sup>3</sup> 624	9 <sup>3</sup> 638	9 <sup>3</sup> 651	
0.00123 0.0 <sup>3</sup> 873	3.4	0.9 <sup>3</sup> 663 0.9 <sup>3</sup> 767	9 <sup>3</sup> 675 9 <sup>3</sup> 776	9 <sup>3</sup> 687 9 <sup>3</sup> 784	9 <sup>3</sup> 698 9 <sup>3</sup> 792	9 <sup>3</sup> 709 9 <sup>3</sup> 800	9 <sup>3</sup> 720 9 <sup>3</sup> 807	9 <sup>3</sup> 730 9 <sup>3</sup> 815	9 <sup>3</sup> 740 9 <sup>3</sup> 822	9 <sup>3</sup> 749 9 <sup>3</sup> 828	9 <sup>3</sup> 758 9 <sup>3</sup> 835	$\vdash$
	000000	10000	7.37007	22/2/13/4/2	02011001100	100000000000000000000000000000000000000	100000000000000000000000000000000000000		2000000	- 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1	(2) DOTHER	-
$0.0^3612$	3.6	0.93841	9 <sup>3</sup> 847	9 <sup>3</sup> 853	9 <sup>3</sup> 858	9 <sup>3</sup> 864	9 <sup>3</sup> 869	9 <sup>3</sup> 874	9 <sup>3</sup> 879	9 <sup>3</sup> 883	9 <sup>3</sup> 888	
$0.0^3 425$ $0.0^3 292$	3.7	0.9 <sup>3</sup> 892 0.9 <sup>4</sup> 277	9 <sup>3</sup> 896 9 <sup>4</sup> 305	9 <sup>4</sup> 004 9 <sup>4</sup> 333	9 <sup>4</sup> 043 9 <sup>4</sup> 359	9 <sup>4</sup> 080 9 <sup>4</sup> 385	9 <sup>4</sup> 116 9 <sup>4</sup> 409	9 <sup>4</sup> 150 9 <sup>4</sup> 433	9 <sup>4</sup> 184	9 <sup>4</sup> 216	9 <sup>4</sup> 247 9 <sup>4</sup> 499	
$0.0^{\circ} 292$ $0.0^{3} 199$	3.8	0.9 277 0.9 <sup>4</sup> 519	9 305 9 <sup>4</sup> 539	9 333 9 <sup>4</sup> 557	9 359 9 <sup>4</sup> 575	9 365 9 <sup>4</sup> 593	9409	9 433 9 <sup>4</sup> 625	9 <sup>4</sup> 456 9 <sup>4</sup> 641	9 <sup>4</sup> 478 9 <sup>4</sup> 655	9 499 9 <sup>4</sup> 670	
$0.0^3 134$	4.0	0.94683	9 <sup>4</sup> 696	9 <sup>4</sup> 709	9 <sup>4</sup> 721	9 <sup>4</sup> 733	9 <sup>4</sup> 744	9 <sup>4</sup> 755	9 <sup>4</sup> 765	9 <sup>4</sup> 775	9 <sup>4</sup> 784	
0.0 <sup>4</sup> 893		0.94 793	94 802	9 <sup>4</sup> 811	9 <sup>4</sup> 819	94826	9 <sup>4</sup> 834	9 <sup>4</sup> 841	9 <sup>4</sup> 848			1
0.0° 589	4.1	0.9 793	9 802 9 <sup>4</sup> 872	9 811 9 <sup>4</sup> 878	9 8 19 9 <sup>4</sup> 883	9 826 9 <sup>4</sup> 888	9 834	9 841	9 848 9 023	9 <sup>4</sup> 854 9 <sup>5</sup> 066	9 <sup>4</sup> 861 9 <sup>5</sup> 107	
0.0 <sup>4</sup> 385	4.3	0.95 146	9 <sup>5</sup> 184	95220	9 <sup>5</sup> 254	9 <sup>5</sup> 288	95319	9 <sup>5</sup> 350	95379	9 <sup>5</sup> 407	95 433	
0.0 <sup>4</sup> 249	4.4	0.95459	95483	9 <sup>5</sup> 506	95529	9 <sup>5</sup> 550	95 571	95590	95 609	95627	95644	
0.0 <sup>4</sup> 160	4.5	0.95660	9 <sup>5</sup> 676	95691	9 <sup>5</sup> 705	9 <sup>5</sup> 719	9 <sup>5</sup> 732	9 <sup>5</sup> 744	9 <sup>5</sup> 756	9 <sup>5</sup> 768	9 <sup>5</sup> 778	
0.0 <sup>4</sup> 101	4.6	0.95 789	9 <sup>5</sup> 799	95808	9 <sup>5</sup> 817	9 <sup>5</sup> 826	9 <sup>5</sup> 834	95842	95 849	9 <sup>5</sup> 857	9 <sup>5</sup> 863	
0.0 <sup>5</sup> 637	4.7	0.95870	95876	9 <sup>5</sup> 882	95888	95893	95 898	9 <sup>6</sup> 032	9 <sup>6</sup> 079	9 <sup>6</sup> 124	9 <sup>6</sup> 166	
0.05396	4.8	0.96 207	9 <sup>6</sup> 245	96 282	9 <sup>6</sup> 317	9 <sup>6</sup> 351	96383	9 <sup>6</sup> 413		96470	9 <sup>6</sup> 496	
0.05 244	4.9	0.9 <sup>6</sup> 521	96 545	96 567	9 <sup>6</sup> 589	9 <sup>6</sup> 609	9 <sup>6</sup> 629	9 <sup>6</sup> 648	96 665	96682	96698	
0.0 <sup>5</sup> 149	5.0	0.9 <sup>6</sup> 713	9 <sup>6</sup> 728	9 <sup>6</sup> 742	9 <sup>6</sup> 755	9 <sup>6</sup> 767	9 <sup>6</sup> 779	9 <sup>6</sup> 790	9 <sup>6</sup> 801	96811	9 <sup>6</sup> 821	
0.0 <sup>6</sup> 897	5.1	0.96830	96839	9 <sup>6</sup> 847	9 <sup>6</sup> 855	9 <sup>6</sup> 863	96870	9 <sup>6</sup> 877	96883	9 <sup>6</sup> 889	9 <sup>6</sup> 895	1
0.0 <sup>6</sup> 536	5.2	0.97004	97056	9 <sup>7</sup> 105	9 <sup>7</sup> 152	9 <sup>7</sup> 197	97240	9 <sup>7</sup> 280	9 <sup>7</sup> 318	9 <sup>7</sup> 354	9 <sup>7</sup> 388	
0.0 <sup>6</sup> 317	5.3	0.97421	97452	9 <sup>7</sup> 481	9 <sup>7</sup> 509	9 <sup>7</sup> 535	9 <sup>7</sup> 560	9 <sup>7</sup> 584	9 <sup>7</sup> 606	9 <sup>7</sup> 628	9 <sup>7</sup> 648	
0.0 <sup>6</sup> 186	5.4	0.9 <sup>7</sup> 667	9 <sup>7</sup> 685	9 <sup>7</sup> 702	9 <sup>7</sup> 718	9 <sup>7</sup> 734	9 <sup>7</sup> 748	9 <sup>7</sup> 762	9 <sup>7</sup> 775	9 <sup>7</sup> 787	9 <sup>7</sup> 799	
0.0 <sup>6</sup> 108	5.5	0.9 <sup>7</sup> 810	9 <sup>7</sup> 821	9 <sup>7</sup> 831	97840	9 <sup>7</sup> 849	9 <sup>7</sup> 857	9 <sup>7</sup> 865	9 <sup>7</sup> 873	9 <sup>7</sup> 880	9 <sup>7</sup> 886	
.0 <sup>7</sup> 618	5.6	0.97893	97899	9 <sup>8</sup> 045	98099	9 <sup>8</sup> 150	9 <sup>8</sup> 198	9 <sup>8</sup> 243	9 <sup>8</sup> 286	9 <sup>8</sup> 327	9 <sup>8</sup> 365	
.0 <sup>7</sup> 351	5.7	0.98401	98435	9 <sup>8</sup> 467	98498	9 <sup>8</sup> 527	9 <sup>8</sup> 554	9 <sup>8</sup> 579	98604	98 626	9 <sup>8</sup> 648	
.0 <sup>7</sup> 198	5.8	0.98668	98 688	98 706	98723	98739	9 <sup>8</sup> 754	98769	98 782	98 795	9 <sup>8</sup> 807	
0.0 <sup>7</sup> 110	5.9	0.9 <sup>8</sup> 818	98829	98839	98849	9 <sup>8</sup> 857	9 <sup>8</sup> 866	98874	98881	98888	9 <sup>8</sup> 895	
0.08608	6.0	0.99013	9°072	99128	9°180	9°229	9°276	9°319	9°360	9°399	9 <sup>9</sup> 435	

The superscript in numbers such as 0.98401 indicates a number of nines, thus: 0.98401 = 0.999999999401, and  $0.9^3032 = 0.999032$ .

ADD PROPORTIONAL PARTS

ADD PROPORTIONAL PARTS

2 3

8 12

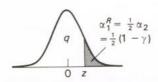
8 12

Proportional parts have not been given in this region because they would not be of sufficient accuracy.

EXAMPLES:  $\Phi(1.2) = \text{Prob}(Z \le 1.2) = 0.8849; \Phi(1.23) =$ 0.8907;  $\Phi(1.234) = 0.8914$ ; Prob  $(Z \ge 2.3) = \text{Prob}(Z \le -2.3)$ =  $\Phi$  (-2.3) = 0.0107 (making use of the symmetry of the normal distribution); Prob (0.32  $\leq$  Z  $\leq$  1.43) =  $\Phi$ (1.43) - $\Phi(0.32) = 0.9236 - 0.6255 = 0.2981$ .

Other normal distributions may be dealt with by standardisation, i.e. by subtracting the mean and dividing by the standard deviation. For example if X has the normal distribution with mean 10.0 and standard deviation 2.0,  $Prob(X \le 17.5) = Prob(Z \le \frac{1}{2}(17.5 - 10.0)) = Prob(Z \le 3.75)$  $= \Phi(3.75) = 0.9^{4}116 = 0.9999116.$ 

## Percentage points of the normal distribution



$q = \Phi(z)$	$\alpha_1^R$	α2	7	Z
0.50				0.0000
0.60	40%			0.2533
0.70	30%			0.5244
0.80	20%	40%	60%	0.8416
0.85	15%	30%	70%	1.0364
0.90	10%	20%	80%	1.2816
0.91	9%	18%	82%	1,3408
0.92	8%	16%	84%	1.4051
0.93	7%	14%	86%	1.4758
0.94	6%	12%	88%	1.5548
0.950	5.0%	10.0%	90.0%	1.6449
0.952	4.8%	9.6%	90.4%	1.6646
0.954	4.6%	9.2%	90.8%	1.6849
0.956	4.4%	8.8%	91.2%	1.7060
0.958	4.2%	8.4%	91.6%	1.7279
0.960	4.0%	8.0%	92.0%	1.7507
0.962	3.8%	7.6%	92.4%	1.7744
0.964	3.6%	7.2%	92.8%	1.7991
0.966	3.4%	6.8%	93.2%	1.8250
0.968	3.2%	6.4%	93.6%	1.8522

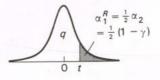
$q = \Phi(z)'$	$\alpha_1^R$	$\alpha_2$	γ	2
0.970	3.0%	6.0%	94.0%	1.8808
0.971	2.9%	5.8%	94.2%	1.8957
0.972	2.8%	5.6%	94.4%	1.9110
0.973	2.7%	5.4%	94.6%	1.9268
0.974	2.6%	5.2%	94.8%	1.9431
0.975	2.5%	5.0%	95.0%	1.9600
0.976	2.4%	4.8%	95.2%	1.9774
0.977	2.3%	4.6%	95.4%	1.9954
0.978	2.2%	4.4%	95.6%	2.0141
0.979	2.1%	4.2%	95.8%	2.0335
0.980	2.0%	4.0%	96.0%	2.0537
0.981	1.9%	3.8%	96.2%	2.0749
0.982	1.8%	3.6%	96.4%	2.0969
0.983	1.7%	3.4%	96.6%	2.1201
0.984	1.6%	3.2%	96.8%	2.1444
0.985	1.5%	3.0%	97.0%	2.1701
0.986	1.4%	2.8%	97.2%	2.1973
0.987	1.3%	2.6%	97.4%	2.2262
0.988	1.2%	2.4%	97.6%	2.2571
0.989	1.1%	2.2%	97.8%	2.2904

$q = \Phi(z)$	$\alpha_1^R$	$\alpha_2$	γ	Z
0.990	1.0%	2.0%	98.0%	2.3263
0.991	0.9%	1.8%	98.2%	2.3656
0.992	0.8%	1.6%	98.4%	2,4089
0.993	0.7%	1.4%	98.6%	2,4573
0.994	0.6%	1.2%	98.8%	2.5121
0.995	0.5%	1.0%	99.0%	2.5758
0.996	0.4%	0.8%	99.2%	2.6521
0.997	0.3%	0.6%	99.4%	2.7478
0.998	0.2%	0.4%	99.6%	2.8782
0.999	0.1%	0.2%	99.8%	3.0902
0.9995	0.05%	0.1%	99.9%	3.2905
0.9999	0.01%	0.02%	99.98%	3.7190
0.99995	0.005%	0.01%	99.99%	3.8906
0.99999	0.001%	0.002%	99.998%	4.2649
0.999995	0.0005%	0.001%	99.999%	4.4172
0.999999	0.0001%	0.0002%	99.9998%	4.7534
0.999995	0.00005%	0.0001%	99.9999%	4.8916
0.9999999	0.00001%	0.00002%	99.99998%	5.1993
0.99999995	0.000005%	0.00001%	99.99999%	5.3267
0.99999999	0.000001%	0.000002%	99.999998%	5.6120

The following notation is used in this and subsequent tables. q represents a quantile, i.e. q and the tabulated value z are related here by  $\operatorname{Prob}(Z \leq z) = q = \Phi(z)$ ; e.g.  $\Phi(1.9600) = q = 0.975$ , where z = 1.9600.  $\alpha_1$ ,  $\alpha_1^L$  and  $\alpha_1^R$  denote significance levels for one-tailed or one-sided critical regions. Sometimes  $\alpha_1^L$  and  $\alpha_1^R$  values, corresponding to critical regions in the left-hand and right-hand tails, need to be tabulated separately; in other cases one may easily be obtained from the other. Here we have included only  $\alpha_1^R$ , since  $\alpha_1^L$  values are obtained using the symmetry of the normal distribution. Thus if a 5% critical region in the right-hand tail is required, we find the entry corresponding to  $\alpha_1^R = 5\%$  and obtain  $Z \geqslant 1.6449$ . Had we required a 5%

critical region in the left-hand tail it would have been  $Z\leqslant -1.6449$ .  $\alpha_2$  gives critical regions for two-sided tests; here  $|Z|\geqslant 1.9600$  is the critical region for the two-sided test at the  $\alpha_2=5\%$  significance level. Finally,  $\gamma$  indicates confidence levels for confidence intervals – so a 95% confidence interval here is derived from  $|Z|\leqslant 1.9600$ . For example with a large sample  $X_1,X_2,\ldots,X_n$  we know that  $(\bar{X}-\mu)/(s/\sqrt{n})$  has approximately a standard normal distribution, where  $\bar{X}=\sum X_i/n$  and the adjusted sample standard deviation s is given by  $s=\{\sum (X_i-\bar{X})^2/(n-1)\}^{1/2}$ . So a 95% confidence interval for  $\mu$  is derived from  $|(\bar{X}-\mu)/(s/\sqrt{n})|\leqslant 1.9600$ , which is equivalent to  $\bar{X}-1.96s/\sqrt{n}\leqslant \mu\leqslant \bar{X}+1.96s/\sqrt{n}$ .

# Percentage points of the Student *t* distribution



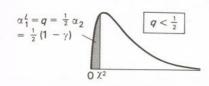
q	0.95	0.975	0.99	0.995
$\alpha_1^R$	5%	2½%	1%	1/4%
02	10%	5%	2%	1%
7	90%	95%	98%	99%
v			2000	C 6 C 5 C 6 C 7 F 6
1	6.3138	12.7062	31.8205	63.6567
2	2.9200	4.3027	6.9646	9.9248
3	2.3534	3.1824	4.5407	5.8409
4	2.1318	2.7764	3.7469	4.6041
5	2.0150	2.5706	3.3649	4.0321
6	1.9432	2.4469	3.1427	3.7074
7	1.8946	2.3646	2.9980	3.4995
8	1.8595	2.3060	2.8965	3.3554
9	1.8331	2.2622	2.8214	3.2498
10	1.8125	2.2281	2.7638	3.1693
13	1.7959	2.2010	2.7181	3.1058
12	1.7823	2.1788	2.6810	3.0545
13	1.7709	2.1604	2.6503	3.0123
14	1.7613	2.1448	2.6245	2.9768
15	1.7531	2.1314	2.6025	2.9467
16	1,7459	2.1199	2.5835	2.9208
17	1.7396	2.1098	2.5669	2.8982
18	1.7341	2.1009	2.5524	2.8784
19	1.7291	2.0930	2.5395	2.8609
20	1.7247	2.0860	2.5280	2.8453

q	0.95	0.975	0.99	0.995
$\alpha_1^R$	5%	21/2%	1%	1/2%
α <sub>2</sub>	10%	5%	2%	1%
γ	90%	95%	98%	99%
v	00 (1890)		\$4500 SEC.50	
21	1.7207	2.0796	2.5176	2.8314
22	1.7171	2.0739	2.5083	2.8188
23	1.7139	2.0687	2.4999	2.8073
24	1.7109	2.0639	2.4922	2.7969
25	1.7081	2.0595	2.4851	2.7874
26	1.7056	2.0555	2.4786	2.7787
27	1.7033	2.0518	2.4727	2.7707
28	1.7011	2.0484	2.4671	2.7633
29	1.6991	2.0452	2.4620	2.7564
30	1.6973	2.0423	2.4573	2.7500
31	1.6955	2.0395	2.4528	2.7440
32	1.6939	2.0369	2.4487	2.7385
33	1.6924	2.0345	2.4448	2.7333
34	1.6909	2.0322	2.4411	2.7284
35	1.6896	2.0301	2.4377	2.7238
36	1.6883	2.0281	2,4345	2.7195
37	1.6871	2.0262	2,4314	2.7154
38	1.6860	2.0244	2.4286	2,7116
39	1.6849	2.0227	2.4258	2.7079
40	1.6839	2.0211	2.4233	2.7045

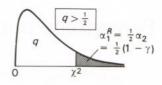
9	0.95	0.975	0.99	0.995
aR	5%	2%%	1%	1/2%
α <sub>2</sub>	10%	5%	2%	1%
γ	90%	95%	98%	99%
y				
42	1.6820	2.0181	2.4185	2.6981
44	1.6802	2.0154	2.4141	2.6923
46	1.6787	2.0129	2.4102	2.6870
48	1.6772	2.0106	2.4066	2.6822
50	1.6759	2.0086	2.4033	2.6778
55	1.6730	2.0040	2.3961	2.6682
60	1.6706	2.0003	2.3901	2.6603
65	1.6686	1.9971	2.3851	2.6536
70	1.6669	1.9944	2.3808	2.6479
75	1.6654	1.9921	2.3771	2.6430
80	1,6641	1.9901	2.3739	2.6387
85	1.6630	1.9883	2.3710	2.6349
90	1.6620	1.9867	2.3685	2.6316
95	1.6611	1.9853	2.3662	2.6286
100	1.6602	1.9840	2.3642	2.6259
125	1.6571	1.9791	2.3565	2.6157
150	1.6551	1.9759	2.3515	2.6090
175	1.6536	1.9736	2.3478	2.6042
200	1.6525	1.9719	2.3451	2.6006
06	1.6449	1.9600	2.3263	2.5758

The t distribution is mainly used for testing hypotheses and finding confidence intervals for means, given small samples from normal distributions. For a single sample,  $(\bar{X}-\mu)/(s/\sqrt{n})$  has the t distribution with  $\nu=n-1$  degrees of freedom (see notation above). So, e.g. if n=10, giving  $\nu=9$ , the  $\gamma=95\%$  confidence interval for  $\mu$  is  $\bar{X}-2.2622s/\sqrt{10} \leqslant \mu \leqslant \bar{X}+2.2622s/\sqrt{10}$ . Given two samples of sizes  $n_1$  and  $n_2$ , sample means  $\bar{X}_1$  and  $\bar{X}_2$ , and adjusted sample standard deviations  $s_1$  and  $s_2$ ,  $(\bar{X}_1-\bar{X}_2)/\sqrt{10}$ 

 $\{s\sqrt{(1/n_1)+(1/n_2)}\}$  has the t distribution with  $\nu=n_1+n_2-2$  degrees of freedom, where  $s=[\{(n_1-1)s_1^2+(n_2-1)s_2^2\}/(n_1+n_2-2)]^{1/2}$ . So if the population means are denoted  $\mu_1$  and  $\mu_2$ , then to test  $H_0\colon \mu_1=\mu_2$  against  $H_1\colon \mu_1>\mu_2$  at the 5% level, given samples of sizes 6 and 10, the critical region is  $(\overline{X}_1-\overline{X}_2)/(s\sqrt{\frac{1}{6}+\frac{1}{10}})\geqslant 1.7613$ , using  $\nu=6+10-2=14$  and  $\alpha_1^R=5\%$ . As with the normal distribution, symmetry shows that  $\alpha_1^L$  values are just the  $\alpha_1^R$  values prefixed with a minus sign.



# Percentage points of the chi-squared $(\chi^2)$ distribution



q	0.005	0.01	0.025	0.05	0.10	0.50	0.90	0.05	0.075	0.00	
$\alpha_1^L$	1/3%	1%	2½%	5%	10%	0.50	0.90	0.95	0.975	0.99	0.995
$\alpha_1^R$	72.0	1.00	1 2/1/0	970	10%			Contract Con		SCHOOL STATE OF THE PARTY OF TH	
0.000	100	00/		1			10%	5%	2%%	1%	1/4%
α2	1%	2%	5%	10%	20%		20%	10%	5%	2%	1%
γ	99%	98%	95%	90%	80%		80%	90%	95%	98%	99%
1	.00004	.00016	.00098	.00393	.0158	0.455	2.700	3.841	5.004	0.005	7.070
2	.0100	.0201	.0506	0.103	0.211	1.386	2.706 4.605	5.991	5.024 7.378	6.635 9.210	7.879 10.597
3	.0717	0.115	0.216	0.352	0.584	2.366	6.251	7.815	9.348	11.345	12.838
4	0.207	0.297	0.484	0.711	1.064	3.357	7,779	9.488	11.143	13.277	14.860
5	0.412	0.554	0.831	1.145	1.610	4.351	9.236	11.070	12.833	15.086	16.750
6	0.676	0.872	1.237	1.635	2.204	5.348	10.645	12.592	14.449 *	16.812	18.548
7	0.989	1.239	1.690	2.167	2.833	6.346	12.017	14.067	16.013	18.475	20.278
8	1.344	1.646	2.180	2.733	3.490	7.344	13.362	15.507	17.535	20.090	21.955
9	1.735	2.088	2.700	3.325	4.168	8.343	14.684	16.919	19.023	21.666	23.589
10	2.156	2.558	3.247	3.940	4.865	9.342	15.987	18.307	20.483	23.209	25.188
11	2.603	3.053	3.816	4.575	5.578	10.341	17.275	19.675	21,920	24.725	26.757
12	3.074	3.571	4.404	5.226	6.304	11.340	18.549	21.026	23.337	26.217	28.300
13	3.565	4.107	5.009	5.892	7.042	12.340	19.812	22.362	24.736	27.688	29.819
15	4.075 4.601	4.660 5.229	5.629	6.571	7.790	13.339	21.064	23.685	26.119	29.141	31.319
Christopholish .			6.262	7.261	8.547	14.339	22.307	24.996	27.488	30.578	32.801
16	5.142	5.812	6.908	7.962	9.312	15.338	23.542	26.296	28.845	32.000	34.267
17	5.697	6.408	7.564	8.672	10.085	16.338	24.769	27.587	30.191	33.409	35.718
19	6.265 6.844	7.015 7.633	8.231	9.390	10.865	17.338	25.989	28.869	31.526	34.805	37.156
20	7.434	8.260	8.907 9.591	10.117	11.651	18.338	27.204	30.144	32.852	36.191	38.582
	10.000	000077		10.851	12.443	19.337	28.412	31.410	34.170	37.566	39.997
21 22	8.034	8.897	10.283	11.591	13.240	20.337	29.615	32.671	35.479	38.932	41.401
23	8.643 9.260	9.542 10.196	10.982	12.338	14.041	21.337	30.813	33.924	36.781	40.289	42.796
24	9.886	10.196	11.689 12.401	13.091 13.848	14.848 15.659	22.337	32.007	35.172	38.076	41.638	44.181
25	10.520	11.524	13.120	14.611	16.473	23.337 24.337	33.196 34.382	36.415	39.364	42.980	45.559
26	11.160	12.198	13.844	100.000.000				37.652	40.646	44.314	46.928
27	11.808	12.130	14.573	15.379 16.151	17.292 18.114	25.336	35.563	38.885	41.923	45.642	48.290
28	12.461	13.565	15.308	16.928	18.939	26.336 27.336	36.741 37.916	40.113 41.337	43.195	46.963	49.645
29	13.121	14.256	16.047	17.708	19.768	28,336	39.087	42.557	44.461 45.722	48.278 49.588	50.993 52.336
30	13.787	14.953	16.791	18.493	20.599	29.336	40.256	43.773	46.979	50.892	53.672
31	14.458	15.655	17.539	19.281	21.434	30.336	41.422	44.985			
32	15.134	16.362	18.291	20.072	22.271	31.336	42.585	46.194	48.232 49.480	52.191 53.486	55.003
33	15.815	17.074	19.047	20.867	23.110	32.336	43.745	47.400	50.725	54.776	56.328 57.648
34	16.501	17.789	19.806	21.664	23.952	33.336	44.903	48.602	51.966	56.061	58.964
35	17.192	18.509	20.569	22.465	24.797	34.336	46.059	49.802	53.203	57.342	60.275
36	17.887	19.233	21.336	23.269	25.643	35.336	47.212	50.998	54.437	58.619	61.581
37	18.586	19.960	22.106	24.075	26.492	36.336	48.363	52.192	55.668	59.893	62.883
38	19.289	20.691	22.878	24.884	27.343	37.335	49.513	53.384	56.896	61.162	64.181
39	19.996	21.426	23.654	25.695	28.196	38.335	50.660	54.572	58.120	62.428	65.476
40	20.707	22.164	24.433	26.509	29.051	39.335	51.805	55.758	59.342	63.691	66.766
45	24.311	25.901	28.366	30.612	33.350	44.335	57.505	61.656	65.410	69.957	73.166
50	27.991	29.707	32.357	34.764	37.689	49.335	63.167	67.505	71.420	76.154	79.490
60	35.534	37.485	40.482	43.188	46.459	59.335	74.397	79.082	83.298	88.379	91.952
70	43.275	45.442	48.758	51.739	55.329	69.334	85.527	90.531	95.023	100.43	104.21
CONTRACTOR DE	51.172	53.540	57.153	60.391	64.278	79.334	96.578	101.88	106.63	112.33	116.32
90	59.196	61.754	65.647	69.126	73.291	89.334	107.57	113.15	118.14	124.12	128.30
100	67.328	70.065	74.222	77.929	82.358	99.334	118.50	124.34	129.56	135.81	140.17
120	83.852	86.923	91.573	95.705	100.62	119.33	140.23	146.57	152.21	158.95	163.65
150 200	109.14	112.67	117.98	122.69	128.28	149.33	172.58	179.58	185.80	193.21	198.36
200	152.24	156.43	162.73	168.28	174.84	199.33	226.02	233.99	241.06	249.45	255.26

The  $\chi^2$  (chi-squared) distribution is used in testing hypotheses and forming confidence intervals for the standard deviation  $\sigma$  and the variance  $\sigma^2$  of a normal population. Given a random sample of size n,  $\chi^2 = (n-1)s^2/\sigma^2$ has the chi-squared distribution with  $\nu = n - 1$  degrees of freedom (s is defined on page 20). So if n = 10, giving  $\nu=9$ , and the null hypothesis  $H_0$  is  $\sigma=5$ , 5% critical regions for testing against (a)  $H_1$ :  $\sigma < 5$ , (b)  $H_1$ :  $\sigma > 5$ and (c)  $H_1$ :  $\sigma \neq 5$  are (a)  $9s^2/25 \leq 3.325$ , (b)  $9s^2/25 \geq$ 16.919 and (c)  $9s^2/25 \le 2.700$  or  $9s^2/25 \ge 19.023$ , using significance levels (a)  $\alpha_1^L$ , (b)  $\alpha_1^R$  and (c)  $\alpha_2$  as appropriate. For example if  $s^2 = 50.0$ , this would result in rejection of  $H_0$  in favour of  $H_1$  at the 5% significance level in case (b) only. A  $\gamma = 95\%$  confidence interval for  $\sigma$  with these data is derived from  $2.700 \le (n-1)s^2/\sigma^2 \le 19.023$ , i.e.  $2.700 \le$  $450.0/\sigma^2 \le 19.023$ , which gives  $450/19.023 \le \sigma^2 \le 450/19.023$ 2.700 or, taking square roots,  $4.864 \le \sigma \le 12.910$ .

The  $\chi^2$  distribution also gives critical values for the familiar  $\chi^2$  goodness-of-fit tests and tests for association in contingency tables (cross-tabulations). A classification scheme is given such that any observation must fall into precisely one class. The data then consist of frequency-counts and the statistic used is  $\chi^2 = \sum (Ob, -Ex.)^2/Ex.$ 

where the sum is over all the classes, Ob. denoting Observed frequencies and Ex. Expected frequencies, these being calculated from the appropriate null hypothesis  $H_0$ . It is common to require that no expected frequencies be less than 5, and to regroup if necessary to achieve this. In goodness-of-fit tests, Ho directly or indirectly specifies the probabilities of a random observation falling in each class. It is sometimes necessary to estimate population parameters (e.g. the mean and/or the standard deviation) to do this. The expected frequencies are these probabilities multiplied by the sample size. The number of degrees of freedom  $\nu =$ (the number of classes -1 - the number of population parameters which have to be estimated). With contingency tables, Ho is the hypothesis of no association between the classification schemes by rows and by columns, the expected frequency in any cell is (its row's subtotal) x (its column's subtotal) ÷ (total number of observations), and the number of degrees of freedom  $\nu$  is (number of rows - 1)  $\times$ (number of columns -1).

In all these cases, it is *large* values of  $\chi^2$  which are significant, so critical regions are of the form  $\chi^2 \geqslant tabulated$  value, using  $\alpha_1^R$  significance levels.

## Percentage points of the F distribution

 $\begin{array}{c|c}
 & \alpha_1^R = \frac{1}{2}\alpha_2 \\
 & = \frac{1}{2}(1 - \gamma)
\end{array}$ 

Three of the main uses of the F distribution are (a) the comparison of two variances, (b) to give critical values in the wide range of analysis-of-variance tests and (c) to find critical values for the multiple correlation coefficient.

have  $1/9.074 \le 4.0/(\sigma_1^2/\sigma_2^2) \le 5.523$  which, after a little manipulation, gives  $4.0/5.523 \le \sigma_1^2/\sigma_2^2 \le 4.0 \times 9.074$ , and taking square roots yields (0.851:6.025) as the  $\gamma=95\%$  confidence interval for  $\sigma_1/\sigma_2$ .

#### (a) Comparison of two variances

Given random samples of sizes  $n_1$  and  $n_2$  from two normal populations having standard deviations  $\sigma_1$  and  $\sigma_2$  respectively, and where  $s_1$  and  $s_2$  denote the adjusted sample standard deviations (see page 20),  $(s_1^2/s_2^2)/(\sigma_1^2/\sigma_2^2)$  has the F distribution with  $(\nu_1, \nu_2) = (n_1 - 1, n_2 - 1)$  degrees of freedom. In the tables the degrees of freedom are given along the top  $(\nu_1)$  and down the left-hand side  $(\nu_2)$ . For economy of space, the tables only give values in the right-hand tail of the distribution. This gives rise to minor inconvenience in some applications, which will be seen in the following illustrations:

- (i) One-sided test  $-H_0$ :  $\sigma_1 = \sigma_2$ ,  $H_1$ :  $\sigma_1 > \sigma_2$ . The tabulated figures are directly appropriate. Thus if  $n_1 = 5$  and  $n_2 = 8$ , giving  $\nu_1 = 4$  and  $\nu_2 = 7$ , the  $\alpha_1^R = 5\%$  critical region is  $s_1^2/s_2^2 \ge 4.120$ .
- (ii) One-sided test  $-H_0$ :  $\sigma_1=\sigma_2$ ,  $H_1$ :  $\sigma_1<\sigma_2$ . Here we would normally need  $\alpha_L^T$  values for  $s_1^2/s_2^2$ . However the tabulated values are appropriate if we use the statistic  $s_2^2/s_1^2$  and switch round the degrees of freedom. So if  $n_1=5$  and  $n_2=8$ , the appropriate  $\alpha_1^R=5\%$  critical region is  $s_2^2/s_1^2\geqslant 6.094$  (using  $\nu_1=7$ ,  $\nu_2=4$ ).
- (iii) Two-sided test  $H_0$ :  $\sigma_1 = \sigma_2$ ,  $H_1$ :  $\sigma_1 \neq \sigma_2$ . Calculate either  $s_1^2/s_2^2$  or  $s_2^2/s_1^2$ , whichever is the larger, switching round the degrees of freedom if  $s_2^2/s_1^2$  is chosen, and enter the tables using the  $\alpha_2$  significance levels. So if  $n_1 = 5$  and  $n_2 = 8$ , giving  $\nu_1 = 4$  and  $\nu_2 = 7$ , then we reject  $H_0$  in favour of  $H_1$  at the  $\alpha_2 = 5\%$  significance level if either  $s_1^2/s_2^2 \geq 5.523$  or  $s_2^2/s_1^2 \geq 9.074$ .
- (iv) Confidence interval for  $\sigma_1/\sigma_2$  or  $\sigma_1^2/\sigma_2^2$ . This is derived from an interval of the form  $f_1 \leq (s_1^2/s_2^2)/(\sigma_1^2/\sigma_2^2) \leq f_2$  where  $f_2$  is read directly from the tables, using the desired confidence level  $\gamma$ , and  $f_1$  is the reciprocal of the tabulated value found after switching the degrees of freedom. Thus if  $\gamma=95\%$ , and  $n_1=5$ ,  $n_2=8$  giving  $\nu_1=4$ ,  $\nu_2=7$  again, then  $f_2=5.523$  and  $f_1=1/9.074$ . So, e.g. if  $s_1^2/s_2^2=4.0$  we

#### (b) Analysis-of-variance(ANOVA) tests

The F statistics produced in the standard analysis-of-variance procedures are in the correct form for direct application of the tables, i.e. the critical regions are  $F \ge tabulated$  value. Note that  $\alpha_1^R$  (not  $\alpha_2$ ) significance levels should be used. In the one-way classification analysis-of-variance,  $\nu_1$  is one less than the number of samples being compared; otherwise in experiments where more than one factor is involved, F statistics can be found to test the effect of each of the factors and  $\nu_1$  is then one less than the number of levels of the particular factor being examined. If an F statistic is being used to test for an interactive effect between two or more factors,  $\nu_1$  is the product of the numbers of degrees of freedom for the component factors.  $v_2$  is the number of degrees of freedom in the residual (or error, or withinsample) sum of squares, and is usually calculated as (total number of observations -1) - (total number of degrees of freedom attributable to individual factors and their interactions (if relevant)). If the experiment includes replication, and a replication effect is included in the underlying model, this also counts as a factor for these purposes.

#### (c) Testing a multiple correlation coefficient

In a multiple linear regression  $\hat{Y}=a_0+a_1X_1+a_2X_2+\ldots+a_kX_k$ , where  $a_0,a_1,a_2,\ldots,a_k$  are estimated by least squares, the multiple correlation coefficient R is a measure of the goodness-of-fit of the regression model. R can be calculated as  $R=+\sqrt{\Sigma(\hat{Y}-\bar{Y})^2/\Sigma(Y-\bar{Y})^2}$ , where Y denotes the observed values and  $\bar{Y}$  their mean. R is also the linear correlation coefficient of  $\hat{Y}$  with Y. Assuming normality of residuals, R can be used to test if the regression model is useful. Calculate  $F=(n-k-1)R^2/k(1-R^2)$ , where n is the size of the sample from which R was computed, and the critical regions showing evidence that the model is indeed useful are of the form  $F \geqslant tabulated value$ , using the F tables with  $v_1=k$ ,  $v_2=n-k-1$  and  $\alpha_1^R$  significance levels.

								q = 0.90	0	$\frac{R}{1} = 10\%$	α2	= 20%	γ=	= 80%							
V2 1	1	2	3	4	5	6	7	8	9	10	12	15	20	25	30	50	75	100	150	00	V1 V2
1	39.86	49.50	53.59	55.83	57.24	58.20	58.91	59.44	59.86	60.19	60.71	61.22	61.74	62.05	62.26	62.69	62.90	63.01	63.11	63.33	1
2	8.526	9.000	9.162	9.243	9.293	9.326	9.349	9.367	9.381	9.392	9.408	9.425	9.441	9.451	9.458	9.471	9.478	9.481	9.485	9.491	2
3	5.538	5.462	5.391	5.343	5.309	5.285	5.266	5.252	5.240	5.230	5.216	5.200	5.184	5.175	5.168	5.155	5.148	5.144	5.141	5.134	3
4	4.545	4.325	4,191	4.107	4.051	4.010	3.979	3.955	3.936	3.920	3.896	3.870	3.844	3.828	3.817			3.778		3.761	4
5	4.060	3.780	3.619	3.520	3.453	3.405	3.368	3.339	3.316	3.297	3.268	3.238	3.207	3.187	3.174	3.147	3.133	3.126	3.119	3.105	5
6	3.776	3,463	3.289	3.181	3.108	3.055	3.014	2.983	2.958	2.937	2,905	2.871	2.836	2.815	2.800	2.770	2.754	2.746	2.738	2.722	6
7	3.589	3.257	3.074	2.961	2.883	2.827	2.785	2.752	2.725	2.703	2.668	2.632	2.595	2.571	2.555	2.523	2.506	2,497	2.488	2.471	7
8	3.458	3.113	2.924	2.806	2.726	2.668	2.624	2.589	2.561	2.538	2.502	2.464	2.425	2.400	2,383	170000000000000000000000000000000000000		2.321		2.293	8
9	3.360	3.006	2.813	2.693	2.611	2.551		2.469	2.440	2.416				2.272		-1-1-		2.189		2.159	9
10	3.285	2.924	2.728	2.605	2,522	2.461	2.414	2.377	2.347	2.323	2.284	2,244	2.201	2.174	2.155	2.117	2.097	2.087	2.077	2.055	10
11	3.225	2.860	2.660	2.536	2.451	2.389	2,342	2,304	2.274	2.248	2.209	2.167	2.123	2.095	2,076	2.036	2.016	2.005	1.994	1.972	11
12	3.177	2.807	2.606	2.480	2.394	2,331	2.283	2.245	2.214	2.188	2.147	2.105	2.060	2.031	2.011	1.970	1.949	1,938	1.927	1.904	12
13	3.136	2.763	2.560	2.434	2.347	2.283	2.234	2.195	2.164	2.138	2.097	2.053	2.007	1.978	1.958	1.915	1,893	1.882	1.870	1.846	13
14	3.102	2.726	2.522	2.395	2,307	2.63%		2,154	2.122	2.095				1.933		1,869	1.846		1.822	1.797	14
15	3.073	2.695	2.490	2.361	2,273	2.208	2.158	2.119	2.086	2.059	2.017	1.972	1.924	1.894	1.873	1.828	1.805	1.793	1,781	1.755	15
16	3.048	2.668	2.462	2.333	2.244	2.178	2.128	2.088	2.055	2.028	1.985	1.940	1.891	1.860	1.839	1.793	1.769	1.757		1.718	16
17	3.026	2.645	2.437	2.308	2.218	2.152	2,102	2,061	2.028	2.001	1.958	1.912	1.862	1.831	1.809	190000000	1.738	1.726		1,686	17
18	3.007	2.624	2.416	2.286	2.196	2.130	2.079		2.005	1.977		1.887	1.837	1.805	1.783	1.736		1.698	1.684	1.657	18
19	2.990		2.397		2.176	2.109	2.058	2.017	1.984	1.956	100000000000000000000000000000000000000			1.782		1.711	1.686	1.673		1.631	19
20	2.975	2.589	2,380	2.249	2.158	2.091	2.040	1.999	1.965	1.937	1.892	1,845	1.794	1.761	1,738	1.690	1.364	1.650	1.636	1.607	20
21	2.961	2.575	2.365	2.233	2.142	2.075	2.023	1.982	1.948	1.920	1.875	1.827	1.776	1.742	1.719	1.670	1.644	1.630	1,616	1.586	21
22	2.949	2.561	2.351	2.219	2.128	2.060	2.008	1.967	1,933	1.904	1.859	1.811	1.759	1.726	1.702	1.652	1.625	1.611		1.567	22
23	2.937	2.549	2.339	2.207	2.115	2.047	1,995	1.953	1.919	1.890	1.845	1.796	1.744	1.710	1.686	1.636	1.609	1.594	1.580	1.549	23
24			2.327		2.103	2.035	1.983	1.941	1,906	1.877		1,783		1.696	1.672	1.621	1.593	1.579		1.533	24
25	2.918	2.528	2.317	2.184	2.092	2.024	1.971	1.929	1.895	1.866	1.820	1.771	1.718	1.683	1.659	1.607	1.579	1.565	1.549	1,518	25
30	2.881	2.489	2.276	2.142	2.049	1.980	1.927	1.884	1.849	1.819	1.773	1.722	1.667	1.632	1.606	1.552	1.523	1.507	1.491	1,456	30
35	2.855	2.461	2.247	2.113	2.019	1.950	1.896	1.852	1,817	1.787	1.739	1.688	1.632	1.595	1.569	1.513	1.482	1.465	1.448	1,411	35
40	2.835	2.440	2.226	2.091	1.997	1.927	1.873	1.829	1.793	1.763	1.715	1.662	1.605	1.568	1.541	N/555000		1.434		1.377	40
50	2.809		2.197	2.061	1.966	1.895	1.840	1.796	1.760	1.729			1.568	1.529	1.502	10000000	1.407		1.369	1.327	50
75	2.774	2.375	2.158	2.021	1.926	1.854	1,798	1.754	1.716	1.685	1,635	1.580	1.519	1.478	1.449	1.384	1.346	1,326	1.304	1,254	75
100	2.756	2.356	2.139	2.002	1.906	1.834	1,778	1.732	1.695	1.663	1,612	1.557	1.494	1.453	1.423	1.355	1,315	1.293	1.270	1.214	100
150	2.739	2.338	2.121	1.983	1.886	1.814	1.757	1.712	1.674	1.642	1.590	1.533	1.470	1.427	1.396	1.325	1.283	1.259	1.233	1.169	150
007	2.706	2.303	2.084	1.945	1.847	1.774	1.717	1.670	1.632	1.599	1.546	1.487	1,421	1.375	1.342	1.263	1.214	1,185	1.151	(1.0)	00

a = 0.06	R - 5%	$\alpha_2 = 10\%$	~ - 90%
q = 0.95	W1 - 370	$\alpha_2 - 10\%$	7 - 90%

וע	1	2	3	4	5	6	7	8	9	10	12	15	20	25	30	50	75	100	150	00	V1/V.
1	161.4	199.5	215.7	224.6	230.2	234.0	236.8	238.9	240.5	241.9	243.9	245.9	248.0	249.3	250.1	251.8	252.6	253.0	253.5	254.3	1
2	18.51	19.00	19.16	19.25	19.30	19.33	19.35	19.37	19.38	19.40	19.41	19.43	19,45	19.46	19.46	19.48	19.48	19.49	19.49	19.50	2
3	10.13	9.552	9.277	9.117	9.013	8.941	8.887	8.845	8.812	8.786	8.745	8.703	8.660	8.634	8.617	8.581	8.563	8.554	8.545	8.526	3
4	7.709	6.944	6.591	6.388	6.256	6.163	6.094	6.041	5.999	5.964	5.912	5.858	5.803	5.769	5.746	5.699	5.676	5.664	5.652	5.628	4
5	6.608	5.786	5.409	5.192	5.050	4.950	4.876	4.818	4.772	4.735	4.678	4.619	4.558	4.521	4.496	4.444	4.418	4,405	4.392	4.365	5
6	5.987	5.143	4.757	4.534	4.387	4.284	4.207	4.147	4.099	4.060	4.000	3.938	3.874	3.835	3.808	3.754	3.726	3.712	3.698	3.669	6
7	5.591	4.737	4.347	4.120	3.972	3.866	3.787	3.726	3.677	3.637	3.575	3.511	3.445	3.404	3.376	3.319	3.290	3.275	3.260	3.230	7
8	5.318	4.459	4.066	3.838	3.687	3.581	3.500	3.438	3.388	3,347	3.284	3.218	3.150	3.108	3.079	3.020	2.990	2.975	2.959	2.928	8
9	5.117	4.256	3.863	3.633	3.482	3.374	3.293	3.230	3.179	3.137	3.073	3.006	2.936	2.893	2.864	2.803	2.771	2.756	2.739	2.707	9
10	4.965	4.103	3.708	3.478	3.326	3.217	3.135	3.072	3.020	2.978	2.913	2.845	2.774	2.730	2.700	2.637	2.605	2.588	2.572	2.538	10
11	4.844	3.982	3.587	3.357	3.204	3.095	3.012	2.948	2.896	2.854	2.788	2.719	2.646	2.601	2.570	2.507	2.473	2.457	2,439	2.404	11
12	4.747	3.885	3.490	3.259	3.106	2.996	2.913	2.849	2.796	2.753	2.687	2.617	2.544	2.498	2.466	2.401	2.367	2.350	2.332	2.296	12
13	4.667	3.806	3.411	3.179	3.025	2.915	2.832	2.767	2.714	2.671	2.604	2.533	2.459	2.412	2,380	2.314	2.279	2.261	2.243	2.206	13
14	4.600	3.739	3.344	3.112	2.958	2.848	2.764	2.699	2.646	2.602	2.534	2.463	2.388	2.341	2.308	2.241	2.205	2.187	2.169	2,131	14
15	4.543	3.682	3.287	3.056	2.901	2.790	2.707	2.641	2.588	2.544	2.475	2.403	2.328	2.280	2.247	2.178	2.142	2.123	2.105	2.066	15
16	4.494	3.634	3.239	3.007	2.852	2.741	2.657	2.591	2.538	2.494	2.425	2.352	2.276	2.227	2.194	2.124	2.087	2.068	2.049	2.010	16
17	4.451	3.592	3.197	2.965	2.810	2.699	2.614	2.548	2.494	2.450	2.381	2.308	2.230	2.181	2.148	2.077	2.040	2.020	2.001	1.960	17
18	4.414	3.555	3.160	2.928	2.773	2.661	2.577	2.510	2.456	2.412	2.342	2.269	2.191	2.141	2.107	2.035	1.998	1.978	1.958	1.917	18
19	4.381	3.522	3.127	2.895	2.740	2.628	2.544	2.477	2.423	2.378	300000000	AND SHEET	2.155	2.106		1.999		1.940	1.920	1.878	19
20	4.351	3.493	3.098	2.866	2.711	2.599	2.514	2.447	2.393	2.348	2.278	2.203	2.124	2.074	2.039	1.966	1.927	1.907	1.886	1.843	20
21	4.325	3.467	3.072	2.840	2.685	2.573	2.488	2.420	2.366	2.321	2.250	2.176	2.096	2.045	2.010	1.936	1.897	1.876	1.855	1.812	21
22	4.301	3.443	3.049	2.817	2.661	2.549	2.464	2.397	2.342	2.297	2.226	2.151	2.071	2.020	1.984	1.909	1.869	1.849	1.827	1.783	22
23	4.279	3.422	3.028	2.796	2.640	2.528	2.442	2.375	2.320	2.275	2.204	2.128	2.048	1.996	1.961	1.885	1.844	1.823	1.802	1.757	23
24	4.260	3.403	3.009	2.776		2.508	2.423	2.355	2.300	2.255	38433	2.108		1.975		1.863	1.822		1.779	1.733	24
25	4.242	3.385	2.991	2.759	2.603	2.490	2.405	2.337	2.282	2.236	2.165	2.089	2.007	1.955	1.919	1.842	1.801	1.779	1.757	1.711	25
30	4.171	3,316	2.922	2.690	2.534	2.421	2.334	2.266	2.211	2.165	2.092		1.932	1.878	1.841	1.761			1.672	1.622	30
35	4.121	3.267	2.874	2.641	2.485	2.372	2.285	2.217	2.161	2.114	503 Att	120000	1.878		1.786	1.703		1.635	1.610	1.558	35
40	4.085	3.232	2.839		2.449	2.336	2.249	2.180	2.124	2.077	2.003		1.839	1.783		201125583	1.614		1.564	1.509	40
50	4.034		2.790	2.557	2.400	2.286	2.199	2.130	2.073	2.026	1.952	1.871		1.727			1.551		1.498	1.438	50
75	3.968	3.119	2.727	2.494	2,337	2.222	2.134	2.064	2.007	1.959	1.884	1.802	1.712	1.653	1.611	1.518	1.466	1.437	1.407	1.338	75
100	3.936	3.087	2.696	2.463	2.305	2.191	2.103	2.032	1.975	1.927	1.850	1.768	1.676	1.616	1.573	1.477	1.422	1.392	1.359	1.283	100
150	3.904	3.056	2.665	2.432	2.274	2.160	2.071	2.001	1.943	1.894	1.817	1.734	1.641	1.580	1.535	1.436	1.377	1.345	1.309	1,223	150
00	3.841	2.996	2.605	2.372	2.214	2.099	2.010	1.938	1.880	1.831	1.752	1.666	1.571	1.506	1.459	1.350	1.283	1.243	1.197	(1.0)	00

							q =	0.975	$\alpha_1^R$	= 21/2%	α2=	5%	γ = 95	%							
V2 V1	1	2	3	4	5	6	7	8	9	10	12	15	20	25	30	50	75	100	150	00	V1 /V2
1	647.8	799.5	864.2	899.6	921.8	937.1	948.2	956.7	963.3	968.6	976.7	984.9	993.1	998.1	1001	1008	1011	1013	1015	1018	1
2	38.51	39.00	39.17	39.25	39.30	39.33	39.36	39.37	39.39	39.40	39.41	39.43	39.45	39.46	39.46	39.48	39.48	39.49	39.49	39.50	2
3	17.44	16.04	15.44	15.10	14.88	14.73	14.62	14.54	14.47	14.42	14.34	14.25	14.17	14.12	14.08	14.01	13.97	13.96	13.94	13.90	3
4	12.22	10.65	9.979	9.605	9.364	9.197	9.074	8.980	8.905	8.844	8.751	8.657	8.560	8.501	8.461	8.381		8.319	8.299	8.257	4
5	10.01	8.434	7.764	7.388	7.146	6.978	6.853	6.757	6.681	6.619	6.525	6.428	6.329	6.268	6.227	6.144	6.101	6.080	6.059	6.015	5
6	8.813	7.260	6.599	6.227	5.988	5.820	5.695	5.600	5.523	5.461	5.366	5.269	5.168	5.107	5.065	4.980	4.937	4.915	4.893	4.849	6
7	8.073	6.542	5.890	5.523	5.285	5.119	4.995	4.899	4.823	4.761	4.666	4.568	4.467	4.405	4.362	4.276	4,232	4.210	4.188	4.142	7
8	7.571	6.059	5.416	5.053	4.817	4.652	4.529	4,433	4.357	4.295	4.200	4.101	3.999	3.937	3.894	3.807	3.762	3.739	3.716	3.670	8
9	7.209	5.715	5.078		4.484	4.320	4.197	4.102	4.026	3.964	3.868	3.769	3.667	3.604		3.472		3.403	3.380	3.333	9
10	6.937	5.456	4.826	4.468	4.236	4.072	3.950	3.855	3,779	3.717	3.621	3.522	3.419	3.355	3.311	3.221	3.175	3.152	3.128	3.080	10
11	,6.724	5.256	4.630	4.275	4.044	3.881	3.759	3.664	3.588	3.526	3.430	3.330	3.226	3.162	3.118	3.027	2.980	2.956	2.932	2.883	11
12	6.554	5.096	4.474	4.121	3.891	3.728	3.607	3.512	3.436	3.374	3.277	3.177	3.073	3.008	2.963	2.871	2.824	2.800	2.775	2.725	12
13	6.414	4.965	4.347	3.996	3.767	3.604	3.483	3.388	3.312	3.250	3.153	3.053	2.948	2.882	2.837	2.744	2.696	2.671	2.647	2.595	13
14	6.298	4.857	4.242	3.892	3.663	3.501	3.380	3.285	3.209	3.147	3.050	2.949	2.844	2.778	2.732	2.638	2.590	2.565	2.539	2.487	14
15	6.200	4.765	4.153	3.804	3.576	3.415	3.293	3.199	3.123	3.060	2.963	2.862	2.756	2.689	2.644	2.549	2.499	2.474	2.448	2.395	15
16	6.115	4.687	4.077	3.729	3.502	3.341	3.219	3,125	3.049	2,986	2.889	2.788	2.681	2.614	2.568	2.472	2.422	2.396	2.370	2.316	16
17	6.042	4.619	4.011	3.665	3.438	3.277	3.156	3.061	2.985	2.922	2.825	2.723	2.616	2.548	2.502	2.405	2.355	2.329	2.302	2.247	17
18	5.978	4.560	3.954	3.608	3.382	3.221	3.100	3.005	2.929	2.866	2.769	2.667	2.559	2.491	2.445	2.347	2.296	2.269	2.242	2.187	18
19	5.922	4.508	3.903	3.559	3.333	3.172	3.051	2.956	2.880	2.817	2.720	2.617	2.509	2.441	2.394	2.295	2.243	2.217	2.190	2.133	19
20	5.871	4.461	3.859	3.515	3.289	3.128	3.007	2.913	2.837	2.774	2,676	2.573	2.464	2.396	2.349	2.249	2.197	2.170	2.142	2.085	20
21	5.827	4.420	3.819	3.475	3.250	3.090	2.969	2.874	2.798	2.735	2,637	2.534	2.425	2.356	2.308	2.208	2.155	2,128	2.100	2.042	21
22	5.786	4.383	3.783	3.440	3.215	3.055	2.934	2.839	2.763	2.700	2.602	2.498	2.389	2.320	2.272	2.171	2.118	2.090	2.062	2.003	22
23	5.750	3.349	3.750	3.408	3.183	3.023	2.902	2.808	2.731	2.668	2.570	2.466	2.357	2.287	2.239	2.137	2.084	2.056	2.027	1.968	23
24	5.717	4.319	3.721	3.379	3.155	2.995	2.874	2.779	2.703	2.640	2.541	2.437	2.327	2.257	2.209	2.107	2.052	2.024	1.995	1.935	24
25	5.686	4.291	3.694	3.353	3.129	2.969	2.848	2.753	2.677	2.613	2.515	2.411	2.300	2.230	2.182	2.079	2.024	1.996	1.966	1.906	25
30	5.568	4.182	3.589	3.250	3.026	2.867	2.746	2.651	2.575	2.511	2,412	2.307	2.195	2.124	2.074	1.968	1.911	1.882	1.851	1.787	30
35	5.485	4.106	3.517	3.179	2.956	2.796	2.676	2.581	2.504	2,440	2.341	2.235	2.122	2.049	1.999	1.890	1.832	1.801	1.769	1.702	35
40	5.424	4.051	3.463	3.126	2.904	2.744	2.624	2.529	2.452	2.388	2.288	2.182	2.068	1.994	1.943	1.832	1.772	1.741	1.708	1.637	40
50	5.340	3.975	3.390	3.054	2.833	2.674	2.553	2.458	2.381	2.317	2.216	2.109	1.993	1.919	1.866	1.752	1.689	1.656	1.621	1.545	50
75	5.232	3.876	3.296	2.962	2.741	2.582	2.461	2.366	2.289	2.224	2.123	2.014	1.896	1.819	1.765	1.645	1.578	1.542	1.503	1.417	75
100	5.179	3.828	3.250	2.917	2.696	2.537	2,417	2.321	2.244	2.179	2.077	1.968	1.849	1.770	1.715	1.592	1.522	1,483	1,442	1.347	100
150	5.126	3.781	3.204	2.872	2.652	2.494	2.373	2.278	2.200		2.032	1,922	1.801	1.722		1.538	1.464		1,379	1.271	150
00	5.024	3.689	3.116	2.786	2.567	2.408	2,288	2.192	2.114	2.048	1.945	1.833	1.708	1.626	1,566	1,428	1.345	1,296	1.239	(1.0)	00
100000		0.535555	and the same		in the second	2	-,	-0186		-15.15	1.0.0				. 1000			. 1200		(1107)	

P2 1	1	2	3	4	5	6	7	8	9	10	12	15	20	25	30	50	75	100	150	00	V1/0
1	4052	4999	5403	5625	5764	5859	5928	5981	6022	6056	6106	6157	6209	6240	6261	6303	6324	6334	6345	6366	
2	98.50	99.00	99.17	99.25	99.30	99.33	99.36	99.37	99.39	99.40	99.42	99.43	99.45	99.46	99.47	99.48	99.49	99.49	99.49	99.50	
3		30.82	29.46	28.71	28.24	27.91	27.67	27.49	27.35	27.23	27.05	26.87	26.69		26.50	26.35	26.28	26.24	26.20	26.13	
4	21.20	18.00	16.69	15.98	15.52	15.21	14.98	14.80	14.66	14.55		14.20	14.02		2000000	13.69		13.58 9.130	13.54 9.094	9.020	
5		13.27	12.06	11.39	10.97	10.67	10.46	10.29	10.16	10.05	9.888	9.722	9.553	9.449	9.379	9.238	1100000000	100000000000000000000000000000000000000	TOTAL COST		
6		10.92		9.148		8.466	8.260	8.102	7.976	7.874		7.559	7.396		7.229	7.091	7.022		6.951	6.880	
7 8		9.547	8.451 7.591	7.847		7.191 6.371	6.993 6.178	6.840	6.719 5.911	6.620 5.814	6.469	6.314 5.515	5.359	6.058 5.263	5,992	5.858 5.065	4.998	5.755	5.720 4.929	5.650 4.859	
9		8.022	6.992	6.422	750.07	5.802	5.613		5.351	5.257		4.962	4.808	4.713	534503	15 Sept 5 5 5 5	4.449		4.380	4.311	
10		7.559	6.552		5.636	5.386	5.200	5.057	4.942	4.849		4.558		4.311			4.048		3.979	3,909	1
OMICS.			6.217	5.668	5.316				4.632			4.251	4.099		3.941	2 010	3.742	2 700	3.673	3.602	1
11		7.206 6.927	5.953	5.412	5.064	5.069 4.821	4.886	4.744	4.032	4.539 4.296		4.010	3.858	3.765	3.701	3.569	3.501		3.432	3.361	1
13		6.701	5.739	5.205	4.862	4.620	4.441		4.191	4.100	3.960	3.815		3.571	3.507	13500000		3.272		3.165	1
14			5.564	5.035	4.695	4.456	4.278	4.140	4.030	3.939	3.800			3.412	200	3.215	3.147	3.112	3.076	3.004	1
15	8.683	6.359	5.417	4.893	4.556	4.318	4.142	4.004	3.895	3.805	3.666	3.522	3.372	3.278	3.214	3.081	3.012	2.977	2.942	2.868	1
16	8.531	6.226	5.292	4.773	4,437	4.202	4.026	3.890	3.780	3.691	3.553	3.409	3.259	3.165	3.101	2.967	2.898	2.863	2.827	2.753	1
17	8.400	6.112	5.185	4.669	4.336	4.102	3.927	3.791	3.682	3.593	3.455	3.312	3.162	3.068	3.003	2.869	2.800	2.764	2.728	2.653	1
18	8.285	6.013	5.092	4.579	4.248	4.015	3.841	3.705	3.597	3.508	3.371	3.227	3.077	2.983	2.919	2.784	2.714	2.678	2.641	2.566	1
19	8.185	5.926	5.010	4.500	4.171	3.939	3.765	3.631	3.523	3.434	3.297	3.153			2.844	2.709		2.602	2.565	2.489	1
20	8.096	5.849	4.938	4,431	4.103	3.871	3.699	3.564	3.457	3.368	3.231	3.088	2.938	2.843	2.778	2.643	2.572	2.535	2.498	2.421	2
21	8.017	5.780	4.874	4.369	4.042	3.812	3.640	3.506	3.398	3.310	3.173	3.030	2.880	2.785	2.720	2.584	2.512	2.475	2.438	2.360	2
22		5.719	4.817	4.313	3.988	3.758	3.587	3.453	3.346	3.258	3.121		2.827	2.733	2.667	2.531		2.422	2.384	2.305	2
23	7.881		4.765	4.264	3,939		3.539	3.406	3.299	3.211		2.931	2.781	2.686	2.620	2.483	2.411		2.335	2.256	1
24	-	5.614	4.718	4.218	3.895	3.667	3.496	3.363	3.256 3.217	3.168		2.889		2.643	2.577	2.440	2.367	2.329	2.291	2.211	2
1000		100000000000000000000000000000000000000		4.177		3.627	3.457		100000000000000000000000000000000000000	3.129	000000000000000000000000000000000000000							110000000000000000000000000000000000000			
30	7.562		4.510	4.018	3.699	3.473	3.304	3.173	3.067	2.979		2.700	2.549		2.386	2.245	2.170		2.091	2.006	3
35 40	7.419		4.396	3.908	3.592 3.514	3.368	3.200	3.069 2.993	2.963	2.876		2.597		2.348	2.281	2.137	2.060 1.980	2.020 1.938	1.979 1.896	1.891	4
50		5.057	4.313	3.720	3.408	3.291	3.124	2.890	2.785	2.698		2.522		2.167	2.203		1.868	1.825	1.780	1.683	
75			4.054	3.580	3.272	3.052	2.887	2.758	2.653	2.567	2.431		2.132		1.960		1.720	1.674	1.625	1.516	7
00	6.895	1 821	3.984	3.513		200000000000000000000000000000000000000	2.823	2.694	2.590	2.503	2 368	2,223	2.067	1.965	1.893	1.735	1.646	1.598	1.546	1.427	10
50	6.807		3.915	3.447	3.142	2.924		2.632	2.528	2.441		2.160	2.007		1.827		1.572	1.520	1.465	1.331	15
		000	3.782	0000011100			2,639		2,407			2.039	1.878				1,419		1.288	(1.0)	0

							q =	0.995	$\alpha_1^R$	= ½%	$\alpha_2 =$	1%	$\gamma = 99$	%							
7/2	1	2	3	4	5	6	7	8	9	10	12	15	20	25	30	50	75	100	150	60	V1/2
1	16211	20000	21615	22500	23056	23437	23715	23925	24091	24224	24426	24630	24836	24960	25044	25211	25295	25337	25380	25464	1
2	198.5	199.0	199.2	199.2	199.3	199.3	199.4	199.4	199.4	199.4	199.4	199.4	199.4	199.5	199.5	199.5	199.5	199.5	199.5	199.5	2
3	55.55	49.80	47.47	46.19	45.39	44.84	44.43	44.13	43.88	43.69	43.39	43.08	42.78	42.59	42.47		42.09	42,02	41.96	41.83	3
4	31.33			23.15			21.62		21.14	20.97	A 5 4 5 14 1	20,44	20.17		19.89			19.50	19.44	19.32	4
5	22.78	18.31	16.53	15.56	14.94	14.51	14.20	13.96	13.77	13.62	13.38	13.15	12.90	12.76	12.66	12.45	12.35	12.30	12.25	12.14	5
6	18.63	14.54	12.92	12.03	11.46	11.07	10.79	10.57	10.39	10.25	10.03	9.814	9,589	9.451	9.358	9.170	9.074	9.026	8.977	8.879	6
7	16.24	12.40	10.88	10.05	9.522	9.155	8.885	8.678	8.514	8.380	8.176	7.968	7.754	7.623	7.534	7.354	7.263	7.217	7.170	7.076	7
8	14.69	11.04	9.596	8.805	8,302	7.952	7.694	7.496	7.339	7.211	7.015	6.814	6.608	6.482	6.396		6.133		6.042	5.951	8
9		10.11	8.717		7.471		6.885	6.693	6.541	6.417	33732255	6.032	5.832		5.625		5.367		5.278	5.188	9
10	12.83	9.427	8.081	7.343	6.872	6.545	6.302	6.116	5.968	5.847	5.661	5.471	5.274	5.153	5.071	4.902	4.816	4.772	4.728	4.639	10
11	12.23	8.912	7.600	6.881	6.422	6.102	5.865	5.682	5.537	5.418	5.236	5.049	4.855	4.736	4.654	4.488	4.402	4.359	4.315	4.226	11
12	11.75	8.510	7.226	6.521	6.071	5.757	5.525	5.345	5.202	5.085	4.906	4.721	4.530	4.412	4,331	4.165	4.080	4.037	3.993	3.904	12
13	11.37	8.186	6.926	6.233	5.791	5.482	5.253	5.076	4.935	4.820	4.643	4.460	4.270	4.153	4.073		3.823		3.736	3.647	13
14	11.06	7.922	6.680	5.998	5.562	5.257	5.031	4.857	4.717	4.603	4.428	4.247	4.059	3.942	3.862		3.612		3.525	3,436	14
15	10.80	7.701	6.476	5.803	5.372	5.071	4.847	4.674	4.536	4.424	4.250	4.070	3.883	3.766	3.687	3.523	3,437	3,394	3.350	3.260	15
16	10.58	7.514	6.303	5.638	5.212	4.913	4.692	4.521	4.384	4.272	4.099	3.920	3.734	3.618	3.539	3.375	3.290	3.246	3.202	3.112	16
17	10.38	7.354	6.156	5.497	5.075	4.779	4.559	4.389	4.254	4.142	3.971	3.793	3.607	3.492	3.412	3.248	3.163	3.119	3.075	2.984	17
18	10.22	7.215	6.028	5.375	4.956	4.663	4.445	4.276	4,141	4.030	3.860	3.683	3.498	3.382	3.303		3.053		2.965	2.873	18
19	10.07	7.093	5.916	5.268	4.853	4.561		4.177		3.933	6888674	3.587	3.402	3.287	3.208		2,957		2.868	2.776	19
20	9.944	6.986	5.818	5.174	4.762	4.472	4.257	4.090	3.956	3.847	3.678	3.502	3.318	3,203	3.123	2.959	2.872	2.828	2.783	2.690	20
21	9.830	6.891	5.730	5.091	4.681	4.393	4.179	4.013	3.880	3.771	3.602	3.427	3.243	3.128	3.049	2.884	2.797	2.753	2.707	2.614	21
22	9.727	6.806	5.652	5.017	4.609	4.322	4.109	3.944	3.812	3.703	3.535	3.360	3.176	3.061	2.982	2.817	2.730	2.685	2.640	2.545	22
23	9.635	6.730	5.582	4.950	4.544	4.259	4.047	3.882	3.750	3.642	3.475	3.300	3.116	3.001	2.922	2.756	2.669	2.624	2.579	2.484	23
24	9.551	6.661	5.519	4.890	4.486	4.202	3.991	3.826	3.695	3.587	3.420	3.246	3.062	2.947	2.868		2.614		2.523	2.428	24
25	9.475	6.598	5.462	4.835	4.433	4.150	3.939	3.776	3.645	3.537	3.370	3.196	3.013	2.898	2.819	2.652	2.564	2.519	2.473	2.377	25
30	9.180	6.355	5.239	4.623	4.228	3.949	3.742	3.580	3.450	3.344	3.179	3.006	2.823	2.708	2.628	2.459	2.370	2.323	2.276	2.176	30
35	8.976	6.188	5.086	4.479	4.088	3.812	3.607	3.447	3.318	3.212	3.048	2.876	2.693	2.577	2.497	2.327		2.188	2.139	2.036	35
40	8.828	6.066	4.976	4.374	3.986	3.713		3.350	3.222	3.117	2.953			2.482	2.401	100000000000000000000000000000000000000	2.137		2.038	1.932	40
50		5.902			3.849			3.219		2.988	5.00	2.653	2.470		2.272		2.001		1.899	1.786	50
75	8.366	5.691	4.635	4.050	3.674	3.407	3.208	3.052	2.927	2.823	2.661	2.490	2.306	2.188	2.105	1.925	1.824	1.771	1.714	1.589	75
100	8.241	5.589	4.542	3.963	3.589	3.325	3.127	2.972	2.847	2.744	2.583	2.411	2.227	2.108	2.024	1.840	1.737	1.681	1.621	1.485	100
150	8.118	5.490	4.453	3.878	3.508	3.245	3.048	2.894	2.770	2.667	2.506	2.335	2.150	2.030	1.944	1.756	1.649	1.590	1.526	1.374	150
00	7.879	5.298	4.279	3.715	3.350	3.091	2.897	2.744	2.621	2.519	2.358	2.187	2.000	1.877	1.789	1.590	1.470	1.402	1.322	(1.0)	00

q = 0.999  $\alpha_1^R = 0.1\%$   $\alpha_2 = 0.2\%$   $\gamma = 99.8\%$ 

The values for  $v_2 = 1$  should be multiplied by 10

V2 V	1 1	2	3	4	5	6	7	8	9	10	12	15	20	25	30	50	75	100	150	00	V1 / V2
1	40528	50000	54038	56250	57640	58594	59287	59814	60228	60562	61067	61576	62091	62402	62610	63029	63239	63344	63450	63662	1
2	998.5	999.0	999.2	999.3	999.3	999.3	999.4	999.4	999.4	999.4	999.4	999.4	999.4	999.5	999.5	999.5	999.5	999.5	999.5	999.5	2
3	167.0	148.5	141.1	137.1	134.6	132.8	131.6	130.6	129.9	129.2	128.3	127.4	126.4	125.8	125.4	124.7	124.3	124.1	123.9	123.5	3
4	74.14	61.25	56.18	53.44	51.71	50.53	49.66	49.00	48.47	48.05	47.41	46.76	46.10	45.70	45.43	44.88	44.61	44.47	44.33	44.05	4
5	47.18	37.12	33.20	31.09	29.75	28.83	28.16	27.65	27.24	26.92	26.42	25.91	25.39	25.08	24.87	24.44	24.22	24.12	24.01	23.79	5
6	35.51	27.00	23.70	21.92	20.80	20.03	19.46	19.03	18.69	18.41	17.99	17.56	17.12	16.85	16.67	16.31	16.12	16.03	15.93	15.75	6
7	29.25	21.69	18.77	17.20	16.21	15.52	15.02	14.63	14.33	14.08	13.71	13.32	12.93	12.69	12.53	12.20	12.04	11.95	11.87	11.70	7
8	25.41	18.49	15.83	14.39	13.48	12.86	12.40	12.05	11.77	11.54	11.19	10.84	10.48	10.26	10.11	9.804	9.650	9.571	9.493	9.334	8
9	22.86	16.39	13.90	12.56	11.71	11.13	10.70	10.37	10.11	9.894	9.570	9.238	8.898	8.689	8.548	8.260	8.113	8.039	7.964	7.813	9
10	21.04	14.91	12.55	11.28	10.48	9.926	9.517	9.204	8.956	8.754	8.445	8.129	7.804	7.604	7.469	7.193	7.052	6.980	6.908	6.762	10
11	19.69	13.81	11.56	10.35	9.578	9.047	8.655	8.355	8.116	7.922	7.626	7.321	7.008	6.815	6.684	6.416	6,280	6.210	6.140	5,998	11
12	18.64	12.97	10.80	9.633	8.892	8.379	8.001	7.710	7.480	7.292	7.005	6.709	6.405	6.217	6.090	5.829	5.695	5.627	5.559	5.420	12
13	17.82	12.31	10.21	9.073	8.354	7.856	7.489	7.206	6.982	6.799	6.519	6.231	5.934	5.751	5.626	5.370	5.239	5.172	5.104	4.967	13
14	17.14	11.78	9.729	8.622	7.922	7.436	7.077	6.802	6.583	6.404	6.130	5.848	5.557	5.377	5.254	5.002	4.873	4.807	4.740	4.604	14
15	16.59	11.34	9.335	8.253	7.567	7.092	6.741	6.471	6.256	6.081	5.812	5.535	5.248	5.071	4.950	4.702	4.573	4.508	4.442	4.307	15
16	16.12	10.97	9.006	7.944	7.272	6.805	6.460	6.195	5.984	5.812	5.547	5.274	4.992	4.817	4.697	4.451	4.324	4.259	4.193	4.059	16
17	15.72	10.66	8.727	7.683	7.022	6.562	6.223	5.962	5.754	5.584	5.324	5.054	4.775	4.602	4.484	4.239	4.113	4.049	3.983	3.850	17
18	15.38	10.39	8.487	7.459	6.808	6.355	6.021	5.763	5.558	5.390	5.132	4.866	4.590	4.418	4.301	4.058	3.933	3.868	3.803	3.670	18
19	15.08	10.16	8.280	7.265	6.622	6.175	5.845	5.590	5.388	5.222	4.967	4.704	4.430	4.259	4.143	3.902	3.777	3.713	3.647	3.514	19
20	14.82	9.953	8.098	7.096	6.461	6.019	5.692	5.440	5.239	5.075	4.823	4.562	4.290	4.121	4.005	3.765	3.640	3.576	3.511	3.378	20
21	14.59	9.772	7.938	6.947	6.318	5.881	5.557	5.308	5.109	4.946	4.696	4.437	4.167	3.999	3.884	3,645	3.520	3.456	3,391	3.257	21
22	14.38	9.612	7.796	6.814	6.191	5.758	5.438	5.190	4.993	4.832	4.583	4.326	4.058	3.891	3.776	3.538	3,413	3.349	3.284	3.151	22
23	14.20	9.469	7.669	6.696	6.078	5.649	5.331	5.085	4.890	4.730	4.483	4.227	3.961	3.794	3.680	3.442	3.318	3.254	3.189	3.055	23
24	14.03	9.339	7.554	6.589	5.977	5.550	5.235	4.991	4.797	4.638	4.393	4.139	3.873	3.707	3.593	3.356	3.232	3.168	3.103	2.969	24
25	13.88	9.223	7.451	6.493	5.885	5.462	5.148	4.906	4.713	4.555	4.312	4.059	3.794	3.629	3.515	3.279	3.154	3.091	3.025	2.890	25
30	13.29	8.773	7.054	6.125	5.534	5.122	4.817	4.581	4.393	4.239	4.001	3.753	3.493	3.330	3.217	2.981	2.857	2.792	2.726	2.589	30
35	12.90	8.470	6.787	5.876	5.298	4.894	4.595	4.363	4.178	4.027	3.792	3.547	3.290	3.128	3.016	2.781	2.655	2.590	2.523	2.383	35
40	12.61	8.251	6.595	5.698	5.128	4.731	4.436	4.207	4.024	3.874	3.642	3.400	3.145	2.984	2.872	2.636	2.510	2.444	2.376	2.233	40
50	12.22	7.956	6.336	5.459	4.901	4.512	4.222	3.998	3.818	3.671	3.443	3.204	2.951	2.790	2.679	2.441	2.313	2.246	2.176	2.026	50
75	11.73	7.585	6.011	5.159	4.617	4.237	3.955	3.736	3.561	3.416	3.192	2.957	2.707	2.547	2.435	2.194	2.062	1.992	1.917	1.754	75
100	11.50	7.408	5.857	5.017	4.482	4.107	3.829	3.612	3.439	3.296	3.074	2.840	2.591	2.431	2.319	2.076	1,940	1.867	1.790	1.615	100
150	11.27	7.236	5.707	4.879	4.351	3.981	3.706	3.493	3.321	3.179	2.959	2.727	2.479	2.319	2.206	1.959	1.820	1.744	1.662	1.469	150
00	10.83	6.908	5.422	4.617	4.103	3.743	3.475	3.266	3.097	2.959	2.742	2.513	2.266	2.105	1.990	1.733	1.581	1.494	1.395	(1.0)	00

q = 0.9999  $\alpha_1^R = 0.01\%$   $\alpha_2 = 0.02\%$   $\gamma = 99.98\%$ 

The values for  $\nu_2=1$  should be multiplied by 1000

Po Pi	1	2	3	4	5	6	7	8	9	10	12	15	20	25	30	50	75	100	150	00	2
1	40528	50000	54038	56250	57640	58594	59287	59814	60228	60'562	61067	61576	62091	62402	62610	63029	63239	63344	63450	63662	T 2
2	9999	9999	9999	9999	9999	9999	9999	9999	9999	9999	9999	9999	9999	9999	9999	9999	9999	9999	9999	9999	
3	784.0	694.7	659.3	640.2	628.2	619.9	613.9	609.3	605.7	602.8	598.3	593.8	589.3	586.5	584.7	581.0	579.1	578.1	577.2	575.3	
4	241.6	198.0	181.0	171.9	166.1	162.2	159.3	157.1	155.4	154.0	151.9	149.7	147.5	146.2	145.3	143.5	142.6	142.1	141.7	140.8	139
5	124.9	97.03	86.29	80.53	76.91	74.43	72.61	71.23	70.13	69.25	67.91	66.54	65.16	64.31	63.75	62.60	62.02	61.73	61.43	60.84	100
6	82.49	61.63	53.68	49.42	46.75	44.91	43.57	42.54	41.73	41.08	40.08	39.07	38.04	37,41	36.98	36.13	35.69	35.47	35.25	34.81	13
7	62.17	45.13	38.68	35.22	33.06	31.57	30.48	29.64	28.99	28.45	27.64	26.82	25.98	25.46	25.12	24.42	24.06	23.88	23.70	23.34	18
8	50.69	36.00	30.46	27.49	25.63	24.36	23.42	22.71	22.14	21.68	20.98	20.27	19.55	19.10	18.80	18.19	17.89	17.73	17.57	17.26	
9	43.48	30.34	25.40	22.77	21.11	19.97	19.14	18.50	18.00	17.59	16.97	16.33	15.68	15.28	15.01	14.47	14.19	14.05	13.91	13.62	
10	38.58	26.55	22.04	19.63	18.12	17.08	16.32	15.74	15.27	14.90	14.33	13.75	13.15	12.78	12.54	12.03	11.77	11.65	11.51	11.25	1
11	35.06	23.85	19.66	17.42	16.02	15.05	14.34	13.80	13.37	13.02	12.49	11.95	11.39	11.05	10.81	10.34	10.10	9.977	9.854	9.605	1
12	32.43	21.85	17.90	15.79	14.47	13.56	12.89	12.38	11.98	11.65	11.14	10.63	10.10	9.777	9.557	9.108	8.878	8.762	8.644	8.406	
13	30.39	20.31	16.55	14.55	13.29	12.42	11.79	11.30	10.92	10.60	10.12	9.632	9.127	8.816	8.606	8.175	7.954	7.842	7.729	7.500	
14	28.77	19.09	15.49	13.57	12.37	11.53	10.92	10.46	10.09	9.785	9.325	8.853	8.366	8.067	7.864	7.448	7.234	7.126	7.016	6.793	
15	27.45	18.11	14.64	12.78	11.62	10.82	10.23	9.780	9.422	9.131	8.686	8.229	7.758	7.468	7.271	6.866	6.658	6.553	6.446	6.229	
16	26.36	17.30	13.93	12.14	11.01	10.23	9.663	9.226	8.878	8.596	8.164	7.720	7.262	6.979	6.787	6.392	6.189	6.086	5.981	5.768	
17	25.44	16.62	13.34	11.60	10.50	9.747	9.191	8.765	8.427	8.152	7.730	7.297	6.850	6.573	6.385	5.999	5.799	5.698	5.595	5.385	
18	24.66	16.04	12.85	11.14	10.07	9.335	8.792	8.376	8.046	7.777	7.365	6.941	6.503	6.232	6.047	5.667	5.471	5.371	5.270	5.063	
19	23.99	15.55	12.42	10.75	9.706	8.983	8.452	8.044	7.720	7.457	7.053	6.637	6.207	5.941	5.759	5.385	5.191	5.093	4.993	4.788	100
20	23.40	15.12	12.05	10.41	9.388	8.679	8.158	7.757	7.439	7.181	6.784	6.375	5.952	5.689	5.510	5.141	4.950	4.852	4.753	4.550	
21	22.89	14.74	11.73	10.12	9.111	8.414	7.901	7.507	7.195	6.940	6.549	6.147	5.729	5.471	5.294	4.929	4.740	4.643	4.545	4.344	
22	22.43	14.41	11.44	9.860	8.867	8.180	7.676	7.288	6.980	6.729	6.343	5.946	5.534	5.279	5.104	4.743	4.555	4.459	4.362	4.162	13
23	22.03	14.12	11.19	9.630	8.651	7.974	7.476	7.093	6.789	6.542	6.161	5.769	5.362	5.109	4.936	4.578	4.392	4.297	4.200	4.000	13
24	21.66	13.85	10.96	9.425	8.458	7.790	7.298	6.920	6.620	6.375	5.999	5.611	5.208	4.958	4.787	4.432	4.247	4.152	4.055	3.857	
25	21.34	13.62	10.76	9,240	8.285	7.624	7.138	6.765	6.468	6.226	5.854	5.470	5.071	4.823	4.653	4.300	4.116	4.022	3.926	3.728	
30	20.09	12.72	9.994	8.544	7.632	7.002	6.537	6.180	5.896	5.664	5.308	4.939	4.554	4.314	4.149	3.806	3.625	3.532	3.437	3.240	
35	19.26	12.12	9.487	8.084	7.202	6.592	6.143	5.796	5.521	5.296	4.950	4.591	4.216	3.981	3.819	3.481	3.303	3.210	3.115	2.918	1
40	18.67	11.70	9.128	7.759	6.899	6.303	5.864	5.526	5.256	5.036	4.697	4.345	3.977	3.746	3.587	3.252	3.074	2.982	2.887	2.688	1
50	17.88	11.14	8.652	7,330	6.498	5.922	5.497	5.170	4.909	4.695	4.366	4.024	3.664	3.438	3.281	2.950	2.773	2.680	2.584	2.380	0
75	16.89	10.44	8.066	6.802	6.006	5.455	5.048	4.734	4.483	4.278	3.961	3.630	3.281	3.060	2.907	2.578	2.399	2.304	2.205	1.988	8
00	16.43	10.11	7.791	6.555	5.777	5.237	4.839	4.531	4.285	4.084	3.773	3.448	3.104	2.885	2.732	2.404	2.223	2.126	2.024	1.795	1
50	15.98	9.800	7.528	6.319	5.558	5.030	4.640	4.338	4.097	3.900	3.594	3.274	2.934	2.718	2.566	2.236	2.052	1.953	1.846	1.597	1
×	15.14	9.210	7.036	5.878	5.149	4.643	4.268	3.978	3.747	3.556	3.261	2.951	2.619	2.406	2.254	1.919	1.724	1.613	1.487	(1.0)	0

# Critical values for the Kolmogorov-Smirnov goodness-of-fit test (for completely specified distributions)

$\alpha_1$	5%	21/2%	1%	1/2%
$\alpha_2$	10%	5%	2%	1%
n				
1	0.9500	0.9750	0.9900	0.9950
2	0.7764	0.8419	0.9000	0.9293
3	0.6360	0.7076	0.7846	0.8290
4	0.5652	0.6239	0.6889	0.7342
5	0.5094	0.5633	0.6272	0.668
6	0.4680	0.5193	0.5774	0.6166
7	0.4361	0.4834	0.5384	0.5758
8	0.4096	0.4543	0.5065	0.5418
9	0.3875	0.4300	0.4796	0.513
10	0.3687	0.4092	0.4566	0.488
11	0.3524	0.3912	0.4367	0.467
12	0.3382	0.3754	0.4192	0.4490
13	0.3255	0.3614	0.4036	0.432
14	0.3142	0.3489	0.3897	0.417
15	0.3040	0.3376	0.3771	0.404
16	0.2947	0.3273	0.3657	0.3920
17	0.2863	0.3180	0.3553	0.3809
18	0.2785	0.3094	0.3457	0.3706
19	0.2714	0.3014	0.3369	0.3612
20	0.2647	0.2941	0.3287	0.3524

$\alpha_1$	5%	21/2%	1%	1/2%
α2	10%	5%	2%	1%
n				
21	0.2586	0.2872	0.3210	0.3443
22	0.2528	0.2809	0.3139	0.3367
23	0.2475	0.2749	0.3073	0.3295
24	0.2424	0.2693	0.3010	0.3229
25	0.2377	0.2640	0.2952	0.3166
26	0.2332	0.2591	0.2896	0.3106
27	0.2290	0.2544	0.2844	0.3050
28	0.2250	0.2499	0.2794	0.2997
29	0.2212	0.2457	0.2747	0.2947
30	0.2176	0.2417	0.2702	0.2899
31	0.2141	0.2379	0.2660	0.2853
32	0.2108	0.2342	0.2619	0.2809
33	0.2077	0.2308	0.2580	0.2768
34	0.2047	0.2274	0.2543	0.2728
35	0.2018	0.2242	0.2507	0.2690
36	0.1991	0.2212	0.2473	0.2653
37	0.1965	0.2183	0.2440	0.2618
38	0.1939	0.2154	0.2409	0.2584
39	0.1915	0.2127	0.2379	0.2552
40	0.1891	0.2101	0.2349	0.2521

$\alpha_1$	5%	21/2%	1%	1/2%
$\alpha_2$	10%	5%	2%	1%
n				
41	0.1869	0.2076	0.2321	0.2490
42	0.1847	0.2052	0.2294	0.2461
43	0.1826	0.2028	0.2268	0.2433
44	0.1805	0.2006	0.2243	0.2406
45	0.1786	0.1984	0.2218	0.2380
46	0.1767	0.1963	0.2194	0.2354
47	0.1748	0.1942	0.2171	0.2330
48	0.1730	0.1922	0.2149	0.2306
49	0.1713	0.1903	0.2128	0.2283
50	0.1696	0.1884	0.2107	0.2260
55	0.1619	0.1798	0.2011	0.2157
60	0.1551	0.1723	0.1927	0.2067
65	0.1491	0.1657	0.1853	0.1988
70	0.1438	0.1597	0.1786	0.1917
75	0.1390	0.1544	0.1727	0.1853
80	0.1347	0.1496	0.1673	0.1795
85	0.1307	0.1452	0.1624	0.1742
90	0.1271	0.1412	0.1579	0.1694
95	0.1238	0.1375	0.1537	0.1649
100	0.1207	0.1340	0.1499	0.1608

Goodness-of-fit tests are designed to test a null hypothesis that some given data are a random sample from a specified probability distribution. The Kolmogorov-Smirnov tests are based on the maximum absolute difference  $D_n$  between the c.d.f. (cumulative distribution function)  $F_0(x)$  of the hypothesised distribution and the c.d.f. of the sample (sometimes called the empirical c.d.f.)  $F_n(x)$ . This sample c.d.f. is the step-function which starts at 0 and rises by 1/n at each observed value, where n is the sample size; i.e.  $F_n(x)$  is equal to the proportion of the sample values which are less than or equal to x.

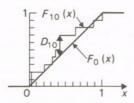
Critical regions for rejecting  $H_0$  are of the form  $D_n \geqslant tabulated$  value, and in most cases the general alternative hypothesis is appropriate, i.e. the  $\alpha_2$  significance levels should be used. One-sided alternative hypotheses can be dealt with by only considering differences in one direction between the c.d.f.s. For example, suppose  $H_1$  says that the actual values being sampled are mainly less than those expected from  $F_0(x)$ . If this is the case  $F_n(x)$  will tend to rise earlier than  $F_0(x)$ , and so instead of  $D_n$  we should then use the statistic  $D_n^+ = \max{\{F_n(x) - F_0(x)\}}$ . In the opposite case, where  $H_1$  says that the values sampled are mainly greater than those expected from  $F_0(x)$ , we should use  $D_n^- = \max{\{F_0(x) - F_n(x)\}}$ . Critical regions are  $D_n^+$  (or  $D_n^-$ )  $\geqslant tabulated$  value, and in these one-sided tests the  $\alpha_1$  significance levels should be used.

For illustration, let us test the null hypothesis  $H_0$  that the following ten observations (derived in fact from part of the top row of the table of random digits on page 42) are a random sample from the uniform distribution over (0:1), having c.d.f.  $F_0(x) = 0$  for x < 0,  $F_0(x) = x$  for  $0 \le x \le 1$ , and  $F_0(x) = 1$  for x > 1:

0.02484 0.88139 0.31788 0.35873 0.63259 0.99886 0.20644 0.41853 0.41915 0.02944

Sorting the data into ascending order, we have:

 $0.02484 \quad 0.02944 \quad 0.20644 \quad 0.31788 \quad 0.35873 \quad 0.41853 \quad 0.41915 \quad 0.63259 \quad 0.88139 \quad 0.99886$ 



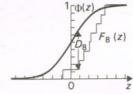
It is then easy to draw the sample c.d.f.,  $F_{10}(x)$ , and from the diagram we find that the maximum vertical distance between the two c.d.f.s, which occurs at x=0.41915, is  $D_{10}=0.7-0.41915=0.28085$ . But the critical region for rejection of  $H_0$  even at the  $\alpha_2=16\%$  significance level is  $D_{10} \ge 0.3687$ , and so we have no reason here to doubt the null hypothesis.

The Kolmogorov-Smirnov test may be used both when  $F_0(x)$  is

continuous and discrete. In the continuous case critical values are exact; in the discrete case they may be conservative (i.e. true  $\alpha <$  nominal  $\alpha$ ).

A particularly useful application of the test is to test data for normality. In this case use may be made of the graph on page 27 of the c.d.f. of the standard normal distribution by first standardising the data, i.e. subtracting the mean and dividing by the standard deviation. The resulting sample c.d.f. may be drawn on page 27 and the Kolmogorov-Smirnov test performed as usual. For example to test the hypothesis that the following data come from the normal distribution with mean 5 and standard deviation 2, we transform each observation X into  $Z = \frac{1}{2}(X-5)$ :

(original) X	8.74	4.08	8.31	7.80	6.39	7.21	7.05	5.94
(transformed) Z	1.87	-0.46	1.655	1.40	0.695	1.105	1.025	0.47



Then we sort the transformed data into ascending order and draw the sample c.d.f. on the graph on page 27 (step-heights are 1/8 since the sample size n is 8 here). The maximum vertical distance between the two c.d.f.s is seen to be about 0.556, and this shows strong evidence that the data do not come from the hypothesised distribution, since the  $\alpha_2 = 1\%$  critical region is  $D_8 \ge 0.5418$ .

Perhaps it is more commonly necessary to test for normality without the mean and standard deviation being specified. To perform the test in these circumstances, first estimate the mean by  $\bar{X} = \Sigma X/n$  and the standard deviation by  $s = \{\Sigma (X - \bar{X})^2/(n-1)\}^{1/2}$ . Standardise the data using these estimates, and then proceed as before except that the critical values on page 27 should be used. For the above eight observations,  $\bar{X} = 6.940$  and s = 1.484. The transformed data are now:

1.213 -1.927 0.923 0.579 -0.371 0.182 0.074 -0.67	1	1.213	-1.927	0.923	0.579	-0.371	0.182	0.074	-0.674
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the maximum difference now found between the c.d.f. of this sample and that of the standard normal distribution is  $D_8 = 0.155$ , and this is certainly not significantly large, for even at the  $\alpha_2 = 10\%$  level the critical region is  $D_8 \ge 0.2652$ . We conclude therefore that although there was strong evidence that the data do not come from the originally specified normal distribution, they could quite easily have come from some other normal distribution. The originator of this type of test was W. H. Lilliefors.

Critical values for larger sample sizes than covered in the tables are discussed on page 35.

## Critical values for the Kolmogorov-Smirnov test for normality

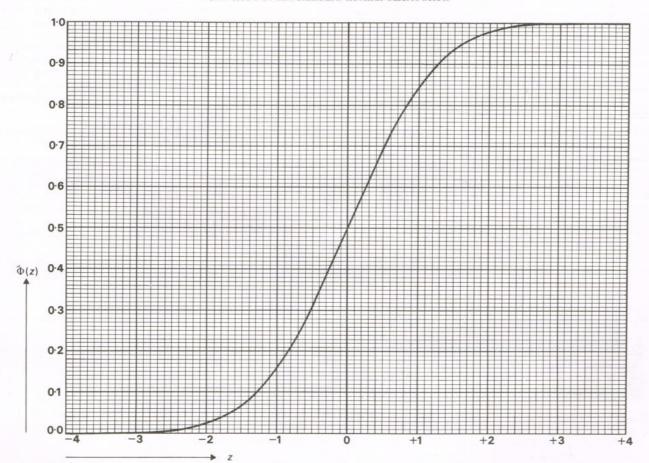
$\alpha_1$	5%	21/2%	1%	1/2%
$\alpha_2$	10%	5%	2%	1%
n	-			
1	-	-	-	-
2	-	-	-	-
3	0.3666	0.3758	0.3812	0.3830
4	0.3453	0.3753	0.4007	0.4131
5	0.3189	0.3431	0.3755	0.3970
6	0.2972	0.3234	0.3523	0.3708
7	0.2802	0.3043	0.3321	0.3509
8	0.2652	0.2880	0.3150	0.3332
9	0.2523	0.2741	0.2999	0.3174
10	0.2411	0.2619	0.2869	0.3037
11	0.2312	0.2514	0.2754	0.2916
12	0.2225	0.2420	0.2651	0.2810
13	0.2148	0.2336	0.2559	0.2714
14	0.2077	0.2261	0.2476	0.2627
15	0.2013	0.2192	0.2401	0.2549
16	0.1954	0.2129	0.2332	0.2476
17	0.1901	0.2071	0.2270	0.2410
18	0.1852	0.2017	0.2212	0.2349
19	0.1807	0.1968	0.2158	0.2292
20	0.1765	0.1921	0.2107	0.2238

$\alpha_1$	5%	21/2%	1%	1/2%
$\alpha_2$	10%	5%	2%	1%
п				
21	0.1725	0.1878	0.2060	0.2188
22	0.1688	0.1838	0.2015	0.2141
23	0.1653	0.1800	0.1974	0.2097
24	0.1620	0.1764	0.1936	0.2056
25	0.1589	0.1730	0.1899	0.2018
26	0.1560	0.1699	0.1865	0.1981
27	0.1533	0.1670	0.1833	0.1947
28	0.1507	0.1642	0.1802	0.1915
29	0.1483	0.1615	0.1773	0.1884
30	0.1460	0.1589	0.1746	0.1855
31	0.1437	0.1565	0.1719	0.1827
32	0.1416	0.1542	0.1693	0.1800
33	0.1395	0.1519	0.1669	0.1774
34	0.1375	0.1498	0.1645	0.1749
35	0.1356	0.1478	0.1622	0.1725
36	0.1338	0.1458	0.1601	0.1702
37	0.1321	0.1439	0.1580	0.1680
38	0.1304	0.1421	0.1560	0.1659
39	0.1288	0.1403	0.1540	0.1638
40	0.1272	0.1386	0.1522	0.1618

$\alpha_1$	5%	21/2%	1%	1/2%
« α <sub>2</sub>	10%	5%	2%	1%
n				
41	0.1257	0.1370	0.1504	0.1599
42	0.1243	0.1354	0.1487	0.1581
43	0.1229	0.1339	0.1470	0.1563
44	0.1216	0.1325	0.1454	0.1546
45	0.1203	0.1311	0.1438	0.1530
46	0.1190	0.1297	0.1423	0.1514
47	0.1178	0.1284	0.1409	0.1498
48	0.1166	0.1271	0.1394	0.1483
49	0.1155	0.1258	0.1380	0.1468
50	0.1144	0.1246	0.1367	0.1454
55	0.1092	0.1190	0.1306	0.1389
60	0.1048	0.1142	0.1253	0.1332
65	0.1008	0.1098	0.1205	0.1281
70	0.0972	0.1060	0.1163	0.1236
75	0.0940	0.1025	0.1125	0.1195
80	0.0911	0.0993	0.1090	0.1158
85	0.0885	0.0964	0.1059	0.1125
90	0.0861	0.0938	0.1030	0.1094
95	0.0838	0.0913	0.1003	0.1065
100	0.0817	0.0890	0.0978	0.1039

For description see page 26; for larger sample sizes, see page 35.

The c.d.f. of the standard normal distribution



#### Nonparametric tests

Pages 29-34 give critical values for six nonparametric tests. The sign test and the Wilcoxon signed-rank test are one-sample tests and can also be applied to matched-pairs data, the Mann-Whitney and Kolmogorov-Smirnov tests are two-sample tests, and the Kruskal-Wallis and Friedman tests are nonparametric alternatives to the standard one-way and two-way analyses-of-variance. Critical values for larger sample sizes than those included in these tables are covered on page 35.

The sign test (page 29). Suppose that the national average mark in an English examination is 60%. (In nonparametric work, the average is usually taken to be the median rather than the mean.) Test whether the following marks, obtained by twelve students from a particular school, are consistent with this average.

70	65	75	58	56	60	80	75	71	69	58	75	
+	+	+	-	-	0	+	+	+	+	-	+	

We have printed + or - under each mark to indicate whether it is greater or less than the hypothesised 60. There is one mark of exactly 60 which is completely ignored for the purposes of the test, reducing the sample size n to 11. The sign test statistic S is the number of + signs or the number of - signs, whichever is smaller; here S=3. Critical regions are of the form  $S \le tabulated\ value$ . As the  $\alpha_2=10\%$  critical region for n=11 is  $S \le 2$ , we cannot reject the null hypothesis  $H_0$  that these marks are consistent with an average of 60%.

For a one-sided test, count either the number of + or - signs, whichever the alternative hypothesis  $H_1$  suggests should be the smaller. For example if  $H_1$  says that the average mark is less than 60%, S would be defined as the number of + signs since if  $H_1$  is true there will generally be fewer marks exceeding 60%. Critical regions are of the same form as previously, but the  $\alpha_1$  significance levels should be used.

The Wilcoxon signed-rank test (page 29). This test is more powerful than the sign test as it takes into account the sizes of the differences from the hypothesised average, rather than just their signs. In the above example, first subtract 60 from each mark, and then rank the resulting differences, irrespective of their signs. Again ignore the mark of exactly 60, and also average the ranks of tied observations.

differences	+ 10	+ 5	+ 15	-2	-4	(0)	+ 20	+ 15	+ 11	+ 9	-2	+ 15
ranks	6	4	9	11/2	3		11	9	7	5	11/2	9

The Wilcoxon statistic T is the sum of the ranks of either the +ve or -ve differences, whichever is smaller. Here  $T=1\frac{1}{2}+3+1\frac{1}{2}=6$ . Critical regions are of the form  $T \le tabulated\ value$ , and the test thus shows evidence at better than the  $\alpha_2=2\%$  significance level that these marks are inconsistent with the national average, since the 2% critical region for n=11 is  $T \le 7$ .

For a one-sided test, let T be the sum of the ranks of either the + ve or the - ve differences, whichever the one-sided  $H_1$  suggests should be the smaller - it will be the same choice as in the sign test - and use the  $\alpha_1$  significance levels.

Matched-pairs data. Matched-pairs data arise in such examples as the following. One member of each of eight pairs of identical twins is taught mathematics by programmed learning, the other by a standard teaching method. Do the test results imply any difference in the effectiveness of the two teaching methods?

twins	a	Ь	С	d	е	f	g	h
programmed learning	70	80	62	50	70	30	49	60
standard method	75	82	65	58	68	41	55	67
differences	+5	+2	+3	+8	-2	+11	+6	+7

Such data may be analysed by either of the above tests, comparing the twin-by-twin differences in the final row with a hypothesised average of 0. The reader may confirm that S=1 and  $T=1\frac{1}{2}$ , so that the null hypothesis of no difference is rejected at the  $\alpha_2=10\%$  level in the sign test and at near to the  $\alpha_2=2\%$  level in Wilcoxon's test.

The Mann-Whitney U test (page 30). Six students from another school take the same English examination as mentioned above. Their marks are: 53, 65, 63, 57, 68 and 56. We want to check whether the two sets of students are of different average standards.

We order the two samples of marks together and indicate by A or B whether a mark comes from the first or second school:

	53	56	56	57	58	58	60	63	65	65 <i>B</i>	68	69	70	71	75	75	75	80
	В	A	В	В	A	A	A	В	A	В	В	A	A	A	A	A	A	A
ranks	1	$2\frac{1}{2}$	21/2	4	5	6	7	8	91	91	11	12	13	14	15	16	17	18

The observations are given ranks as shown, the ranks being averaged in the case of ties (unnecessary if a tie only involves members of one sample). Then either form the sum  $R_A$  of the ranks of observations from sample A, and calculate  $U_A = R_A - \frac{1}{2}n_A(n_A+1)$ , or the sum  $R_B$  of the ranks of observations from sample B, and calculate  $U_B = R_B - \frac{1}{2}n_B(n_B+1)$ , where  $n_A$  and  $n_B$  are the sizes of samples A and B. Finally obtain U as the smaller of  $U_A$  or  $n_An_B - U_A$ , or equivalently the smaller of  $U_B$  or  $n_An_B - U_B$ . Critical regions have the form  $U \le tabulated$  value. In the above example,  $R_A = 135$  so that  $U_A = 135 - \frac{1}{2}(12)(13) = 57$ , or  $R_B = 36$  and  $U_B = 36 - \frac{1}{2}(6)(7) = 15$ . In either case U is found to be 15, and this provides a little evidence for a difference between the two sets of students since the  $\alpha_2 = 10\%$  critical region is  $U \le 17$  and the 5% region is  $U \le 14$ . (In the table, sample sizes are denoted by  $n_1$  and  $n_2$  with  $n_1 \le n_2$ .)

For a one-sided test, calculate whichever of  $U_A$  and  $U_B$  is more likely to be small if the one-sided  $H_1$  is true, use this in place of U, and refer to the  $\alpha_1$  significance levels.

The Kolmogorov-Smirnov two-sample test (page 31). Whereas the Mann-Whitney test is designed specifically to detect differences in average, the Kolmogorov-Smirnov test is used when other types of difference may also be of interest. To calculate the test statistic D, draw the sample c.d.f.s (see page 26) for both sample A and sample B on the same graph; D is then the maximum vertical distance between these two c.d.f.s. To use the table on page 31, form  $D^* = n_A n_B D$ , and critical regions are of the form  $D^* \ge tabulated value$ , using the  $\alpha_2$  significance levels. A one-sided version of the test is also available, but is not often used since the alternative hypothesis is then essentially concerned not with general differences but a difference in average, for which the Mann-Whitney test is more powerful. Applied to the above example on the two sets of English results, D = 7/12 and  $D^* = 12 \times 12$  $6 \times 7/12 = 42$ . This is not even significant at the  $\alpha_2 = 10\%$  level, as that critical region is  $D^* \ge 48$ . This supports the above remark that the Mann-Whitney test (which gave significance at better than the 10% level) is more powerful as a test for differences in average.

The Kruskal-Wallis test (pages 32-34). The Kruskal-Wallis test is also designed to detect differences in average, but now when we have three or more samples to compare. Again, as in the Mann-Whitney test, we rank all of the data together (averaging the ranks of tied observations) and form the sum of the ranks in each sample. The test statistic is

$$H = \frac{12}{N(N+1)} \sum_{i=1}^{k} \frac{R_i^2}{n_i} - 3(N+1)$$

where k is the number of samples,  $n_1, n_2, \ldots, n_k$  are their sizes,  $N = \sum n_i$  and  $R_1, R_2, \ldots, R_k$  are the rank sums. Critical regions are of the form  $H \geqslant tabulated\ value$ . Tables are given on page 32 for k=3 and  $N \leqslant 19$ , on page 33 for k=4 ( $N \leqslant 14$ ), k=5 ( $N \leqslant 13$ ) and k=6 ( $N \leqslant 13$ ), and on page 34 for  $3 \leqslant k \leqslant 6$  and equal sample sizes  $n_1 = n_2 = \ldots = n_k = n$  for  $2 \leqslant n \leqslant 25$ .

To illustrate the Kruskal-Wallis test, we show samples of mileages per gallon for three different engine designs:

design		mileage	per gallor		32	rai	nks		rank sums
8	19.8	20.5	20.8	19.7	4	6	71/2	21/2	20
b	21.7	20.8	21.2		10	$7\frac{1}{2}$	9		26½
c	19.7	19.4	19.9		21/2	1	5		81

Then
$$H = \frac{12}{10 \times 11} \left( \frac{20^2}{4} + \frac{(26\frac{1}{2})^2}{3} + \frac{(8\frac{1}{2})^2}{3} \right) - 3 \times 11$$

$$= 0.1091 \times (358.167) - 33 = 6.073.$$

This is significant of a difference between average mileages at better than the 5% level, the  $\alpha = 5\%$  critical region being  $H \ge 5.791$ . (In such cases where there is no meaningful one-sided version of the test,  $\alpha_2$  is written as  $\alpha$  with no subscript.)

Friedman's test (page 34). Friedman's test applies when the observations in three or more samples are related or 'blocked' (similarly as with matched-pairs data). If there are k samples and n blocks, the observations in each block are ranked from 1 to k, the rank sums  $R_1, R_2, \ldots, R_k$  for each sample obtained, and Friedman's test statistic is then

$$M = \frac{12}{nk(k+1)} \sum_{i=1}^{k} R_i^2 - 3n(k+1)$$

To illustrate the test, suppose that in a mileages survey we use cars of five different ages and obtain the following data:

			age of ca	ar		1	1867-L		100		
design	1	2	3	4	5			ranks			rank sums
a	21.3	21.6	21,2	20.7	20.1	2	2	21/2	2	2	101
b	21.6	21.7	21.2	20.9	20.6	3	3	21/2	3	3	141
c	20.0	20.1	19.9	19.5	19.0	1	1	1	1	1	5

Then  $M = 12/(15 \times 4) \{(10\frac{1}{2})^2 + (14\frac{1}{2})^2 + 5^2\} - (15 \times 4) = 0.2 \times 345.5 - 60 = 9.1$ , which is strongly significant since the  $\alpha = 1\%$  critical region is  $M \ge 8.400$ .

Note: All of the nonparametric tests described above have discrete-valued statistics, so that the exact nominal  $\alpha$ -levels are not usually obtainable. The tables give best conservative critical regions, i.e. the largest regions with significance levels less than or equal to  $\alpha$ .

## Critical values for the sign test

$\alpha_{i}$	5%	21/2%	1%	1/2%	$\alpha_1$	5%	21/2%	1%	1/2%	$\alpha_1$	5%	2½%	1%	1/2%	$\alpha_1$	5%	21/2%	1%	1/2%
$\alpha_2$	10%	5%	2%	1%	$\alpha_2$	10%	5%	2%	1%	$\alpha_2$	10%	5%	2%	1%	$\alpha_2$	10%	5%	2%	1%
n					n	2				n					n				
1	-	-	-	-	26	8	7	6	6	51	19	18	16	15	76	30	28	27	26
2	-	-	-	-	27	8	7	7	6	52	19	18	17	16	77	30	29	27	26
3	-	-	-	-	28	9	8	7	6	53	20	18	17	16	78	31	29	28	27
4	-	-	-	-	29	9	8	7	7	54	20	19	18	17	79	31	30	28	27
5	0	_	_	-	30	10	9	8	7	55	20	19	18	17	80	32	30	29	28
6	0	0	-	-	31	10	9	8	7	56	21	20	18	17	81	32	31	29	28
7	0	0	0	-	32	10	9	8	8	57	21	20	19	18	82	33	31	30	28
8	1	0	0	0	33	11	10	9	8	58	22	21	19	18	83	33	32	30	29
9	1	1	0	0	34	11	10	9	9	59	22	21	20	19	84	33	32	30	29
10	1	1	0	0	35	12	11	10	9	60	23	21	20	19	85	34	32	31	30
11	2	1	1	0	36	12	11	10	9	61	23	22	20	20	86	34	33	31	30
12	2	2	1	1	37	13	12	10	10	62	24	22	21	20	87	35	33	32	31
13	3	2	1	1	38	13	12	11	10	63	24	23	21	20	88	35	34	32	31
14	3	2	2	1	39	13	12	11	11	64	24	23	22	21	89	36	34	33	31
15	3	3	2	2	40	14	13	12	11	65	25	24	22	21	90	36	35	33	32
16	4	3	2	2	41	14	13	12	11	66	25	24	23	22	91	37	35	33	32
17	4	4	3	2	42	15	14	13	12	67	26	25	23	22	92	37	36	34	33
18	5	4	3	3	43	15	14	13	12	68	26	25	23	22	93	38	36	34	33
19	5	4	4	3	44	16	15	13	13	69	27	25	24	23	94	38	37	35	34
20	5	5	4	3	45	16	15	14	13	70	27	26	24	23	95	38	37	35	34
21	6	5	4	4	46	16	15	14	13	71	28	26	25	24	96	39	37	36	34
22	6	5	5	4	47	17	16	15	14	72	28	27	25	24	97	39	38	36	35
23	7	6	5	4	48	17	16	15	14	73	28	27	26	25	98	40	38	37	35
24	7	6	5	5	49	18	17	15	15	74	29	28	26	25	99	40	39	37	36
25	7	7	6	5	50	18	17	16	15	75	29	28	26	25	100	41	39	37	36

For description, see page 28; for larger sample sizes, see page 35.

## Critical values for the Wilcoxon signed-rank test

$\alpha_1$	5%	21/2%	1%	1/2%
$\alpha_2$	10%	5%	2%	1%
n				
1	-	-	-	-
2	-	-	_	-
3	_	-	-	-
4	-	-	-	-
5	. 0	-	-	-
6	2	0	_	-
7	3	2	0	_
8	5	3	1	0
9	8	5	3	1
10	10	8	5	3
11	13	10	7	5
12	17	13	9	7
13	21	17	12	9
14	25	21	15	12
15	30	25	19	15
16	35	29	23	19
17	41	34	27	23
18	47	40	32	27
19	53	46	37	32
20	60	52	43	37
21	67	58	49	42
22	75	65	55	48
23	83	73	62	54
24	91	81	69	61
25	100	89	76	68

$\alpha_1$	5%	21/2%	1%	1/2%
$\alpha_2$	10%	5%	2%	1%
n				
26	110	98	84	75
27	119	107	92	83
28	130	116	101	91
29	140	126	110	100
30	151	137	120	109
31	163	147	130	118
32	175	159	140	128
33	187	170	151	138
34	200	182	162	148
35	213	195	173	159
36	227	208	185	171
37	241	221	198	182
38	256	235	211	194
39	271	249	224	207
40	286	264	238	220
41	302	279	252	233
42	319	294	266	247
43	336	310	281	261
44	353	327	296	276
45	371	343	312	291
46	389	361	328	307
47	407	378	345	322
48	426	396	362	339
49	446	415	379	355
50	466	434	397	373

$\alpha_1$	5%	21/2%	1%	1/2%
α2	10%	5%	2%	1%
п				
51	486	453	416	390
52	507	473	434	408
53	529	494	454	427
54	550	514	473	445
55	573	536	493	465
56	595	557	514	484
57	618	579	535	504
58	642	602	556	525
59	666	625	578	546
60	690	648	600	567
61	715	672	623	589
62	741	697	646	611
63	767	721	669	634
64	793	747	693	657
65	820	772	718	681
66	847	798	742	705
67	875	825	768	729
68	903	852	793	754
69	931	879	819	779
70	960	907	846	805
71	990	936	873	831
72	1020	964	901	858
73	1050	994	928	884
74	1081	1023	957	912
75	1112	1053	986	940

$\alpha_1$	5%	21/2%	1%	1/2%
$\alpha_2$	10%	5%	2%	1%
n				
76	1144	1084	1015	968
77	1176	1115	1044	997
78	1209	1147	1075	1026
79	1242	1179	1105	1056
80	1276	1211	1136	1086
81	1310	1244	1168	1116
82	1345	1277	1200	1147
83	1380	1311	1232	1178
84	1415	1345	1265	1210
85	1451	1380	1298	1242
86	1487	1415	1332	1275
87	1524	1451	1366	1308
88	1561	1487	1400	1342
89	1599	1523	1435	1376
90	1638	1560	1471	1410
91	1676	1597	1507	1445
92	1715	1635	1543	1480
93	1755	1674	1580	1516
94	1795	1712	1617	1552
95	1836	1752	1655	1589
96	1877	1791	1693	1626
97	1918	1832	1731	1664
98	1960	1872	1770	1702
99	2003	1913	1810	1740
100	2045	1955	1850	1779

## Critical values for the Mann-Whitney U test

$\alpha_1$ $\alpha_2$	5% 2½% 1% ½% 10% 5% 2% 1%	$\alpha_1$ $\alpha_2$	5% 2½% 1% ½% 10% 5% 2% 1%	$\alpha_1$ $\alpha_2$	The second second	1% ½% 2% 1%		$\alpha_1$ $\alpha_2$	<b>5%</b> :	2½% 1% 5% 2%	½% 1%		$\alpha_1$ $\alpha_2$	<b>5%</b>	21/2%	1%	½% 1%
	10% 0% 2% 1%		10.4	100000			$n_1$	n <sub>2</sub>				n <sub>1</sub>	n <sub>2</sub>				
n <sub>1</sub> n <sub>2</sub>		$n_1$ $n_2$							04	70 04			23	143	132	118	109
2 2		5 5		8 16 8 17		26 22 28 24	12	21	81 85	73 64 77 67	58 61	18	24	150	138	124	115
2 3		5 6	5 3 2 1	8 18		30 26	12	23	90	81 71	64	18	25	157		130	121
2 4 2 5	0	5 8		8 19		32 28	12	24	94	85 75	68			_			
2 6	0	5 9		8 20	47 41	34 30	12	25	98	89 78	71	19	19	123	113	101	93
2 7	0	5 10	11 8 6 4	8 21	49 43	36 32						19	20	130		107	99
2 8	1 0	5 11		8 22	N BOOK TABLE	38 34	13	13	51	45 39	34	19	21	138	126	113	105
2 9	1 0	5 12		8 23		40 35	13	14	56	50 43 54 47	38 42	19	22	145 152	133	120 126	111
2 10	1 0	5 13		8 24 8 25		42 37 45 39	13	15	61 65	54 47 59 51	45	19	24	160	147	133	123
2 11 2 12	2 1	5 15		0 20	00 55	40 00	13	17	70	63 55	49	19	25	167	154	139	129
2 13	2 1 0 -	5 16		9 9	21 17	14 11	13	18	75	67 59	53			_			
2 14	3 1 0 -	5 17	20 17 13 10	9 10	24 20	16 13	13	19	80	72 63	57	20	20	138	127	114	105
2 15	3 1 0 -	5 18	22 18 14 11	9 11	27 23	18 16	13	20	84	76 67	60	20	21	146	134	121	112
2 16	3 1 0 -	5 19		9 12	2.00	21 18	13	21	89	80 71	64	20	22	154	141	127	118
2 17	3 2 0 -	5 20		9 13		23 20 26 22	13	22	94 98	85 75 89 79	68 72	20	23	161 169	149 156	134	125 131
2 18	4 2 0 -	5 21		9 14 9 15		28 24	13	24	103	94 83	75	20	25	177	163	148	138
2 19	4 2 1 0	5 23		9 16	1007	31 27	13	25	108	98 87	79				3550		
2 21	5 3 1 0	5 24		9 17		33 29						21	21	154	142	128	118
2 22	5 3 1 0	5 25	32 27 21 17	9 18	48 42	36 31	14	14	61	55 47	42	21	22	162	150	135	125
2 23	5 3 1 0			9 19		38 33	14	15	66	59 51	46	21	23	170	157	142	132
2 24	6 3 1 0	6 6		9 20		40 36	14	16	71	64 56	50	21	24	179 187	165 173	150 157	139
2 25	6 3 1 0	6 8		9 21 9 22		43 38 45 40	14	17	77 82	69 60 74 65	54 58	21	20	107	1/3	107	140
3 3	0	6 9		9 23		48 43	14	19	87	78 69	63	22	22	171	158	143	133
3 4	0	6 10		9 24		50 45	14	20	92	83 73	67	22	23	179	166	150	140
3 5	1 0	6 11	16 13 9 7	9 25	69 62	53 47	14	21	97	88 78	71	22	24	188	174	158	147
3 6	2 1	6 12	2 17 14 11 9				14	22	102	93 82	75	22	25	197	182	166	155
3 7	2 1 0 -	6 13		10 10	27 23	19 16	14	23	107	98 87	79			100	475	150	140
3 8	3 2 0 -	6 14		10 11	31 26	22 18	14	24		102 91 107 95	83 87	23	23	189 198	175 183	158 167	148
3 9	4 2 1 0	6 16		10 12	34 29 37 33	24 21 27 24	14	25	118	107 95	07	23	25	207	192	175	163
3 10	5 3 1 0	6 17		10 14	41 36	30 26	15	15	72	64 56	51			1.57.7.0	100	57756	-///
3 12	5 4 2 1	6 18		10 15	44 39	33 29	15	16	77	70 61	55	24	24	207	192	175	164
3 13	6 4 2 1	6 19	30 25 20 17	10 16	48 42	36 31	15	17	83	75 66	60	24	25	217	201	184	172
3 14	7 5 2 1	6 20		10 17	51 45	38 34	15	18	88	80 70	64					400	400
3 15	7 5 3 2	6 21		10 18	55 48	41 37	15	19	94	85 75	69	25	25	227	211	192	180
3 16	8 6 3 2	6 22		10 19	58 52 62 55	44 39 47 42	15	20	100	90 80 96 85	73 78			-			
3 17 3 18	9 6 4 2	6 23		10 20	62 55 65 58	50 44	15	22		101 90	82	26	26	247	230	211	198
3 19	10 7 4 3	6 25		10 22	68 61	53 47	15	23		106 94	87	27	27	268	250	230	216
3 20	11 8 5 3			10 23	72 64	55 50	15	24	122	111 99	91	28	28	291	272	250	235
3 21	11 8 5 3	7 7	7 11 8 6 4	10 24	75 67	58 52	15	25	128	117 104	96	29	29	314	294	271	255
3 22	12 9 6 4	7 8	13 10 7 6	10 25	79 71	61 55						30	30	338	317	293	276
3 23	13 9 6 4	7 9		** **	24 20	25 24	16	16	83	75 66 91 71	60 65						
3 24	13 10 6 4	7 10		11 11	34 30 38 33	25 21 28 24	16	17	89 95	81 71 86 76	70	31	31	363	341	315	298
3 25	14 10 7 5	7 11		11 12	42 37	31 27	16	19	101	92 82	74	32	32	388	365	339	321
4 4	1 0	7 13		11 14	46 40	34 30	16	20	107	98 87	79	33	33	415	391	363	344
4 5	2 1 0 -	7 14		11 15	50 44	37 33	16	21		103 92	84	34	34	443	418	388	369
4 6	3 2 1 0	7 15	5 28 24 19 16	11 16	54 47	41 36	16	22		109 97	89	35	35	471	445	414	394
4 7	4 3 1 0	7 16		11 17	57 51	44 39	16	23	VA153151 3	115 102		20	20	E01	473	441	420
4 8	5 4 2 1	7 17		11 18	61 55	47 42	16	24	131 137	120 108 126 113	99	36	36	501 531	503	469	447
4 9	6 4 3 1 7 5 3 2	7 18		11 19 11 20	65 58 69 62	50 45 53 48	10	20	137	.20 113	104	38	38	563	533	498	475
4 10	7 5 3 2 8 6 4 2	7 20		11 21	73 65	57 51	17	17	96	87 77	70	39	39	595	564	528	504
4 12	9 7 5 3	7 2		11 22	77 69	60 54	17	18	102	93 82		40	40	628	596	558	533
4 13	10 8 5 3	7 2		11 23	81 73	63 57	17	19	109	99 88	81			-			
4 14	11 9 6 4	7 2		11 24	85 76	66 60	17	20		105 93				000	600	EOO	FO
4 15	12 10 7 5	7 2		11 25	89 80	70 63	17	21	300000	111 99 117 105	91 96	41	41	662 697	628 662	590 622	564 598
4 16	14 11 7 5	7 2	5 50 44 36 32	12 12	42 37	31 27	17	22	2000	117 105 123 110		42	42	733	697	655	627
4 17 4 18	15 11 8 6 16 12 9 6	8 1	8 15 13 9 7	12 12	47 41	35 31	17	24	141			44	44	770	732	689	660
4 18	17 13 9 7	100000	9 18 15 11 9	12 14	51 45	38 34	17		100000	135 122	5 0 70 15 1	45	45	808	769	724	694
4 20	18 14 10 8	8 1		12 15	55 49	42 37									32.02	1200	5,872
4 21	19 15 11 8	8 1		12 16	60 53	46 41	18	18	109	99 88	81	46	46	846	806	760	729
4 22	20 16 11 9	8 1:		12 17	64 57	49 44	18	19		106 94	87	47	47	886	845	797	765
4 23	21 17 12 9	8 1:		12 18	68 61	53 47	18	20	3200	112 100	92	48	48	926	884 924	835 873	802
4 24	22 17 13 10	8 14		12 19 12 20	72 65 77 69	56 51 60 54	18	21	130 136	119 106 125 112	98 104	49 50	49	968	965	913	
4 25	23 18 13 10		m 22 70 70 70		1/ DM	UU 24		11	130	120 112	104	UU	90	1010	000	010	

## Critical values for the Kolmogorov - Smirnov two-sample test

	$\alpha_1$	5%	21/2%	1%	1/2%		$\alpha_1$	5%	21/2%	1%	1/2%		$\alpha_1$	5%	21/2%	1%	1/2%		$\alpha_1$	5%	21/2%	1%	1/2%	$\alpha_1$	5%	2½%	1%	1/2%
	α2	10%	5%	2%	1%		$\alpha_2$	10%	5%	2%	1%	_	$\alpha_2$	10%	5%	2%	1%	١.	$\alpha_2$	10%	5%	2%	1%	$\alpha_2$	10%	5%	2%	1%
	n <sub>1</sub> n <sub>2</sub>					n <sub>1</sub>			0.5	0.5		1000	n <sub>2</sub>	70		-00	-00	П	$n_1$ $n_2$			400		$n_1  n_2$	450	470	400	204
	2 2 2 3	-	_	_	_	5	5	20	25 24	25 30	25 30	1 8	3 16	72 68	80 77	88 85	88	Н	12 21	108	120	132 138	141	18 23 18 24	152 162	170 180	189 198	204
	2 4	-	-	-	-	5	7	25	28	30	35		3 18	72	80	88	94	Н	12 23		125	138	149	18 25	162	180	202	216
	2 5 2 6	10	_	_	_	5	8	30	30 35	35 36	35 40	1000	3 19	74	82 88	93	98	Н	12 24 12 25	132	144	156 153	168	19 19	152	171	190	190
	2 7	14	-	-	-	5	10	35	40	40	45	100	3 21	81	89	102	107	Н	12 20	120	,,,,	100		19 20	144	160	171	187
	2 8 2 9	16	16 18	_	-	5	11	35 36	39 43	44 48	45 50	1000	22	84 89	94 98	106 107	112 115	П	13 13 13 14	91 78	91 89	104 102	117	19 21 19 22	147 152	163 169	184 190	199 204
	2 10	18	20	-	-	5	13	40	45	50	52	1000	24	96	104	120	128	П	13 15	87	96	107	115	19 23	159	177	197	209
- 1	2 11	20	22	-	-	5	14	42	46	51	56	8	25	95	104	118	125	П	13 16	91	101	112	121	19 24	164	183	204	218
	2 12 2 13	22 24	24 26	26	-	5	15	50 48	55 54	60 59	60 64	5	9	54	54	63	63	П	13 17 13 18	96 99	105	118 123	127	19 25	168	187	211	224
	2 14	24	26	28	-	5	17	50	55	63	68	1000	10	50	53	61	63		13 19	104	114	130	138	20 20	160	180	200	220
-	2 15 2 16	26	28	30	_	5	18	52 56	60	65 70	70 71	9		52	59 63	63 69	70 75		13 20 13 21	108	120 126	135 140	143	20 21	154 160	173 176	193 196	199
	2 17	30	32	34	-	5	20	60	65	75	80	5	13	59	65	73	78	1 8	13 22	117		143	156	20 23	164	184	205	219
-	2 18 2 19	32	34 36	36 38	38	5	21	60 63	69 70	75 78	80	9	14	63 69	70 75	80	90		13 23		135 140	152 155	161	20 24 20 25	172 180	192 200	212 220	228
	2 20	34	38	40	40	5	23	65	72	82	87	1000	16	69	78	87	94	- 10	13 24 13 25			160	166 172	20 25	100	200	220	233
	2 21 2 22	36 38	38	42 44	42	1100	24 25	67 75	76 80	85	90	1000	17	74	82	92	99		10 14	00	110	110	120	21 21	168	189	210	231
	2 22	38	40 42	44	46	5	20	75	80	90	95	9	18	81	90	99	108	- 1	14 14 14 15	98 92	112 98	112	126	21 22 21 23	163 171	183 189	205 213	223
1	2 24	40	44	46	48	6	6	30	30	36	36	9		84	93	104	111	- 81	14 16	96	106	120	126	21 24	177	198	222	237
-	2 25	42	46	48	50	6	7 8	28 30	30	35 40	36 40	1000	21	90	99	111	117	- 80	14 17 14 18	100 104	111	125 130	134	21 25	182	202	225	244
1	3 3	9	-	-	-	6	9	33	39	42	45	1000	23	94	106	117	126	- 65	14 19		121	135	148	22 22	198	198	242	242
-	3 4 3 5	12 15	- 15	_	_	6	10	36 38	40 43	44	48 54	1000	24	99	111	123	132 135	- 81	14 20 14 21	114	126	142 154	152 161	22 23 22 24	173	194	217 228	237
1	3 6	15	18	_	_	1000	12	48	48	54	60	-	25	101	114	125	135	- 88	14 22	126 124	140 138	152	164	22 25	182 189	204	234	250
-	3 7	18	21	21	-	1000	13	46	52	54	60	1000	10	60	70	70	80	- 81	14 23		142	159	170					
-	3 8 3 9	21	21	24	27	6	14	48 51	54 57	60 63	64	10		57 60	60 66	69 74	77 80	- 81	14 24 14 25		146 150	164 169	176	23 23 24	207 183	230	253 228	253 249
1	3 10	24	27	30	30	6	16	54	60	66	72	10		64	70	78	84							23 25	195	216	243	262
-	3 11 3 12	27	30	33	33	1000	17	56 66	62 72	68 78	73 84	10		68 75	74 80	90	90	- 40	15 15 15 16		120 114	135 120	135	24 24	216	240	264	288
-	3 13	30	33	36	39	00000	19	64	70	77	83	10		76	84	94	100	- 10	15 17		116	131	142	24 25	204	225	254	262
	3 14 3 15	33	36	39	42	100000	20	66	72	80	88	10		79	89	99	106	- 81	15 18		123	138	147	05 05	205	050	075	200
	3 15 3 16	33 36	36 39	42 45	42 45	1000	21	69 70	75 78	84 88	90	10		82 85	92 94	104	108	- 88	15 19 15 20		127 135	142 150	152	25 25	225	250	275	300
-	3 17	36	42	45	48	10000	23	73	80	91	97	10		100	110	120	130	- 10	15 21		138	156	168					
1	3 18	39 42	45 45	48 51	51	777000	24	78 78	90	96 96	102	0.955	21	95 98	105	118 120	126	- 18	15 22 15 23	130	144	160 165	173	26 26 27 27	234	260 270	286 324	312
1	3 20	42	48	54	57				252			10		101	114	127	137	- 69	15 24	141	156	174	186	28 28	280	308	336	364
1	3 21 3 22	45 48	51 51	54 57	57 60	7	7 8	35 34	42 40	42 42	42 48	17.53	24 25	106	118 125	130	140 150		15 25	145	160	180	195	29 29 30 30	290 300	319 330	348	377 390
1	3 23	48	54	60	63	7	9	36	42	47	49				120	140	100	15	16 16	112	128	144	160	30 30	300	550	300	330
	3 24 3 25	51 54	57 60	63 66	66 69	100	10	40 44	46 48	50	53	1000	11	66	77	88	88	- 80	16 17		124	139	143	24 24	210	244	272	400
1	3 23	54	00	00	08	1000	12	46	53	55 58	59 60	12323	13	64	72 75	77 86	86 91	- 100	16 18 16 19	116 120		142 151	154 160	31 31 32 32	310	341 352	416	403
- 11	4 4	16	16	-	-	1000	13	50	56	63	65	1000	14	73	82	90	96	188	16 20		140	156	168	33 33	330	396	429	462
- 1	4 5 4 6	16 18	20	20	24	10.5355	14	56 56	63 62	70 70	77 75	119533	15 16	76 80	84 89	95	102	- 80	16 21 16 22		145 150	162 168	173	34 34 35 35	374 385	408 420	442 455	476 490
1	4 7	21	24	28	28	7	16	59	64	73	77	11	17	85	93	104	110	1	16 23	141	157	175	187				7255	
- 11	4 8 4 9	24	28 28	32	32	1000	17	61 65	68 72	77 83	84	10000	18 19	88 92	97	108	118	- 80	16 24 16 25	152 149		184 186	200 199	36 36 37 37	396 407		468 518	504 518
- 8	4 10	28	30	36	36	1200	19	69	76	86	91	100000	20	96	107		127		10 20	143	107	100	155	38 38	418	456	532	570
- 8	4 11	29	33	40	40	100	20	72	79	91	93	1000	21	1000	112		134	- 80	17 17	136		153	170	39 39	429	468	546	585
- 8	4 12 4 13	36 35	36 39	40 44	44 48	12053	21	77 77	91 84	98 97	105	1000	22	110	121	143	143	- 81	17 18 17 19		133 141	150 158	164	40 40	440	520	560	600
I	4 14	38	42	48	48	7	23	80	89	101	108	11	24	111	124	139	150		17 20	130	146	163	175					
- 8	4 15	40 44	44 48	48 52	52 56	3000	24	84 86			112	11	25	117	129	143	154	- 80	17 21 17 22			168 176	180 187	41 41 42 42	492 504		574 588	615 630
- 81	4 17	44	48	56	60			50	01	100	110	12	12	72	84	96	96	- 100	17 23			181	196	43 43	516	559	645	688
- 18	4 18	46	50	56	60	8	8	40	48	48	56	7000	13	71	81	92	95	- 80	17 24			187	203	44 44	528		660	704
- 81	4 19	49 52	53 60	57 64	64	8	9	40 44	46 48	54 56	55 60	1000	14	78 84	86 93	94 102	104		17 25	156	173	196	207	45 45	540	585	675	720
	4 21	52	59	64	72	8	11	48	53	61	64	12	16	88	96	108	116	- 80	18 18			180	180	46 46	552		690	736
- 81	4 22 4 23	56 57	62 64	66 69	72 76	122350	12	52 54	60 62	64 67	68 72	10000	17 18	90 96		112 120	119 126	- 100	18 19 18 20			160 170	176 182	47 47 48 48	564 576		705 720	752 768
- 81	4 24	60	68	76	80	100000	14	58	64	72	76	1000	19	99		121	130	- 100	18 21			177	189	49 49	637		735	833
	4 25	63	68	75	84	8	15	60	67	75	81	12	20	104	116	128	140		18 22	148	164	184	196	50 50	650		800	850

## Critical values for the Kruskal-Wallis test (small sample sizes)

$$H = \frac{12}{N(N+1)} \sum_{i=1}^{k} \frac{R_i^2}{n_i} - 3(N+1)$$

 $k = 3 \text{ samples } (N \leq 19)$ 

	amp size		α 10	% 5%	2%	1%
1	1	1	-	_	_	2
2	1	1				
2	2	1		_	_	_
2	2	2	4.57	1 -	_	_
3	1	1	4.00	-	-	_
3	2	1 2	4.28		_	_
3	3	1	4.57			-
3	3	2	4.55			_
3	3	3	4.62	2 5.600	6.489	7.200
4					7	
4	1 2	1	4.50	0 -	_	550
4	2	2	4.45		6.000	=
4	3	1	4.05			-
4	3	2	4.51	1 5.444	6.144	6.444
4	3	3	4.70		6.564	
4	4	1	4.16		6.667	
4	4	2	4.55 4.54		6.600	2000
4	4	4	4.65		6.962	
			-		5.002	,,004
5	1	1	-		-	-
5	2	1	4.20			-
5	2	2	4.37		6.000	A DESCRIPTION
5	3	2	4.65		6.124	
5	3	3	4.53		6.533	
5	4	1	3.98	7 4.985	6.431	6.955
5	4	2	4.54	1 5.273	6.505	7.205
5	4	3	4.54		6.676	
5	4	4	4.66		6.953	
5	5	1 2	4.10			
5	5	3	4.54			
5	5	4	4.52		7.000	7.823
5	5	5	4.56	0 5.780	7.220	8.000
6	1	1	-	-	-	-
6	2	1	4.20			-
6	2	2	4.54		6.182	6.655
6	3	1 2	3.90 4.68		6.236 6.227	6.873 6.970
6	3	3	4.59		6.590	7.410
6	4	1	4.03		6.174	7.106
6	4	2	4.49	4 5.340	6.571	7.340
6	4	3	4.60		6.725	7.500
6	4	4	4.59		6.900	7.795
6	5	1 2	4.12			7.182
6	5	3	4.59 4.53			7.376 7.590
6	5	4	4.52			7.936
6	5	5	4.54		7.110	8.028
6	6	1	4.00		6.286	7.121
6	6	2	4.43		6.667	7.467
6	6	3	4.55		6.900	7.725
6	6	5	4.54 4.54		7.107 7.152	8.000 8.124
6	6	6	4.64		7.152	8.222
-				20		
7	1 2	1	4.26		5.891	_
7		2	4.52		6.058	7.000
7 7 7	2	1	4.17		6.043	7.030
7	3		4.58	2 5.357	6.339	6.839
7 7		2	98,623,70		6.656	7.228
7 7 7 7 7	3 3	3	4.60			
7 7 7 7 7 7	3 3 4	3	4.60 4.12	1 4.986	6.319	6.986
7 7 7 7 7 7 7 7,	3 3 4 4	3 1 2	4.60 4.12 4.54	1 4.986 9 5.376	6.319 6.447	7.321
7 7 7 7 7 7 7 7 7	3 3 4 4 4	3 1 2 3	4.60 4.12 4.54 4.52	1 4.986 9 5.376 7 5.623	6.319 6.447 6.780	7.321 7.550
7 7 7 7 7 7 7 7,	3 3 4 4	3 1 2	4.60 4.12 4.54	1 4.986 9 5.376 7 5.623 2 5.650	6.319 6.447	7.321

		1	K :	O Juli	iples (/v	≈ 19)	
	sam		α	10%	5%	2%	1%
7	5	3		4.535	5.607	6.874	7.697
7	5	4		4.542	5.733		7.931
7	5	5		4.571	5.708		8.108
7	6	1 2		4.033 4.500	5.067		
7	6	3		4.550	5.357		7.490
7	6	4		4.562	5.706		8.039
7	6	5		4.560	5.770		8.157
7	6	6		4.530	5.730	7.197	8.257
7	7	1	1	3.986	4.986	6.300	7.157
7	7	2		4.491	5.398	6.693	7.491
7	7	3		4.613	5.688		7.810
7	7	4		4.563	5.766		8.142
7	7	5		4.546	5.746	7.247	8.257
8	1	1		4.418	-	-	-
8	2	1		4.011	4.909		-
8	2	2		4.587	5.356		6.663
8	3	1		4.010	4.881		6.804
8	3	2		4.451 4.543	5.316		7.022
8	4	1		4.038	5.617 5.044		6.973
8	4	2		4.500	5.393		7.350
8	4	3		4.529	5.623		7.585
8	4	4		4.561	5.779	7.075	7.853
8	5	1		3.967	4.869	6.257	7.110
8	5	2		4.466	5.415	6.571	7.440
8	5	3		4.514	5.614		7.706
8	5	4		4.549	5.718		7.992
8	5	5		4.555	5.769		8.116
8	6	2		4.015 4.463	5.015		7.256 7.522
8	6	3		4.575	5.678		7.796
8	6	4		4.563	5.743		8.045
8	6	5		4.550	5.750		8.226
8	7	1		4.045	5.041	6.366	7.308
8	7	2		4.451	5.403	6.619	7.571
8	7	3		4.556	5.698	7.021	7.827
8	7	4		4.548	5.759		8.118
8	8	1		4.044	5.039		7.314
8	8	2		4.509 4.555	5.408		7.654 7.889
					0.704	7,021	7.000
9 9	1 2	1	1 3	4.545 3.906	4.842	5.662	6.346
9	2	2		4.484	5.260		6.897
9	3	1		4.073	4.952		6.886
9	3	2		4.492	5.340	6.359	7.006
9	3	3		4.633	5.589	6.800	7.422
9	4	1		3.971	5.071		7.171
9	4	2		4.489	5.400		7.364
9	4	3		4.526 4.576	5.652		7.614
9	5	1		4.056	5.040		7.149
9	5	2		4.465	5.396		7.447
9	5	3		4.587	5.670		7.733
9	5	4		4.531	5.713	7.121	8.025
9	5	5	100	4.557	5.770		8.173
9	6	1		3.953	5.049		7.248
9	6	2		4.481	5.392		7.566
9	6	3		4.548 4.546	5.671		7.823 8.109
9	7	1		4.011	5.042		7.282
9	7	2		4.480	5.429		7.637
9	7	3	1	4.547	5.656		7.861
9	8	1	:	3.986	4.985	6.351	7.394
9	8	2		4.492	5.420		7.642
9	9	1	4	4.007	4.961	6.407	7.333
10	1	1	31	4.654	4.654	_	_
10	2	1	100	4.114	4.840		6.429
10	2	2		4.434 3.996	5.120		6.537 6.851
10	3	2		1.470	5.362	6.375	7.042
100	186	100		80087		700000	12000

5	amp		α	10%	5%	2%	1%
10	3	3		4.529	5.588	6.784	7.372
10	4	1		4.042	5.018	6.158	7.105
10	4	2		4.462	5.345	6.492	7.357
10	4	3		4.588	5.661	6.905	7.617
10	4	4		4.565	5.716	7.065	7.907
10	5	1		3.988	4.954	6.318	7.178
10	5	2		4.455	5.420	6.612	7.514
10	5	3		4.552	5.636	6.938	7.752
10	5	4		4.557	5.744	7.135	8.048
10	6	1		3.967	5.042	6.383	7.316
10	6	2		4.480	5.406	6.669	7.588
10	6	3		4.551	5.656	7.002	7.882
10	7	1		3.981	4.986	6.370	7.252
10	7	2		4.492	5.377	6.652	7.641
10	8	1		3.964	5.038	6.414	7.359
			$\vdash$	51500.00	ACCEPTANCE OF THE PARTY OF THE		
11	1	1		4.028	4.747	-	-
11	2	1		4.044	4.816	5.834	6.600
11	2	2		4.414	5.164	6.050	6.766
11	3	1		3.985	5.030	6.030	6.818
11	3	2		4.487	5.374	6.379	7.094
11	3	3	1	4.589	5.583	6.776	7.418
11	4	1		3.991	4.988	6.111	7.090
11	4	2		4.484	5.365	6.553	7.396
11	4	3		4.536	5.660	6.881	7.679
11	4	4		4.550	5.740	7.036	7.945
11	5	1		4.026	5.020	6.284	7.130
11	5	2		4.490	5.374	6.648	7.507
11	. 5	3		4.550	5.646	6.962	7.807
11	6	1		4.029	5.062	6.304	7.261
11	6	2		4.463	5.408	6.693	7.564
11	7	1		4.045	4.985	6.409	7.330
			_				
12	1	1		4.148	4.829	_	-
12	2	1		4.092	4.875	5.550	6.229
12	2	2		4.379	5.173	5.967	6.761
12	3	1		3.930	4.930	6.018	6.812
12	3	2		4.477	5.350	6.412	7.134
12	3	3		4.579	5.576	6.746	7.471
12	4	1		4.003	4.931	6.225	7.108
12	4	2		4.500	5.442	6.547	7.389
12	4	3		4.524	5.661	6.903	7.703
12	5	1		3.985	4.977	6.326	7.215
12	5	2		4.486	5.395	6.649	7.512
12	6	1		4.050	5.005	6.371	7.297
	10000				380-30		
13	1	1		4.254	4.900	-	-
13	2	1		3.989	4.819	5.727	6.312
13	2	2		4.385	5.199	6.134	6.792
13	3	1		4.095	5.024	6.081	6.846
13	3	2		4.485	5.371	6.407	7.138
13	3	3		4.539	5.613	6.755	7.449
13	4	1		4.045	4.963	6.325	7.052
13	4	2		4.484	5.368	6.587	7.434
13	5	1		4.043	4.993	6.288	7.238
1	1			0.75-			$\neg$
14	1	1		3.728	4.963		-
14	2	1		4.070	4.863	5.737	6.356
14	2	2		4.441	5.193	6.045	6.812
14	3	1		4.075	4.977	6.029	6.811
14	3	2		4.515	5.383	6.413	7.218
14	4	1	,	4.020	4.991	6.265	7.176
				2.042	F 000		
15	1	1		3.843	5.020	-	0.050
15	2	1		4.032	4.827	5.599	6.053
15	2	2		4.461	5.184	6.044	6.760
15	3	1		4.055	5.019	6.139	6.813
10		1		3 000	A E 1 1	E 070	
16	1	1		3.886	4.511	5.070	6 190
16	2	1		4.044	4.849	5.670	6.189
17	1	1		3.986	4.581	5.116	-
00	00	00		4.605	5.991	7.824	9.210
					200 100 No. 1	The second second	

### Critical values for the Kruskal-Wallis test (small sample sizes)

	san si:	nple		α	10%	5%	2%	1%
1	1	1	1		-	-	-	-
2	1	1	1		-	-	-	-
2	2	1	1		-	-	-	
2	2	2	1		5.357	5.679	_	-
2	2	2	2		5.667	6.167	6.667	6.667
3	1	1	1		\	=	_	-2
3	2	1	1		5.143	-	-	-
3	2	2	1	1	5.556	5.833	6.500	-
3	2	2	2		5.644	6.333	6.978	7.133
3	3	1	1	1	5.333	6.333	-	-
3	3	2	1	1	5.689	6.244	6.689	7.200
3	3	2	2		5.745	6.527	7.182	7.636
3	3	3	1		5.655	6.600	7.109	7.400
3	3	3	2		5.879	6.727	7,636	8.015
3	3	3	3		6.026	7.000	7.872	8.538
4	1	1	1		-	-	-	_
4	2	1	1		5.250	5.833	-	-
4	2	2	1		5.533	6.133	6.667	7.000
4	2	2	2		5.755	6.545	7.091	7.391
4	3	1	1		5.067	6.178	6.711	7.067
4	3	2	1		5.591	6.309	7.018	7.455
4	3	2	2		5.750	6.621	7.530	7.871
4	3	3	1		5.689	6.545	7.485	7.758
4	3	3	2		5.872	6.795	7.763	8.333
4	3	3	3		6.016	6.984	7.995	8.659
4	4	1	1		5.182	5.945	7.091	7.909
4	4	2	1		5.568	6.386	7.364	7.909
4	4	2	2	1	5.808	6.731	7.750	8.346
4	4	3	1		5.692	6,635	7.660	8.231
4	4	3	2		5.901	6.874	7.951	8.621
4	4	3	3		6.019	7.038	8.181	8.876
4	4	4	1	1	5.654	6.725	7.879	8.588
4	4	4	2		5.914	6.957	8.157	8.871

5     6     6 <th>1 1 1 2 1 2 2 1 1 2 2 2 3 1 3 2 3 3 1 1</th> <th></th> <th>5.333 5.267 5.542 5.636 5.160 5.518 5.772</th> <th>6.109 6.564 6.004 6.364</th> <th>- 6.600 6.927 7.364 6.964 7.285</th> <th>7.276 7.773 7.400</th>	1 1 1 2 1 2 2 1 1 2 2 2 3 1 3 2 3 3 1 1		5.333 5.267 5.542 5.636 5.160 5.518 5.772	6.109 6.564 6.004 6.364	- 6.600 6.927 7.364 6.964 7.285	7.276 7.773 7.400
6 2 2 2 3 3 3 3 3 5 5 5 5 5 5 5 5 5 5 5 5	2 1 2 2 1 1 2 1 2 2 3 1 3 2 3 3 1 1		5.542 5.636 5.160 5.518	6.109 6.564 6.004 6.364	6.927 7.364 6.964	7,773
5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	2 2 1 1 2 1 2 2 3 1 3 2 3 3 1 1		5.636 5.160 5.518	6.564 6.004 6.364	7.364 6.964	7,773
5     6     6 <td>1 1 2 1 2 2 3 1 3 2 3 3 1 1</td> <td></td> <td>5.160 5.518</td> <td>6.004 6.364</td> <td>6.964</td> <td></td>	1 1 2 1 2 2 3 1 3 2 3 3 1 1		5.160 5.518	6.004 6.364	6.964	
5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	2 1 2 2 3 1 3 2 3 3 1 1		5.518	6.364		7.400
5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	2 2 3 1 3 2 3 3 1 1				7.285	
5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	3 1 3 2 3 3 1 1		5.772			7.758
5 5 3 3 4 4 4 4 4 4 4 5 5 5 5 5 5 5 5 5	3 2 3 3 1 1			6.664	7,626	8.203
5 3 4 4 4 4 4 4 4 5 5 5 5 5 5 5 5 5 5 5	3 3 1 1		5.667	6.641	7.656	8.128
5 5 4 4 4 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5	1 1		5.866	6.822	7.912	8.607
5 4 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5			6.021	7.019	8.124	8.848
5 4 5 4 5 5 5 5 5 5 5 5 5 6 1 2 2 6 6 3 6 3 6 3 6 4	-		5.255	6.041	7.182	7.909
5 4 5 4 5 5 5 5 5 5 5 5 5 6 1 6 6 2 6 6 3 6 6 3 6 6 3	2 1		5.581	6.419	7.477	8.173
5 4 5 5 5 5 5 5 5 5 5 6 2 6 2 6 3 6 3 6 3 6 3	2 2		5.782	6.725	7.849	8.473
5 4 5 5 5 5 5 5 5 5 5 6 1 6 2 6 2 6 3 6 3 6 3 6 3	3 1		5.656	6.685	7,793	8.409
5 5 5 5 5 5 5 5 5 5 6 1 6 2 6 2 6 3 6 3 6 3 6 3 6 4	3 2		5.902	6.926	8.069	8.802
5 5 5 5 5 5 6 1 6 2 6 2 6 3 6 3 6 3 6 3 6 4	4 1		5.674	6.760	7.986	8.726
5 5 5 5 6 1 6 2 6 2 6 3 6 3 6 3 6 3 6 4	1 1		5.154	6.077	7.308	8.108
5 5 6 1 6 2 6 2 6 2 6 3 6 3 6 3 6 3 6 3	2 1		5.585	6.541	7.536	8.327
6 1 6 2 6 2 6 2 6 3 6 3 6 3 6 3	2 2		5.800	6.777	7.943	8.634
6 2 6 2 6 3 6 3 6 3 6 3	3 1		5.663	6.745	7.857	8.611
6 2 6 2 6 3 6 3 6 3 6 3 6 3	1 1		6.667	5.667	-	-
6 2 6 3 6 3 6 3 6 3 6 3 6 4	1 1		.145	5.964	6.600	7.036
6 3 6 3 6 3 6 3 6 3	2 1		.470	6.242	7.000	7.500
6 3 6 3 6 3 6 3 6 4	2 2	. 5	.744	6.538	7.513	7.923
6 3 6 3 6 3	1 1	. 5	.197	6.045	7.091	7.621
6 3 6 3 6 4	2 1	. 5	5.577	6.397	7.321	7.885
6 3	2 2	. 5	.780	6.703	7.758	8.363
6 4	3 1	5	.659	6.637	7.725	8.220
	3 2	. 5	.886	6.876	7.962	8.695
	1 1	5	.186	6.071	7.250	8.000
6 4	2 1	5	.571	6.489	7.516	8.302
6 4	2 2	- 5	.810	6.743	7.929	8.610
6 4	3 1	5	.657	6.710	7.819	8.538

		nple zes		α	10%	5%	2%	1%
6	5	2	1		5.589	6.541	7.598	8.389
6	6	1	1		5.219	6.133		8.181
7	1	1	1		5.197	5.945	_	_
7	2	1	1	П	5.097	6.006	6.786	7.273
7	2	2	1	ш	5.484	6.319	7.011	7.626
7	2	2	2		5.689	6.565	7.568	8.053
7	3	1	1		5.147	6.070	7.037	7.652
7	3	2	1		5.576	6.466	7.383	8.005
7	3	2	2		5.795	6.718	7.759	8.407
7	3	3	1		5.664	6.671	7.721	8.352
7	4	1	1		5.169	6.104	7.222	8.032
7	4	2	1		5.580	6.543	7.531	8.337
7	5	1	1		5.225	6/113	7.318	8.148
8	1	1	1		4.955	6.182	-	-
8	2	1	1		5.154	5.933	6.692	7.423
8	2	2	1		5.481	6.305	7.096	7.648
8	2	2	2		5.714	6.571	7.600	8.207
8	3	1	1		5.231	6.099	7.154	7.788
8	3	2	1		5.579	6.464	7.455	8.114
8	4	1	1		5.200	6.143	7.271	8.029
9	1	1	1		4.880	5.701	6.385	-
9	2	1	1		5.128	5.919	6.725	7.326
9	2	2	1		5.492	6.292	7.130	7.692
9	3	1	1		5.216	6.105	7,171	7.768
10	1	1	1		5.037	5.908	6.560	-
10	2	1	1	1	5.194	5.937	6.794	7.251
11	1	1	1		1.969	5.457	6.714	
00	00	00	000		3.251	7,815	9.837	11,34

		am; size			α	10%	5%	2%	1%
1	1	1	1	1		-	-	-	-
2	1	1	1	1			_	-	=
2	2	1	1	1		5.786	-	-	-
2	2	2	1	1		6.250	6.750	-	-
2	2	2	2	1		6.600	7.133	7.533	7.533
2	2	2	2	2		6.982	7.418	8.073	8.291
3	1	1	1	1		S	-	-	_
3	2	1	1	1		6.139	6.583	-	-
3	2	2	1	1	1	6.511	6.800	7.400	7.600
3	2	2	2	1	1	6.709	7.309	7.836	8.127
3	2	2	2	2		6.955	7.682	8.303	8.682
3	3	1	1	1		6.311	7.111	7.467	-
3	3	2	1	1		6.600	7.200	7.782	8.073
3	3	2	2	1	1	6.788	7.591	8.258	8.576
3	3	2	2	2		7.026	7.910	8.667	9.115
3	3	3	1	1		6.788	7.576	8.242	8.424
3	3	3	2	1	1	6.910	7.769	8.590	9.051
3	3	3	2	2		7.121	8.044	9.011	9.505
3	3	3	3	1		7.077	8.000	8.879	9.451
4	1	1	1	1		6.167	-	-	-
4	2	1	1	1		6.200	6.733	7 267	

	3	amp			a	10%	5%	2%	1%
4	2	2	1	1		6.491	7.145	7.636	7,936
4	2	2	2	1		6.773	7.500	8.205	8.545
4	2	2	2	2	1	7.000	7.846	8.673	9.077
4	3	1	1	1	ш	6.227	7.073	7.691	8.236
4	3	2	1	1		6.614	7.439	8.091	8.394
4	3	2	2	1		6.833	7.679	8.545	8.962
4	3	2	2	2	1	7.055	7.984	8.918	9.429
4	3	3	1	1		6.737	7.660	8.513	8.891
4	3	3	2	1		6.956	7.874	8.830	9.374
4	4	1	1	1		6.364	7.114	8.182	8.636
4	4	2	1	1		6.654	7.500	8.385	8.885
4	4	2	2	1		6.890	7.797	8.802	9.330
4	4	3	1	1		6.758	7.714	8.742	9.247
5	1	1	1	1		6.667	6.667	-	-
5	2	1	1	1		6.295	6.905	7.418	7.855
5	2	2	1	1		6.527	7.273	7.909	8.318
5	2	2	2	1	1	6.754	7.600	8.408	8.831
5	2	2	2	2	1	6.989	7.925	8.782	9.316
5	3	1	1	1		6.364	7.164	7.939	8.303
5	3	2	1	1		6.641	7.462	8.272	8.756
5	3	2	2	1		6.866	7.756	8.705	9.251
5	3	3	1	1	1	6.725	7.684	8.651	9.187

k = 5 samples  $(N \le 13)$ 

		size			α	10%	5%	2%	1%
5	4	1	1	1	1	6.388	7.154	8.235	8.831
5	4	2	1	1	1	6.679	7.520	8.492	9.152
5	5	1	1	1		6.356	7.226	8.334	9,152
6	1	1	1	1	Г	6.073	7.091	-	-
6	2	1	1	1		6.288	6.909	7,682	8.000
6	2	2	1	1	1	6.577	7,308	8.051	8.628
6	2	2	2	1		6.802	7.593	8.549	9.077
6	3	1	1	1		6.423	7.051	8.064	8.590
6	3	2	1	1		6.648	7.505	8.407	9.000
6	4	1	1	1		6.396	7.187	8.286	9.033
7	1	1	7	1		6.182	6.831	7.455	-
7	2	1	1	1		6.368	6.984	7.753	8.231
7	2	2	1	1	1	6.593	7.356	8.143	8.689
7	3	1	1	1	1	6.367	7.152	8.119	8.779
8	1	1	1	1		6.087	6.538	7.769	-
8	2	1	1	1		6.338	6.997	7.821	8.308
9	1	1	1	1		6.095	6.755	7.458	8.044
00	be.	.00	90	00	1	7.779	9.488	11.67	13.28

 $k = 6 \text{ samples } (N \le 13)$ 

			n p l	e		Ct	10%	5%	2%	1%
1	1	1	1	1	1		-	=	-	-
2	1	1	1	1	1		-	-	-	-
2	2	1	1	1	1		6.833	-	-	-
2	2	2	1	1	1		7.267	7,600	7.800	-
2	2	2	2	1	1		7.527	8.018	8.455	8.618
2	2	2	2	2	1		7.909	8.455	9.000	9.227
2	2	2	2	2	2		8.154	8.846	9.538	9.846
3	1	1	1	1	1		_	84	-	-
3	2	1	1	1	1		7.133	7.467	-	-
3	2	2	1	1	1		7.418	7.945	8.345	8.509
3	2	2	2	1	1		7.727	8.348	8.939	9.136
3	2	2	2	2	1		7.987	8.731	9.346	9.692
3	2	2	2	2	2		8.198	9.033	9.813	10.22
3	3	1	1	1	1		7.400	7.909	8.564	8.564
3	3	2	1	1	1		7.697	8.303	8.803	9.045
3	3	2	2	1	1		7.872	8,615	9.269	9.628

			npie zes			α 10%	5%	2%	1%
3	3	2	2	2	1	8.077	8.923	9,714	10.15
3	3	3	1	1	1	7.821	8.641	9.205	9.564
3	3	3	2	1	1	8.000	8.835	9.670	10.08
4	1	1	1	1	1	7.333	7.333	-	-
4	2	1	1	1	1	7.255	7.827	8.236	8.400
4	2	2	1	1	1	7.545	8.205	8.727	9.000
4	2	2	2	1	1	7.808	8.558	9.192	9.538
4	2	2	2	2	1	8.044	8.868	9.643	10.07
4	3	1	1	-1	1	7.394	8.053	8.758	9.023
4	3	2	1	1	1	7.679	8.429	9.115	9.506
4	3	2	2	1	1	7,929	8.742	9.577	10.01
4	3	3	1	1	1	7.780	8.654	9.495	9.934
4	4	1	1	1	1	7.404	8.231	9.096	9.538
4	4	2	1	1	1	7.714	8.571	9.445	9.940
5	1	1	1	1	1	7.385	7.909		_
5	2	1	1	1	1	7.345	7.891	8.473	8.682

			iple res			α 10%	5%	2%	1%
5	2	2	1	1	1	7.638	8.308	8.938	9.362
5	2	2	2	1	1	7.833	8.624	9.442	9.890
5	3	1	1	1	. 1	7.369	8.169	9.062	9.503
5	3	2	1	1	1	7.701	8,495	9.371	9.837
5	4	1.	1	1	1	7.503	8.242	9.234	9.841
6	1	1	1	1	1	7,197	7.879	8.409	-
6	2	1	1	1	1	7.397	8.013	8.692	9.051
6	2	2	1	1	1	7.626	8.374	9.165	9.604
6	3	1	1	1	1	7.473	8.209	9.176	9.659
7	1	1	1	1	1	7.198	7.791	8.846	8.846
7	2	1	1	1	1	7.389	8.119	8.821	9.268
8	1	1	1	1	1	7.154	7.788	8.712	9.231
00	00	00	00	00	00	9.236	11.07	13.39	15.09

## Critical values for the Kruskal-Wallis test (equal sample sizes)

$$H = \frac{12}{n^2 k(nk+1)} \sum_{i=1}^{k} R_i^2 - 3(nk+1)$$

		k = 3		
a	10%	5%	2%	1%
2	4.571	-	-	_
3	4.622	5.600	6.489	7.200
4	4.654	5.692	6.962	7.654
5	4.560	5.780	7.220	8.000
6	4.643	5.801	7.240	8.222
7	4.594	5.819	7.332	8.378
8	4.595	5.805	7.355	8.465
9	4.586	5.831	7.418	8.529
10	4.581	5.853	7.453	8.607
11	4.587	5.885	7.489	8.648
12	4.578	5.872	7.523	8.712
13	4.601	5.901	7.551	8.735
14	4.592	5.896	7.566	8.754
15	4.591	5.902	7.582	8.821
16	4.595	5.909	7.596	8.822
17	4.593	5.915	7.609	8.856
18	4.596	5.932	7.622	8.865
19	4.598	5.923	7.634	8.887
20	4.594	5.926	7.641	8.905
21	4.597	5.930	7.652	8.918
22	4.597	5.932	7.657	8.928
23	4.598	5.937	7.664	8.947
24	4.598	5.936	7.670	8.964
25	4.599	5.942	7.682	8.975
00	4.605	5.991	7.824	9.210

10%	5%	2%	1%
5.667	6.167	6.667	6.667
6.026	7.000	7.872	8.538
6.088	7.235	8.515	9.287
6.120	7.377	8.863	9.789
6.127	7.453	9.027	10.09
6.141	7.501	9,152	10.25
6.148	7.534	9.250	10.42
6.161	7.557	9.316	10.53
6.167	7.586	9.376	10.62
6.163	7.623	9.422	10.69
6.185	7.629	9.458	10.75
6.191	7.645	9.481	10.80
6.198	7.658	9.508	10.84
6.201	7.676	9.531	10.87
6.205	7.678	9.550	10.90
6.206	7.682	9.568	10.92
6.212	7.698	9.583	10.95
6.212	7.701	9.595	10.98
6.216	7.703	9.606	10.98
6.218	7.709	9.623	11.01
6.215	7.714	9.629	11.03
6.220	7.719	9.640	11.03
6.221	7.724	9.652	11.06
6.222	7.727	9.659	11.07
6.251	7.815	9.837	11.34

10%	5%	2%	1%
6.982	7.418	8.073	8.291
7.333		9.467	
7.457	0.000		
7.532	8.876	10.47	11.57
7.557	9.002	10.72	11.91
7.600	9.080	10.87	12.14
7.624	9.126	10.99	12.29
7.637	9.166	11.06	12.41
7.650	9.200	11.13	12.50
7.660	9.242	11.19	12.58
7.675	9.274	11.22	12.63
7.685	9.303	11.27	12.69
7.695	9.307	11.29	12.74
7.701	9.302	11.32	12.77
7.705	9.313	11.34	12.79
7.709	9.325	11.36	12.83
7.714	9.334	11.38	12.85
7.717	9.342	11.40	12.87
7.719	9.353	11.41	12.91
7.723	9.356	11.43	12,92
7.724	9.362	11.43	12.92
7.727	9.368	11.44	12.94
7.729	9.375	11.45	12.96
7.730	9.377	11.46	12.96
7.779	9,488	11.67	13.28

		Г	k = 6		
	10%	5%	2%	1%	9/2
Ì	8.154	8.846	9.538	9.846	2
١	8.620	9.789	11.03	11.82	3
1	8.800	10.14	11.71	12.72	4
	8.902	10.36	12.07	13.26	5
Ì	8.958	10.50	12,33	13.60	6
1	8.992	10.59	12.50	13.84	7
1	9.037	10.66	12.62	13.99	8
9	9.057	10.71	12.71	14.13	9
	9.078	10.75	12.78	14.24	10
Ī	9.093	10.76	12.84	14.32	11
1	9.105	10.79	12.90	14.38	12
1	9.115	10.83	12.93	14.44	13
1	9.125	10.84	12.98	14.49	14
1	9.133	10.86	13.01	14.53	15
	9.140	10.88	13.03	14.56	16
ı	9.144	10.88	13.04	14.60	17
1	9.149	10.89	13.06	14.63	18
1	9.156	10.90	13.07	14.64	19
1	9.159	10.92	13.09	14.67	20
	9.164	10.93	13.11	14.70	21
ı	9.168	10.94	13.12	14.72	22
ı	9.171	10.93	13.13	14.74	23
ı	9.170	10.93	13.14	14.74	24
l	9.177	10.94	13.15	14.77	25
	9.236	11.07	13.39	15.09	00

For description, see page 28.

### Critical values for Friedman's test

$$M = \frac{12}{nk(k+1)} \sum_{i=1}^{k} R_i^2 - 3n(k+1)$$

		k = 3		
Va	10%	5%	2%	1%
2	_	_	_	_
3	6.000	6.000	_	-
4	6.000	6.500	8.000	8.000
5	5.200	6.400	8.400	8.400
6	5.333	7.000	8.333	9.000
7	5.429	7.143	8.000	8.857
8	5.250	6.250	7.750	9.000
9	5.556	6.222	8.000	9.556
10	5.000	6.200	7.800	9.600
11	5.091	6.545	7.818	9.455
12	5.167	6.500	8.000	9.500
13	4.769	6.615	8.000	9.385
14	5.143	6.143	8.143	9.143
15	4.933	6.400	8.133	8.933
16	4.875	6.500	7.875	9.375
17	5.059	6.118	7.529	9.294
18	4.778	6.333	8.111	9.000
19	5.053	6.421	7.895	9.579
20	4.900	6.300	7.900	9.300
21	4.952	6.095	7.714	9.238
22	4.727	6.091	8.273	9.091
23	4.957	6.348	8.087	9.391
24	5.083	6.250	7.750	9.250
25	4.880	6.080	7.760	8.960
00	4,605	5,991	7.824	9.210

	k =	= 4	
10%	5%	2%	1%
6.000	6.000	-	-
6.600	7.400	8.200	9.000
6.300	7.800	8.400	9.600
6.360	7.800	9.000	9.960
6.400	7.600	9.400	10.20
6.429	7.800	9.171	10.54
6.300	7.650	9.450	10.50
6.200	7.667	9.400	10.73
6.360	7.680	9.480	10.68
6.273	7.691	9.655	10.75
6.300	7.700	9.500	10.80
6.138	7.800	9.646	10.85
6.343	7.714	9.600	10.89
6.280	7.720	9.640	10.92
6.300	7.800	9.600	10.95
6.318	7.800	9.635	11.05
6.333	7.733	9.667	10.93
6.347	7.863	9.632	11.02
6.240	7.800	9.600	11.10
6.314	7.800	9.686	11.06
6.327	7.800	9.709	11.07
6.287	7.800	9.678	11.09
6.250	7.750	9.700	11.15
6.264	7.800	9.672	11.16
6.251	7.815	9.837	11.34

k = 5				
10%	5%	2%	1%	
7.200	7.600	8.000	8.000	
7.467	8.533	9.600	10.13	
7.600	8.800	10.20	11.20	
7.680	8.960	10.56	11.68	
7.733	9.067	10.80	11.87	
7.771	9.143	10.97	12.11	
7.700	9.200	11.00	12.30	
7.733	9.244	11.11	12.44	
7.760	9.280	11.20	12.48	
7.782	9.309	11.20	12.58	
7.733	9.333	11.27	12.60	
7.754	9.354	11.32	12.68	
7.771	9.371	11.37	12.74	
7.787	9.387	11.36	12.80	
7.750	9.400	11.40	12.80	
7.765	9.412	11.44	12.85	
7.778	9.422	11.47	12.89	
7.789	9.432	11.45	12.88	
7.760	9.400	11.48	12.92	
7.771	9.448	11.50	12.91	
7.782	9.418	11.49	12.95	
7.791	9.426	11.51	12.97	
7.767	9.433	11.50	13.00	
7.776	9.440	11.52	12.99	
7.779	9.488	11.67	13.28	

	F	k = 6		
10%	5%	2%	1%	9/1
8.286	9.143	9.429	9.714	2
8.714	9.857	11.00	11.76	3
9.000	10.29	11.71	12.71	4
9.000	10.49	12.09	13.23	5
9.048	10.57	12.38	13.62	6
9.122	10.67	12.55	13.86	7
9.071	10.71	12.64	14.00	8
9.127	10.78	12.75	14.14	9
9.143	10.80	12.80	14.23	10
9.130	10.84	12.92	14.32	11
9.143	10.86	12.95	14.38	12
9.176	10.89	13.00	14.45	13
9.184	10.90	13.02	14.49	14
9.210	10.92	13.06	14.54	15
9.214	10.96	13.07	14.57	16
9.202	10.95	13,10	14.61	17
9.206	10.95	13.11	14.63	18
9.196	11.00	13.14	14.67	19
9.200	11.00	13.11	14.66	20
9.218	10.99	13.14	14.69	21
9.221	10.96	13.14	14.73	22
9.236	11.00	13.19	14.73	23
9.238	10.95	13.19	14.74	24
9.229	10.99	13.21	14.74	25
9.236	11.07	13,39	15.09	00

### Critical values for nonparametric tests with large samples

For all the eight tests dealt with on pages 26-34 there are approximate methods for finding critical values when sample sizes exceed those covered in the tables.

Approximate critical values for the sign test, Wilcoxon signed-rank test and Mann—Whitney U test may be found from the table of percentage points of the standard normal distribution on page 20. Denote by z the appropriate percentage point of the standard normal distribution, e.g. 1.9600 for an  $\alpha_2=5\%$  two-sided test or 1.6449 for an  $\alpha_1=5\%$  one-sided test. Then calculate  $\mu$  and  $\sigma$  from the table below. The required critical value is  $[\mu-z\sigma-\frac{1}{2}]$ , the square brackets denoting the integer part.

	Д	σ
sign test	$\frac{1}{2}n$	½√n
Wilcoxon signed-rank test	$\frac{1}{4}n(n+1)$	$\left\{\frac{1}{24}n(n+1)(2n+1)\right\}^{1/2}$
Mann-Whitney U test	$\frac{1}{2}n_{1}n_{2}$	$\{\frac{1}{12}n_1n_2(n_1+n_2+1)\}^{1/2}$

For example in the sign test with sample size n=144,  $\mu=\frac{1}{2}(144)=72$  and  $\sigma=\frac{1}{2}\sqrt{144}=6$ , so that the  $\alpha_2=5\%$  critical value is  $[72-1.96\times 6-\frac{1}{2}]=[59.74]=59$ , i.e. the  $\alpha_2=5\%$  critical region is  $S\leqslant 59$ . The reader may verify similarly that (i) for the signed-rank test with n=144:  $\mu=5220$ ,  $\sigma=501.428$ , and the  $\alpha_2=5\%$  critical region is  $T\leqslant 4236$ ; and (ii) in the Mann-Whitney test with sample sizes 25 and 30:  $\mu=375$ ,  $\sigma=59.161$ , and the  $\alpha_2=5\%$  critical region is  $U\leqslant 258$ .

For the Kolmogorov-Smirnov goodness-of-fit test, approximate critical values are simply found by dividing the constants b in the following table by  $\sqrt{n}$ :

$\alpha_1$	5%	21/2%	1%	1/2%
$\alpha_2$	10%	5%	2%	1%
b	1.2238	1.3581	1.5174	1.6276
C	0.8255	0.8993	0.9885	1.0500

So with a sample of size n=144, the  $\alpha_2=5\%$  critical value is  $1.3581/\sqrt{144}=0.1132$ , i.e. the critical region is  $D_{144}\geqslant 0.1132$ . The same constants b are used to obtain approximate critical regions for the Kolmogorov–Smirnov two-sample test. In this case b is multiplied by  $\{1/n_1+1/n_2\}^{1/2}$  to give critical values for D (not  $D^*$ ). So with sample sizes 25 and 30,  $\{1/n_1+1/n_2\}^{1/2}=\{1/25+1/30\}^{1/2}=0.2708$  and the  $\alpha_2=5\%$  critical region is  $D\geqslant 1.3581\times 0.2708=0.3678$ . For the Kolmogorov–Smirnov test for normality (with unspecified mean and standard deviation), the critical values are found as in the goodness-of-fit test except that the second row of constants c is used instead of b. In this case the  $\alpha_2=5\%$  critical region with n=144 is  $D_{144}\geqslant 0.8993/\sqrt{144}=0.0749$ .

Finally, the Kruskal-Wallis and Friedman test statistics are, for large sample sizes, both distributed approximately as the  $\chi^2$  distribution with  $\nu=k-1$  degrees of freedom. The appropriate values have been inserted at the ends of the tables on pages 32-34;  $\alpha_1^R$  values from the  $\chi^2$  table (page 21) are appropriate.

### Linear and rank correlation

When data consist of pairs (X,Y) of related measurements it is often important to study whether there is at least an approximate linear relationship between X and Y. The strength of such a relationship is measured by the linear correlation coefficient  $\rho$  (rho), which always lies between -1 and +1.  $\rho=0$  indicates no linear relationship;  $\rho=+1$  and  $\rho=-1$  indicate exact linear relationships of  $+\infty$  and  $+\infty$  slopes respectively. More generally, values of  $+\infty$  near 0 indicate little linear relationship, and values near  $+\infty$  1 or  $+\infty$ 1 indicate strong linear relationships.

Tests, etc. concerning  $\rho$  are formulated using the sample linear correlation coefficient  $r=\Sigma (X-\bar{X})(Y-\bar{Y})/\{\Sigma (X-\bar{X})^2\Sigma (Y-\bar{Y})^2\}^{1/2}, \bar{X}$  and  $\bar{Y}$  being the sample mean values of X and Y. The first table on page 36 is for testing the null hypothesis  $H_0$  that  $\rho=0$ . Critical regions are  $|r| \geq tabulated\ value$  if  $H_1$  is the two-sided alternative hypothesis  $\rho \neq 0$  (using significance levels  $\alpha_2$ ) or  $r \geq tabulated\ value$  or  $r \leq -(tabulated\ value)$  if  $H_1$  is  $\rho > 0$  or  $\rho < 0$  respectively (using levels  $\alpha_1^R$ ).

The following data show the market value (in units of £10 000) of eight houses four years ago (X) and currently (Y).

X	0.8 1.3	1.7	2.4	0.9	1.2	1.6	1.7	2.9
Y	1.3	3.3	3.8	1.1	2.4	3.1	3.5	3.9

Here r is found to be 0.8918. This is very strong evidence in favour of

the one-sided  $H_1\colon \rho>0$ , since the  $\alpha_1^R=\frac{1}{2}\%$  critical region with sample size n=8 is  $r\geqslant 0.8343$ . Had  $\alpha_1^L$  critical values been required, they would have been given by the  $\alpha_1^R$  values prefixed with a minus sign.

The construction of confidence intervals for  $\rho$  and the testing of values of  $\rho$  other than  $\rho = 0$  may be accomplished using Fisher's z-transformation. For any value of r or  $\rho$ , this gives a 'z-value', z(r) or  $z(\rho)$ , computed from

$$z(r) = \frac{1}{2}\log_e\left(\frac{1+r}{1-r}\right) = 1.1513\log_{10}\left(\frac{1+r}{1-r}\right)$$

and z(r) is known to have an approximate normal distribution with mean  $z(\rho)$  and standard deviation  $1/\sqrt{n-3}$ . A table giving z(r) is provided on page 36, and on page 37 there is a table for converting back from a z-value to its corresponding r-value or  $\rho$ -value. If r or  $\rho$  is -ve, attach a minus sign to the z-value, and vice versa.

So to find a  $\gamma=95\%$  confidence interval for  $\rho$  with the above data, we first find the 95% confidence interval for  $z(\rho)$  as  $\{z(r)-1.9600/\sqrt{n-3}:z(r)+1.9600/\sqrt{n-3}\}$  (the 1.9600 being the  $\gamma=95\%$  value in the table of normal percentage points on page 20) where n=8 and z(r)=z(0.8918), which is about 1.4306 (interpolating between z(0.891)=1.4268 and z(0.892)=1.4316 on page 36). This interval works out to (0.554:2.307). These limits for the value of  $z(\rho)$  are then converted to  $\rho$ -values by the table on page 37, giving the confidence interval for  $\rho$  of (0.503:0.980). As a second example, if we wish to test  $H_0$ :  $\rho=0.8$  against  $H_1$ :  $\rho>0.8$  at the  $\alpha_1^R=5\%$  significance level, the critical value for z(r) would be  $z(0.8)+1.6449/\sqrt{n-3}=1.0986+1.6449/\sqrt{5}=1.834$  (the 1.6449 again coming from page 20). The critical region  $z(r) \ge 1.834$  then converts to  $r \ge 0.950$  from page 37, and so we are unable to reject  $H_0$ :  $\rho=0.8$  in favour of  $H_1$ :  $\rho>0.8$  at this significance level.

An alternative and quicker method is to use the charts on pages 38-39. For confidence intervals, locate the obtained value of r on the horizontal axis, trace along the vertical to the points of intersection with the two curves labelled with the sample size n, and read off the confidence limits on the vertical axis. For critical values, locate the hypothesised value of  $\rho$ , say  $\rho_0$ , on the vertical axis, trace along the horizontal to the points of intersection with the two curves, and read off the critical values on the horizontal axis. If these two values are  $r_1$  and  $r_2$ , with  $r_1 < r_2$ , then the one-sided critical regions with significance level  $\alpha_1$  for testing  $H_0$ :  $\rho = \rho_0$  against  $H_1$ :  $\rho < \rho_0$  or  $H_1$ :  $\rho > \rho_0$  are  $r < r_1$  and  $r > r_2$  respectively, and the critical region with significance level  $\alpha_2 = 2\alpha_1$  for testing  $H_0$  against  $H_1$ :  $\rho \ne \rho_0$  is comprised of both of these one-sided regions.

The reader may check the charts for the results found above using the z-transformation. Accuracy may be rather limited, especially when r and  $\rho$  are close to +1 or -1; however the z-transformation methods are not completely accurate either, especially for small n. Further inaccuracies may occur for sample sizes not included on the charts, in which case the user has to judge distances between the curves.

All of the above work depends on the assumption that (X, Y) has a bivariate normal distribution. Tables for two nonparametric methods, which do not require such an assumption, are given on page 40. These methods do not test specifically for linearity but for the tendency of Y to increase (or decrease) as X increases.

To calculate Spearman's rank correlation coefficient, first rank the X-values and Y-values separately from 1 to n, calculate the difference in ranks for each (X, Y) pair, and sum the squares of these differences to obtain  $D^2$ . Spearman's coefficient  $r_S$  is calculated as  $r_S = 1 - 6D^2/(n^3 - n)$ . With the above data we have:

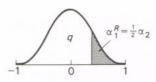
X-ranks	1	51/2	7	2	3	4	51	8
Y-ranks	2	5	7	1	3	4	6	8
rank differences	-1	$\frac{1}{2}$	0	1	0	0	$-\frac{1}{2}$	0

Thus  $D^2$  is  $2(1)^2 + 2(\frac{1}{2})^2 + 4(0)^2 = 2\frac{1}{2}$ , giving  $r_S = 1 - 6 \times 2\frac{1}{2}/(8^3 - 8) = 0.9702$ . The  $\alpha_1^R = \frac{1}{2}\%$  critical region for testing against the tendency for Y to increase with X is  $r_S \ge 0.8810$ , so there is virtually conclusive proof that this tendency is present. The general forms of the critical regions are the same as for r above.

For Kendall's rank correlation coefficient, we compare each (X,Y) pair in turn with every other pair; if the pair with the smaller X-value also has the smaller Y-value, the pair is said to be concordant, but if it has the larger Y-value the pair is discordant. If  $N_C$  and  $N_D$  are the total numbers of concordant and discordant pairs, Kendall's coefficient  $\tau$  is calculated as  $\tau = (N_C - N_D)/\frac{1}{2}n(n-1)$ , where in fact  $\frac{1}{2}n(n-1)$  is the total number of comparisons made. Any comparison in which the X-values and/or the Y-values are equal counts  $\frac{1}{2}$  to both  $N_C$  and  $N_D$ . Critical regions are of the same forms as with r and  $r_S$ . In the above example,  $N_C = 26\frac{1}{2}$ ,  $N_D = 1\frac{1}{2}$ , and  $\tau = (26\frac{1}{2} - 1\frac{1}{2})/28 = 0.8929$ . This is again clearly significant of the tendency for Y to increase with X, since the  $\alpha_1^R = \frac{1}{2}\%$  critical region is  $\tau \ge 0.7857$ .

Critical regions for large n may be found using the facts that, under the null hypothesis,  $r, r_S$  and  $\tau$  have approximate normal distributions with zero means and standard deviations  $1/\sqrt{n-1}$  for both r and  $r_S$ , and  $\{2(2n+5)/9n(n-1)\}^{1/2}$  for  $\tau$ . For example the reader may check that with n=144 the approximate  $\alpha_2=5\%$  critical regions are  $|r| \ge 0.1639$ ,  $|r_S| \ge 0.1639$  and  $|\tau| \ge 0.1102$ .

## Critical values for the sample linear correlation coefficient *r*



q	0.95	0.975	0.99	0.995
$\alpha_i^R$	5%	21/2%	1%	1/2%
$\alpha_2$	10%	5%	2%	1%
n				
1	-	-	-	==
2	-	-	-	-
3	0.9877	0.9969	0.9995	0.9999
4	0.9000	0.9500	0.9800	0.9900
5	0.8054	0.8783	0.9343	0.9587
6	0.7293	0.8114	0.8822	0.9172
7	0.6694	0.7545	0.8329	0.8745
8	0.6215	0.7067	0.7887	0.8343
9	0.5822	0.6664	0.7498	0.7977
10	0.5494	0.6319	0.7155	0.7646
11	0.5214	0.6021	0.6851	0.7348
12	0.4973	0.5760	0.6581	0.7079
13	0.4762	0.5529	0.6339	0.6835
14	0.4575	0.5324	0.6120	0.6614
15	0.4409	0.5140	0.5923	0.6411
16	0.4259	0.4973	0.5742	0.6226
17	0.4124	0.4821	0.5577	0.6055
18	0.4000	0.4683	0.5425	0.5897
19	0.3887	0.4555	0.5285	0.5751
20	0.3783	0.4438	0.5155	0.5614
21	0.3687	0.4329	0.5034	0.5487
22	0.3598	0.4227	0.4921	0.5368
23	0.3515	0.4132	0.4815	0.5256
24	0.3438	0.4044	0.4716	0.5151
25	0.3365	0.3961	0.4622	0.5052
26	0.3297	0.3882	0.4534	0.4958
27	0.3233	0.3809	0.4451	0.4869
28	0.3172	0.3739	0.4372	0.4785
29	0.3115	0.3673	0.4297	0.4705
30	0.3061	0.3610	0.4226	0.4629

9	0.95	0.975	0.99	0.995
$\alpha_1^R$	5%	2½%	1%	1/2%
α2	10%	5%	2%	1%
n	10.000.000.000.0	800000000000	200700000000	PARTY 1000
31	0.3009	0.3550	0.4158	0.4556
32	0.2960	0.3494	0.4093	0.4487
33	0.2913	0.3440	0.4032	0.4421
34	0.2869	0.3388	0.3972	0.4357
35	0.2826	0.3338	0.3916	0.4296
36	0.2785	0.3291	0.3862	0.4238
37	0.2746	0.3246	0.3810	0.4182
38	0.2709	0.3202	0.3760	0.4128
39	0.2673	0.3160	0.3712	0.4076
40	0.2638	0.3120	0.3665	0.4026
41	0.2605	0.3081	0.3621	0.3978
42	0.2573	0.3044	0.3578	0.3932
43	0.2542	0.3008	0.3536	0.3887
44	0.2512	0.2973	0.3496	0.3843
45	0.2483	0.2940	0.3457	0.3801
46	0.2455	0.2907	0.3420	0.3761
47	0.2429	0.2876	0.3384	0.3721
48	0.2403	0.2845	0.3348	0.3683
49	0.2377	0.2816	0.3314	0.3646
50	0.2353	0.2787	0.3281	0.3610
51	0.2329	0.2759	0.3249	0.3575
52	0.2306	0.2732	0.3218	0.3542
53	0.2284	0.2706	0.3188	0.3509
54	0.2262	0.2681	0.3158	0.3477
55	0.2241	0.2656	0.3129	0.3445
56	0.2221	0.2632	0.3102	0.3415
57	0.2201	0.2609	0.3074	0.3385
58	0.2181	0.2586	0.3048	0.3357
59	0.2162	0.2564	0.3022	0.3328
60	0.2144	0.2542	0.2997	0.3301

9	0.95	0.975	0.99	0.995
$\alpha_1^R$	5%	2%%	1%	1/2%
$\alpha_2$	10%	5%	2%	1%
n				
61	0.2126	0.2521	0.2972	0.3274
62	0.2108	0.2500	0.2948	0.3248
63	0.2091	0.2480	0.2925	0.3223
64	0.2075	0.2461	0.2902	0.3198
65	0.2058	0.2441	0.2880	0.3173
66	0.2042	0.2423	0.2858	0.3150
67	0.2027	0.2404	0.2837 -	0.3126
68	0.2012	0.2387	0.2816	0.3104
69	0.1997	0.2369	0.2796	0.3081
70	0.1982	0.2352	0.2776	0.3060
71	0.1968	0.2335	0.2756	0.3038
72	0.1954	0.2319	0.2737	0.3017
73	0.1940	0.2303	0.2718	0.2997
74	0.1927	0.2287	0.2700	0.2977
75	0.1914	0.2272	0.2682	0.2957
76	0.1901	0.2257	0.2664	0.2938
77	0.1888	0.2242	0.2647	0.2919
78	0.1876	0.2227	0.2630	0.2900
79	0.1864	0.2213	0.2613	0.2882
80	0.1852	0.2199	0.2597	0.2864
82	0.1829	0.2172	0.2565	0.2830
84	0.1807	0.2146	0.2535	0.2796
86	0.1786	0.2120	0.2505	0.2764
88	0.1765	0.2096	0.2477	0.2732
90	0.1745	0.2072	0.2449	0.2702
92	0.1726	0.2050	0.2422	0.2673
94	0.1707	0.2028	0.2396	0.2645
96	0.1689	0.2006	0.2371	0.2617
98	0.1671	0.1986	0.2347	0.2591
100	0.1654	0.1966	0.2324	0.2565

For description, see page 35.

### The Fisher z-transformation

$$z(r) = \frac{1}{2} \log_{e} \left( \frac{1+r}{1-r} \right) = 1.1513 \log_{10} \left( \frac{1+r}{1-r} \right)$$

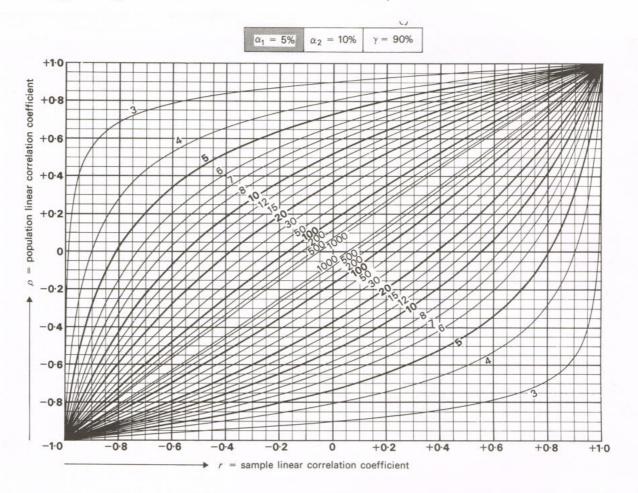
1	0	1	2	3	4	5	6	7	8	9
0.0	0.0000	0.0100	0.0200	0.0300	0.0400	0.0500	0.0601	0.0701	0.0802	0.0902
0.1	0.1003	0.1104	0.1206	0.1307	0.1409	0.1511	0.1614	0.1717	0.1820	0.1923
0.2	0.2027	0.2132	0.2237	0.2342	0.2448	0.2554	0.2661	0.2769	0.2877	0.2986
0.3	0.3095	0.3205	0.3316	0.3428	0.3541	0.3654	0.3769	0.3884	0.4001	0.4118
0.4	0.4236	0.4356	0.4477	0.4599	0.4722	0.4847	0.4973	0.5101	0.5230	0.5361
0.5	0.5493	0.5627	0.5763	0.5901	0.6042	0.6184	0.6328	0.6475	0.6625	0.6777
0.6	0.6931	0.7089	0.7250	0.7414	0.7582	0.7753	0.7928	0.8107	0.8291	0.8480
0.7	0.8673	0.8872	0.9076	0.9287	0.9505	0.9730	0.9962	1.0203	1.0454	1.0714
0.80	1.0986	1.1014	1.1042	1.1070	1,1098	1.1127	1.1155	1.1184	1.1212	1,1241
0.81	1.1270	1.1299	1.1329	1.1358	1.1388	1.1417	1.1447	1.1477	1.1507	1.1538
0.82	1.1568	1.1599	1.1630	1,1660	1.1692	1.1723	1.1754	1.1786	1.1817	1.1849
0.83	1.1881	1.1914	1.1946	1.1979	1.2011	1.2044	1.2077	1.2111	1.2144	1.2178
0.84	1.2212	1.2246	1.2280	1.2315	1.2349	1.2384	1.2419	1.2454	1.2490	1.2526
0.85	1.2562	1.2598	1.2634	1.2671	1.2707	1.2745	1.2782	1.2819	1.2857	1.2895
0.86	1.2933	1.2972	1.3011	1.3050	1.3089	1.3129	1.3169	1.3209	1.3249	1.3290
0.87	1.3331	1.3372	1.3414	1.3456	1.3498	1.3540	1.3583	1.3626	1.3670	1.3714
0.88	1.3758	1.3802	1.3847	1.3892	1.3938	1.3984	1.4030	1.4077	1.4124	1,4171
0.89	1.4219	1.4268	1.4316	1.4365	1.4415	1.4465	1,4516	1.4566	1.4618	1,4670
0.90	1.4722	1.4775	1.4828	1.4882	1.4937	1.4992	1.5047	1.5103	1.5160	1.5217
0.91	1.5275	1.5334	1.5393	1.5453	1.5513	1.5574	1.5636	1.5698	1.5762	1.5826
0.92	1.5890	1.5956	1.6022	1.6089	1.6157	1.6226	1.6296	1.6366	1.6438	1.6510
0.93	1.6584	1.6658	1.6734	1.6811	1.6888	1.6967	1.7047	1.7129	1.7211	1.7295
0.94	1.7380	1.7467	1.7555	1.7645	1.7736	1.7828	1.7923	1.8019	1.8117	1.8216
0.95	1.8318	1.8421	1.8527	1.8635	1.8745	1.8857	1.8972	1.9090	1.9210	1.9333
0.96	1.9459	1.9588	1.9721	1.9857	1.9996	2.0139	2.0287	2.0439	2.0595	2.0756
0.97	2.0923	2.1095	2.1273	2.1457	2.1649	2.1847	2.2054	2.2269	2.2494	2.2729
0.98	2.2976	2.3235	2.3507	2.3796	2.4101	2.4427	2.4774	2.5147	2.5550	2.5987
0.99	2.6467	2.6996	2.7587	2.8257	2.9031	2.9945	3,1063	3.2504	3.4534	3.8002

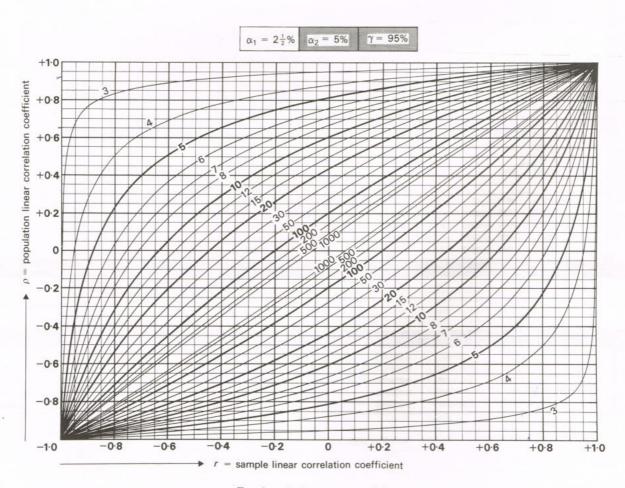
### The inverse of the Fisher z-transformation

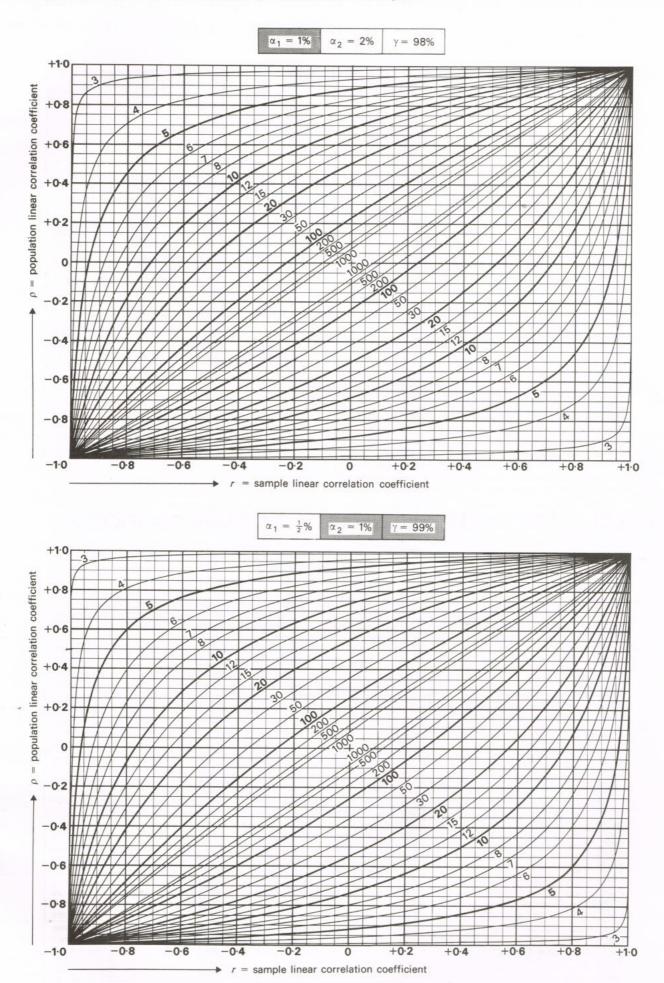
													Р	ROPOR	TION		TS		
Z	0	1	2	3	4	5	6	7	8	9	1	2	3	4	5	6	7	8	
0.0	0.0000	0100	0200	0300	0400	ACC THE ACCORD	A-7-10-2-10-10-1	600-000 total			10	20	30	40	50	60	70	80	9
		2222	0.02			0500	0599	0699	0798	0898	10	20	30	40	50	60	70	80	8
0.1	0.0997	1096	1194	1293	1391			0000000			10	20	30	39	49	59	69	79	8
0.2	0.1974	2070	2165	2260	2255	1489	1586	1684	1781	1877	10	19	29	39	48	58	68	78	8
0.2	0.1574	2070	2100	2260	2355	2449	2543	2636	2729	2821	10	19 19	28	38	48	57	66	76	8
0.3	0.2913	3004	3095	3185	3275	2440	2043	2030	2/29	2021	9	18	28 27	37 36	46 45	56 54	65 63	74 72	8
					1000000	3364	3452	3540	3627	3714	9	17	26	35	44	52	61	70	
0.4	0.3799	3885	3969	4053	4136						8	17	25	34	42	50	59	67	7
						4219	4301	4382	4462	4542	8	16	24	32	40	48	56	64	7
0.5	0.4621	4699	4777	4854	4930						8	15	23	31 -	38	46	54	61	6
						5005	5080	5154	5227	5299	7	15	22	29	36	44	51	58	6
0.6	0.5370	5441	5511	5581	5649						7	14	21	28	35	42	49	56	6
						5717	5784	5850	5915	5980	7	13	20	26	33	39	46	52	Ę
0.7	0.6044	6107	6169	6231	6291	0051	0411	0400	0507	0504	6	12	18	25	31	37	43	49	5
0.8	0.6640	6696	6751	6805	6858	6351	6411	6469	6527	6584	6 5	12	17	23	29	35	40	46	5
0.0	0.0040	0000	0751	0000	0000	6911	6963	7014	7064	7114	5	10	16 15	22	27 25	33	38 35	43	4
0.9	0.7163	7211	7259	7306	7352	0011	0000	7014	7004	/114	5	9	14	19	24	28	33	38	4
					90 (00000)	7398	7443	7487	7531	7574	4	9	13	17	22	26	31	35	3
1.0	0.7616	7658	7699	7739	7779						4	8	12	16	20	24	28	32	3
						7818	7857	7895	7932	7969	4	7	11	15	19	22	26	30	3
1.1	0.8005	8041	8076	8110	8144						3	7	10	14	17	21	24	28	3
					55.846775	8178	8210	8243	8275	8306	3	6	10	13	16	19	22	25	2
1.2	0.8337	8367	8397	8426	8455						3	6	9	12	15	18	20	23	2
	0.0017	0040	0000	0000		8483	8511	8538	8565	8591	3	5	8	11	13	16	19	21	2
1.3	0.8617	8643	8668	8692	8717	0741	0704	0707	2010	0000	2	5	7	10	12	15	17	20	2
1.4	0.8854	8875	8896	8917	8937	8741	8764	8787	8810	8832	2	5	7	9	11	14 12	16 14	18 16	2
		00.0	0000	0017	0007	8957	8977	8996	9015	9033	2	4	6	8	9	11	13	15	1
1.5	0.9051	9069	9087	9104	9121			10070.00701	100000000000000000000000000000000000000	5000000	2	3	5	7	100	7900	Value 1	30/3034	
	0.0001	0000	0007	3104	3121	9138	9154	9170	9186	9201	2	3	5	6	9	10	12 11	14 13	1
1.6	0.9217	9232	9246	9261	9275	0.00	0101	0170	0100	5201	1	3	4	6	7	9	10	12	1
						9289	9302	9316	9329	9341	1	3	4	5	6	8	9	10	1
1.7	0.9354	9366	9379	9391	9402					20.000	1	2	4	5	6	7	8	10	1
	0.0400	0.170		20.22	0000	9414	9425	9436	9447	9458	1	2	3	4	5	6	8	9	1
1.8	0.9468	9478	9488	9498	9508	0547	0507	0500	0545		1	2	3	4	5	6	7	8	
1.9	0.9562	9571	9579	9587	9595	9517	9527	9536	9545	9554	1	2	3	4	4	5	6	7	
	0.0002	3371	3373	3367	9090	9603	9611	9618	9626	9633	1	2	2	3	4	5	6 5	7	
2.0	0.9640	9647	9654	0661	0007	0000		0010	0020	0000		_		- 00		- 00	3.5%		_
	0.0040	3047	5054	9661	9667	9674	9680	9687	9693	9699	1	1	2 2	3	3	4	5	5	
2.1	0.9705	9710	9716	9721	9727	5074	3000	9007	9093	9099	1	1	2 2	2	3	3	4	5	
						9732	9737	9743	9748	9753	0	1	2	2	2	3	4	4	
2.2	0.9757	9762	9767	9771	9776					5,000	0	1	1	2	2	3	3	4	
	V-20-20-00-0		52020000		V. N.S. M. S. N. S. N. S.	9780	9785	9789	9793	9797	0	1	1	2	2	3	3	3	
2.3	0.9801	9805	9809	9812	9816					22.00	0	1	1	2	2	2	3	3	
2.4	0.0027	0040	0040	0040	0010	9820	9823	9827	9830	9833	0	1	- 1	1	2	2	2	3	
2.4	0.9837	9840	9843	9846	9849	9852	9855	9858	9861	0962	0	1	1	1	2	2	2	2	
PAGE 1	0.0000	000-	007			50000000		Association	10.000	9863	0	1	1	1	1	2	2	2	
2.6	0.9866	9869 9892	9871 9895	9874	9876	9879	9881	9884	9886	9888	0	0	1	1	1	1	2	2	
2.7	0.9890	9892	9895	9897 9915	9899 9917	9901 9919	9903 9920	9905 9922	9906 9923	9908	0	0	1	1	1	1	1	2	
2.8	0.9926	9928	9929	9931	9917	9933	9935	9936	9923	9925 9938	0	0	0	1	1	1	1	1	
2.9	0.9940	9941	9942	9943	9944	9945	9946	9947	9949	9950	0	0	0	0	1	1	1	1	
	0	1	2	3	4	5	6	7	8	9	1	2	3	4	5	6	7	8	
Z																			

Z	0	1	2	3	4	5	6	7	8	9
3.	0.995055	0.995949	0.996682	0.997283	0.997775	0.998178	0.998508	0.998778	0.999000	0.999181
4.	0.999329	0.999451	0.999550	0.999632	0.999699	0.999753	0.999798	0.999835	0.999865	0.999889
5.	0.999909	0.999926	0.999939	0.999950	0.999959	0.999967	0.999973	0.999978	0.999982	0.999985
6.	0.999988	0.999990	0.999992	0.999993	0.999994	0.999995	0.999996	0.999997	0.999998	0.999998
7.	0.999998	0.999999	0.999999	0.999999	0.999999	0.999999	0.999999	1.000000	1.000000	1.000000

### Charts giving confidence intervals for $\rho$ and critical values for r







### Critical values for Spearman's rank correlation coefficient

$$r_S = 1 - \frac{6D^2}{n^3 - n^2}$$

$\alpha_1^R$	5%	21/2%	1%	1/2%
$\alpha_2$	10%	5%	2%	1%
п				
1	-	-	77	-
2		-	-	-
3	-	-	-	-
4	1.0000		-	-
5	0.9000	1.0000	1.0000	-
6	0.8286	0.8857	0.9429	1.0000
7	0.7143	0.7857	0.8929	0.9286
8	0.6429	0.7381	0.8333	0.8810
9	0.6000	0.7000	0.7833	0.8333
10	0.5636	0.6485	0.7455	0.7939
11	0.5364	0.6182	0.7091	0.7545
12	0.5035	0.5874	0.6783	0.7273
13	0.4835	0.5604	0.6484	0.7033
14	0.4637	0.5385	0.6264	0.6791
15	0.4464	0.5214	0.6036	0.6536
16	0.4294	0.5029	0.5824	0.6353
17	0.4142	0.4877	0.5662	0.6176
18	0.4014	0.4716	0.5501	0.5996
19	0.3912	0.4596	0.5351	0.5842
20	0.3805	0.4466	0.5218	0.5699
21	0.3701	0.4364	0.5091	0.5558
22	0.3608	0.4252	0.4975	0.5438
23	0.3528	0.4160	0.4862	0.5316
24	0.3443	0.4070	0.4757	0.5209
25	0.3369	0.3977	0.4662	0.5108
26	0.3306	0.3901	0.4571	0.5009
27	0.3242	0.3828	0.4487	0.4915
28	0.3180	0.3755	0.4401	0.4828
29	0.3118	0.3685	0.4325	0.4749
30	0.3063	0.3624	0.4251	0.4670

$\alpha_1^R$	5%	21/2%	1%	1/2%
a2	10%	5%	2%	1%
n				
31	0.3012	0.3560	0.4185	0.4593
32	0.2962	0.3504	0.4117	0.4523
33	0.2914	0.3449	0.4054	0.4455
34	0.2871	0.3396	0.3995	0.4390
35	0.2829	0.3347	0.3936	0.4328
36	0.2788	0.3300	0.3882	0.4268
37	0.2748	0.3253	0.3829	0.4211
38	0.2710	0.3209	0.3778	0.4155
39	0.2674	0.3168	0.3729	0.4103
40	0.2640	0.3128	0.3681	0.4051
41	0.2606	0.3087	0.3636	0.4002
42	0.2574	0.3051	0.3594	0.3955
43	0.2543	0.3014	0.3550	0.3908
44	0.2513	0.2978	0.3511	0.3865
45	0.2484	0.2945	0.3470	0.3822
46	0.2456	0.2913	0.3433	0.3781
47	0.2429	0.2880	0.3396	0.3741
48	0.2403	0.2850	0.3361	0.3702
49	0.2378	0.2820	0.3326	0.3664
50	0.2353	0.2791	0.3293	0.3628
51	0.2329	0.2764	0.3260	0.3592
52	0.2307	0.2736	0.3228	0.3558
53	0.2284	0.2710	0.3198	0.3524
54	0.2262	0.2685	0.3168	0.3492
55	0.2242	0.2659	0.3139	0.3460
56	0.2221	0.2636	0.3111	0.3429
57	0.2201	0.2612	0.3083	0.3400
58	0.2181	0.2589	0.3057	0.3370
59	0.2162	0.2567	0.3030	0.3342
60	0.2144	0.2545	0.3005	0.3314

$\alpha_1^R$	5%	2½%	1%	1/2%
α2	10%	5%	2%	1%
n				
61	0.2126	0.2524	0.2980	0.3287
62	0.2108	0.2503	0.2956	0.3260
63	0.2091	0.2483	0.2933	0.3234
64	0.2075	0.2463	0.2910	0.3209
65	0.2058	0.2444	0.2887	0.3185
66	0.2042	0.2425	0.2865	0.3161
67	0.2027	0.2407	0.2844	0.3137
68	0.2012	0.2389	0.2823	0.3114
69	0.1997	0.2372	0.2802	0.3092
70	0.1982	0.2354	0.2782	0.3070
71	0.1968	0.2337	0.2762	0.3048
72	0.1954	0.2321	0.2743	0.3027
73	0.1940	0.2305	0.2724	0.3006
74	0.1927	0.2289	0.2706	0.2986
75	0.1914	0.2274	0.2688	0.2966
76	0.1901	0.2259	0.2670	0.2947
77	0.1888	0.2244	0.2652	0.2928
78	0.1876	0.2229	0.2635	0.2909
79	0.1864	0.2215	0.2619	0.2891
80	0.1852	0.2201	0.2602	0.2872
82	0.1829	0.2174	0.2570	0.2837
84	0.1807	0.2147	0.2539	0.2804
86	0.1785	0.2122	0.2510	0.2771
88	0.1765	0.2097	0.2481	0.2740
90	0.1745	0.2074	0.2453	0.2709
92	0.1725	0.2051	0.2426	0.2680
94	0.1707	0.2029	0.2400	0.2651
96	0.1689	0.2008	0.2375	0.2623
98	0.1671	0.1987	0.2351	0.2597
100	0.1654	0.1967	0.2327	0.2571

For description, see page 35.

### Critical values for Kendall's rank correlation coefficient

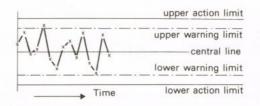
$$\tau = \frac{N_C - N_D}{\frac{1}{2}n(n-1)}$$

$\alpha_1^R$	5%	2%%	1%	1/2%
α <sub>2</sub>	10%	5%	2%	1%
n				
1	-	-	-	-
2	-	_	_	-
3	-	_	-	-
4	1.0000	~	_	-
5	0.8000	1.0000	1.0000	-
6	0.7333	0.8667	0.8667	1.0000
7	0.6190	0.7143	0.8095	0.9048
8	0.5714	0.6429	0.7143	0.7857
9	0.5000	0.5556	0.6667	0.7222
10	0.4667	0.5111	0.6000	0.6444
11	0.4182	0.4909	0.5636	0.6000
12	0.3939	0.4545	0.5455	0.5758
13	0.3590	0.4359	0.5128	0.5641
14	0.3626	0.4066	0.4725	0.5165
15	0.3333	0.3905	0.4667	0.5048
16	0.3167	0.3833	0.4333	0.4833
17	0.3088	0.3676	0.4265	0.4706
18	0.2941	0.3464	0.4118	0.4510
19	0.2865	0.3333	0.3918	0.4386
20	0.2737	0.3263	0.3789	0.4211
21	0.2667	0.3143	0.3714	0.4095
22	0.2641	0.3074	0.3593	0.3939
23	0.2569	0.2964	0.3518	0.3913
24	0.2464	0.2899	0.3406	0.3768
25	0.2400	0.2867	0.3333	0.3667
26	0.2369	0.2800	0.3292	0.3600
27	0.2308	0.2707	0.3219	0.3561
28	0.2275	0.2646	0.3122	0.3439
29	0.2217	0.2611	0.3103	0.3399
30	0.2184	0.2552	0.3011	0.3333

$\alpha_i^R$	5%	2%%	1%	1/2%
α2	10%	5%	2%	1%
n				
31	0.2129	0.2516	0.2946	0.3247
32	0.2097	0.2460	0.2903	0.3226
33	0.2045	0.2424	0.2879	0.3144
34	0.2014	0.2371	0.2799	0.3119
35	0.1966	0.2336	0.2773	0.3042
36	0.1937	0.2317	0.2730	0.3016
37	0.1922	0.2282	0.2673	0.2973
38	0.1892	0.2233	0.2632	0.2916
39	0.1876	0.2200	0.2605	0.2874
40	0.1846	0.2179	0.2564	0.2846
41	0.1805	0.2146	0.2537	0.2805
42	0.1777	0.2125	0.2497	0.2753
43	0.1761	0.2093	0.2470	0.2735
44	0.1734	0.2072	0.2431	0.2685
45	0.1717	0.2040	0.2404	0.2667
46	0.1691	0.2019	0.2386	0.2638
47	0.1674	0.1989	0.2359	0.2599
48	0.1667	0.1968	0.2323	0.2571
49	0.1633	0.1956	0.2296	0.2534
50	0.1624	0.1918	0.2278	0.2506
51	0.1608	0.1906	0.2251	0.2486
52	0.1584	0.1885	0.2232	0.2459
53	0.1567	0.1872	0.2206	0.2438
54	0.1558	0.1852	0.2187	0.2411
55	0.1542	0.1825	0.2162	0.2391
56	0.1519	0.1805	0.2143	0.2364
57	0.1516	0.1792	0.2118	0.2343
58	0.1494	0.1773	0.2099	0.2317
59	0.1479	0.1759	0.2086	0.2297
60	0.1469	0.1740	0.2068	0.2282

$\alpha_1^R$	5%	2%%	1%	1/4%		
α2	10%	5%	2%	1%		
n						
61	0.1454	0.1727	0.2044	0.2262		
62	0.1444	0.1719	0.2025	0.2237		
63	0.1429	0.1705	0.2012	0.2227		
64	0.1419	0.1687	0.1994	0.2202		
65	0.1404	0.1673	0.1981	0.2183		
66	0.1394	0.1655	0.1963	0.2168		
67	0.1389	0.1642	0.1949	0.2148		
68	0.1370	0.1633	0.1932	0.2133		
69	0.1364	0.1620	0.1918	0.2114		
70	0.1354	0.1611	0.1901	0.2099		
71	0.1340	0.1598	0.1887	0.2089		
72	0.1330	0.1581	0.1878	0.2074		
73	0.1324	0.1575	0.1865	0.2055		
74	0.1314	0.1559	0.1847	0.2040		
75	0.1301	0.1553	0.1834	0.2029		
76	0.1291	0.1537	0.1825	0.2014		
77	0.1285	0.1531	0.1811	0.2003		
78	0.1275	0.1515	0.1795	0.1988		
79	0.1269	0.1509	0.1788	0.1970		
80	0.1259	0.1500	0.1772	0.1962		
82	0.1244	0.1478	0.1749	0.1936		
84	0.1228	0.1457	0.1727	0.1910		
86	0.1212	0.1442	0.1710	0.1885		
88	0.1196	0.1426	0.1688	0.1865		
90	0.1186	0.1406	0.1665	0.1845		
92	0.1171	0.1390	0.1648	0.1820		
94	0.1155	0.1375	0.1631	0.1801		
96	0.1145	0.1360	0.1614	0.1785		
98	0.1134	0.1349	0.1597	0.1765		
100	0.1119	0.1333	0.1580	0.1745		

## Control chart constants and conversion factors for estimating $\sigma$



n	W	A	w <sub>1</sub>	W <sub>2</sub>	81	a2	di	d <sub>2</sub>	d <sub>3</sub>	c
2	1.2282	1.9365	0.0393	2.8092	0.0016	4.1241	1.1284	2.0000	1.4142	0.8862
3	0.6686	1.0541	0.1791	2.1756	0.0356	2.9916	1.6926	2.3391	1,9099	0.5908
4	0.4760	0.7505	0.2888	1.9352	0.0969	2.5787	2.0588	2.5803	2.2346	0.4857
5	0.3768	0.5942	0.3653	1.8045	0.1580	2.3577	2,3259	2.7665	2.4744	0.4299
6	0.3157	0.4978	0.4206	1.7207	0.2110	2.2172	2.5344	2.9177	2.6635	0.3946
7	0.2739	0.4319	0.4624	1.6616	0.2556	2.1187	2.7044	3.0448	2.8189	0.3698
8	0.2434	0.3837	0.4952	1.6173	0.2932	2.0451	2.8472	3.1541	2.9504	0.3512
9	0.2200	0.3468	0.5218	1.5826	0.3251	1.9875	2.9700	3.2499	3.0641	0.3367
10	0.2014	0.3175	0.5438	1.5545	0.3524	1.9410	3.0775	3.3352	3.1640	0.3249
11	0.1863	0.2937	0.5624	1.5312	0.3761	1.9024	3.1729	3.4118	3.2531	0.3152
12	0.1736	0.2738	0.5783	1.5115	0.3969	1.8697	3.2585	3.4815	3.3333	0.3069
13	0.1629	0.2569	0.5922	1.4945	0.4152	1.8417	3.3360	3.5452	3.4061	0.2998
14	0.1538	0.2424	0.6044	1.4796	0.4316	1.8172	3.4068	3.6039	3.4728	0.2935
15	0.1458	0.2298	0.6153	1.4666	0.4463	1.7957	3.4718	3.6584	3.5343	0.2880
16	0.1387	0.2187	0.6250	1.4550	0.4596	1.7765	3,5320	3.7091	3.5913	0.2831
17	0.1325	0.2089	0.6338	1.4445	0.4717	1.7592	3.5879	3.7565	3.6443	0.2787
18	0.1269	0.2001	0.6417	1,4351	0.4827	1.7437	3.6401	3.8011	3.6940	0.2747
19	0.1219	0.1922	0.6490	1.4265	0.4928	1.7295	3.6890	3.8430	3.7405	0.2711
20	0.1173	0.1850	0.6557	1.4186	0.5022	1.7165	3.7350	3.8827	3.7844	0.2677

Control charts are designed to aid the regular periodic checking of production and other processes. The situation envisaged is that a quite small sample (the table caters for sample sizes n up to 20) is drawn and examined at regular intervals, and in particular the sample mean  $\overline{X}$  and the sample range R are recorded (the range is the largest value in the sample minus the smallest value).  $\overline{X}$  and R are then plotted on separate control charts to monitor respectively the process average and variability.

The general form of a control chart is illustrated in the diagram. There is a central line representing the expected (i.e. average) value of the quantity  $(\overline{X} \text{ or } R)$  being plotted when the process is behaving normally (is in control). On either side of the central line are warning limits and action limits. These terms are virtually self-explanatory. The levels are such that if an observation falls outside the warning limits the user should be alerted to watch the subsequent behaviour of the process but should also realise that such observations are bound to occur by chance occasionally even when the process is in control. An observation may also fall outside the action limits when the process is in control, but the probability of this is very small and so a more positive alert would normally be signalled. Information can also be obtained by watching for possible trends and other such features on the charts.

The central line and warning and action limits may be derived from studying pilot samples taken when the process is presumed or known to be in control, or alternatively may be fixed by a priori considerations. If they are derived from pilot samples we shall assume that they are of the same size as those to be taken when the control scheme is in operation and that the mean  $\overline{X}$  and range R are calculated for each such sample. These quantities are then averaged over all the pilot samples to obtain  $\overline{\overline{X}}$  and  $\overline{R}$ . We may also calculate, instead of R, either the unadjusted or the adjusted sample standard deviations S or s (see below). The charts are then drawn up as follows:

X-chart	Central line is $\overline{\overline{X}}$ ; lower warning limit is $\overline{\overline{X}} - W\overline{R}$ ; upper warning limit is $\overline{\overline{X}} + W\overline{R}$ ; lower action limit is $\overline{\overline{X}} - A\overline{R}$ ; upper action limit is $\overline{\overline{X}} + A\overline{R}$ .
R-chart	Central line is $\overline{R}$ ; lower warning limit is $w_1\overline{R}$ ; upper warning limit is $w_2\overline{R}$ ; lower action limit is $a_1\overline{R}$ ; upper action limit is $a_2\overline{R}$ .

As an alternative to using pilot samples, specifications of the mean  $\mu$  and/or the standard deviation  $\sigma$  of the process measurements may be used to define the 'in control' situation. If  $\mu$  is given, use it in place of  $\overline{X}$  in drawing up the  $\overline{X}$ -chart. If  $\sigma$  is given, the expected value of R is equal to  $d_1\sigma$ , so here define R as  $d_1\sigma$  and then proceed as above. This application allows an exact interpretation to be made of the warning and action limits, for if the process measurements are normally distributed with mean  $\mu$  and standard deviation  $\sigma$  the warning limits thus obtained correspond

to quantiles q of 0.025 and 0.975 and the action limits to quantiles of 0.001 and 0.999. In other words, the limits can be regarded as critical values for testing the null hypothesis that the data are indeed from a normal distribution with mean  $\mu$  and standard deviation  $\sigma$ , the warning limits corresponding to significance levels of  $\alpha_1 = 2\frac{1}{2}\%$  or  $\alpha_2 = 5\%$  and the action limits to levels of  $\alpha_1 = 0.1\%$  or  $\alpha_2 = 0.2\%$ .

If pilot samples are used it may be that the variability of the process has been measured by recording the sample standard deviations rather than ranges. If the unadjusted sample standard deviation  $S = \left\{ \Sigma (X - \bar{X})^2 / n \right\}^{1/2}$  has been calculated for each pilot sample, average the values of S to obtain  $\bar{S}$ , and then define  $\bar{R} = d_2 \bar{S}$  and proceed as above. Or, if adjusted sample standard deviations  $s = \left\{ \Sigma (X - \bar{X})^2 / (n-1) \right\}^{1/2}$  have been calculated, multiply their average  $\bar{s}$  by  $d_3$  to obtain  $\bar{R} = d_3 \bar{s}$ , and again proceed as above. It should be understood that in general these formulae for  $\bar{R}$  will not give exactly the same value as if  $\bar{R}$  were calculated directly from the pilot samples, but represent the expected value of  $\bar{R}$  given the information available.

For convenience we have also included in this table a column of constants c for forming unbiased estimators of the standard deviation  $\sigma$  from either the range of a single sample or the average range of more than one sample of the same size. Denoting by  $\bar{R}$  the range or average range,  $\sigma$  is estimated by  $c\bar{R}$ .  $\sigma$  may also be estimated from  $\bar{S}$  or  $\bar{s}$  by  $cd_2\bar{S}$  or  $cd_3\bar{s}$  respectively.

EXAMPLES: If samples are of size n=10, and pilot samples have average value of the sample means  $\overline{X}=15.00$  and average range  $\overline{R}=7.00$ , then the  $\overline{X}$ -chart has central line at 15.00, warning limits at 15.00  $\pm$  0.2014  $\times$  7.00, i.e. 13.59 and 16.41, and action limits at 15.00  $\pm$  0.3175  $\times$  7.00, i.e. 12.78 and 17.22; the R-chart has central line at 7.00, warning limits at 0.5438  $\times$  7.00 = 3.81 and 1.5545  $\times$  7.00 = 10.88, and action limits at 0.3524  $\times$  7.00 = 2.47 and 1.9410  $\times$  7.00 = 13.59. The standard deviation  $\sigma$  may be estimated from the pilot samples as  $c\overline{R}=0.3249 \times$  7.00 = 2.27

Alternatively, if the unadjusted sample standard deviations S had been computed instead of ranges, and the average value  $\overline{S}$  of the S-values were  $\overline{S}=2.00$ , we would define  $\overline{R}=d_2\overline{S}=3.3352\times2.00=6.670$ . The reader may confirm that the  $\overline{X}$ -chart would then have central line 15.00, warning limits 13.66 and 16.34, and action limits 12.88 and 17.12; and the R-chart would have central line 6.670, warning limits 3.63 and 10.37, and action limits 2.35 and 12.95. The standard deviation  $\sigma$  could be estimated as  $cd_2\overline{S}=0.3249\times6.670=2.17$ .

Finally if the 'in control' situation is defined by a mean value  $\mu=14.0$  and standard deviation  $\sigma=2.5$ , we define  $\overline{R}=d_1\sigma=3.0775\times2.5=7.694$ , and then obtain an  $\overline{X}$ -chart with central line 14.0, warning limits 12.45 and 15.55, and action limits 11.56 and 16.44; and the R-chart would have central line 7.694, warning limits 4.18 and 11.96, and action limits 2.71 and 14.93.

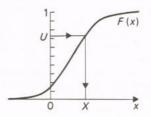
### Random digits

83680 56131 12238 68291 95093 07362 74354 13071 77901 63058 19200 66512 25179 25254 65582 09074 66260 76215 79590 45927																				
1973   1975   1976	02484	88139	31788	35873	63259	99886	20644	41853	41915	02944	82414	59559	41440	22668	37841	70679	62723	50128	30374	90243
0.000   0.00		56131	12238	68291	95093	07362	74354	13071	77901	63058	19200	66512	25179	25254			66260			45927
62040   01912   48847   73952   42147   71784   88894   88904   48901   7175   72827   38915   28150   20206   48568   64247   20206   48568   48247   20206   48268   48268   20206   48268   20206   48268   48268   20206   48268   48268   20206   48268	37336	63266	18632	79781	09184	83909	77232	57571	25413	82680	06125	38600	70556	95945	61968	20673	73403	71431	05563	28155
						88098	75956	85250	05015	99184	82611	23886	16940	24878	51235	37651	76444	45211	98681	33905
1929   1929	62040	01812	46847	79352	42478	71784	65864	84904	48901	17115	85297	33517	26576	23195	12091	45048	01265	90873	55762	74771
1379   1379	96417	63336	88491	73259	21086	51932	32304	45021	61697	73953	89168	81340	50382	30286	84550	59488	95424	31734	02673	45586
2006   2007   2008   2007   2008	42293	29755	24119	62125	33717	20284	55606	33308	51007	68272	39426	52113	93433	45546	68180	72212	84593	85572	80863	65594
	31378	35714	00941	53042	99174	30596	67769	59343	53193	19203	31228	18442	47214	53414	97924	05540	64402	86719	57304	53443
1915   1928   1964   1912   1915   1916	27098	38959	49721	69341	40475	55998	87510	55523	15549	32402	76523	03405	77137	70253	31107	24658	98796	18445	02089	56076
1878   1898   1898   1898   1899   1890	66527	73898	66912	76300	52782	29356	35332	52387	29194	21591	25159	42707	57089	69043	32052	69578	16270	89165	77408	90560
1868   1870   1978   1980   1980   1981   1987   1980   1980   1982   1980	61621	52967	40644	91293	80576	67485	88715	45293	59454	76218	78176	87146	99734	32799	45627	75063	53661	34527	92601	26837
1908-2   2892   51891   0.4007   8800   58004   6733   2853   3768   8524   6734   6734   6745   8451   8585   2432   8460   83041   3331   7481   8575   2332   2857   3780	18798	99633	32948	49802	40261	35555	76229	00486	64236	74782	91613	53259	63858	50229	04979	79377	65502	43457	49356	88489
1.00   1.00	36864	66460	87303	13788	04806	31140	75253	79692	47618	20024	16022	27081	00058	97199	68594	35853	17062	89925	25742	27742
1.02.23   1.02	A Committee of the Comm					58042	67833	23539	37668	16324	97243	03199	45435	45355	24374	84490	83041	03381	74618	90176
92956 04040 51322 04038 34131 34122 21643 90774 08985 26000 94468 63268 27450 91790 09793 08956 04951 23304 46170 53871 93890 04729 57666 0565 24903 42903 6872 49036 27490 24293 68827 67837 087172 40399 9188 85881 39283 43477 91282 34578 91392 381676 68714 58820 24293 68827 68837 08939 38030 27410 98937 98058 58939 381676 81840 48930 24931 48930 24949 27806 91898 47428 18932 90818 3839 381678 58184 151399 81625 64049 24983 68819 39308 81941 815399 816416 815399 816418 815399 816418 815399 816418 816419 81641	20582	49576	91822	63807	99450	18240	70002	75386	26035	21459	74543	48514	68504	04476	80747	64071	03321	29629	37709	73893
	12023	82328	54810	64766	58954	76201	78456	98467	34166	84186	99960	67514	19200	38021	83572	98676	74079	20282	48402	57304
1		20815	51322	04936	33413	43128	21643	90674	98858	26060	64465	63266	27453	91770	99793	25895	98769	42883	10806	69144
94101 21192 00256 81645 48500 73237 95420 9874 39036 21781 51966 12077 46259 07256 94259 34793 57706 8382 54331 50358 20200 44301 96937 886176 80102 48211 61149 71246 19939 73086 8355 55090 94560 40248 94120 93919 77556 5350 94162 20393 02856 91566 64917 91709 79884 44742 18010 11699 47756 97356 98359 34462 98811 96330 45290 21168 10026 79370 17080 94180 18099 9750 18461 42334 06965 28306 1832 83140 13762 17556 18471 9470 18485 18590 94760 94760				100		100000000000000000000000000000000000000			10.00	40399	99188	85861	39263	43477	91282	97590	60951	25330	46710	53871
2004   03117   96937   86176   03102   48211   01149   71246   19993   79708   79708   45745   19101   15199   03194   49218   03194   27860   09166   7333   58398   33462   98611   03304   45280   21681   36707   97804   48192   27263   55390   19199   19199   16841   13199   27652   67308   12973   35609   9750   68528   07839   68528   07839   19101   19199   19199   18641   13199   27652   67308   12973   35609   9750   68528   07839   68528   07839   19101   19109											TOTAL STATE				11869	27637	31443			95214
1800   1800   1800   1801   1801   1800   1801	69101	21192	00256	81645	48500	73237	95420	98974	36036	21781	51966	12077	46259	07825	94235	34793	57776	68352	54531	50358
1862   1864   1869   1866   6917   1870   7884   47742   18071   11899   78736   18399   33462   6881   9033   45280   2188   10928   78737   17080   18184   18199   18793   18199	100000000000000000000000000000000000000					2222					85745	81363	20818	36767	97847	82547	26236	85668	77300	66986
91398   1894   1819   1829   1829   1829   1829   1829   2																01696	07840	48192	27263	55309
6650   6650   6456   4233   6666   2630   6632   6340   1376   1562   6345   6345   6345   6355	100000000000000000000000000000000000000										100000000000000000000000000000000000000				AVEC TO THE					
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82490         86291         27290         55566         65034         40588         63015         06872         56579         25469         85728         37237         40103         50433         59150         84496         42377         53768         52133         68811           85582         09721         32438         88402         69737         3949         82171         18649         83509         85186         14785         42421         19119         0322         69005         2460         08833         55677         7433         1820         29267         78554         96813         1711         51522         22492         78589         89825         5637         60230         33538         81812         97752         47814         90852         5666         69267         17117         45206         69414         6283         3556         69273         78939         9866         67657         1808         26066         6926         78766         6927         78414         90825         5676         9928         78788         89739         98330         5686         67074         4809         68672         69153         6672         81414         28326         68161         2920					1100000						330.353				,,,,,,					
85852         09721         32438         88402         69377         39643         4219         18649         83509         85166         14785         04821         19119         08325         26905         24560         08833         55675         76433         6733           23396         63296         73130         18400         02901         82926         78564         90482         56440         81318         71414         27979         12176         01130         7778         47874         32190         74863         17311         67328           24949         73949         98652         55637         60230         33588         48182         97752         47814         90855         56194         79853         26706         71602         77910         06696         69737         79330         52248         12804         76602         9977         7013         22795         79476         68805         01511         14238         28255         67944         48065         8409         64977         5446         16260         67279         73701         82779         79476         68805         01511         14238         28255         67944         48065         84091         749771	100000000000000000000000000000000000000										100000000000000000000000000000000000000									
28396         63296         73130         18400         02901         82926         78554         90463         25440         81318         71414         27979         12176         01123         07778         47874         32190         74583         17331         67238           59998         50022         98409         5261         50134         26029         67725         44121         23826         89886         67473         72683         31564         16361         56367         62330         3538         48182         97752         47814         90825         23256         69928         59318         87985         78300         86844         93722         61372         7910         00699         66677         36867         62384         93737         9330         22482         41832         17809         96766         62846         96872         65676         62846         96676         62846         91320         04486         12001         1814         25320         77870         13884           24820         17601         76702         86765         61284         17637         64724         76082         84609         64977         54612         246200         66762         62846	100000000000000000000000000000000000000			\$500 E																
59998         60022         98409         54261         60134         26029         67725         44121         23525         88988         57474         72693         31564         16376         54678         62080         22427         41599         98856         66375         31696         26020         33538         48182         97752         47814         90825         22266         62025         33618         67857         31696         23727         41599         00659         32216         62025         33618         67867         31696         23227         47814         90825         22666         26925         33618         37895         78300         68647         46281         22560         63935         246617         68050         16114         23202         78612         46281         22560         63936         16114         23202         77870         13864         46281         22560         64395         56163         3308         78361         17027         00244         6908         68977         74467         24080         69682         67944         48056         56108         68978         48142         24080         68265         67944         48062         69083         88610																				
2492         73949         98852         5637         60230         33538         48182         97752         47814         90855         63265         63925         93818         97895         78380         68844         93722         61372         27910         00695           39349         38886         67457         17930         62248         12804         45281         6260         64395         6461         75644         9821         72866         61940         79833         2298         37983         52248         12804         42821         6260         64395         64681         756461         76864         91320         04486         12011         16114         23232         77873         13884           45307         98424         17664         96768         1289         13413         37732         46527         6150         33008         74354         17027         00244         29018         9133         3803         48128         87028         87141         40150         55090         87847         13795         70104         65742         03616         94083         38651         9721         40203         8803         48162         872730         88071         38208					1,100,000	300000000	AVERAGE OF	217.0715.5			Escale Control				0.0000000000000000000000000000000000000	Parameters.		90 (07770)	200000000000000000000000000000000000000	200000000000000000000000000000000000000
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24828         41532         17809         99677         77013         22795         79476         68805         01511         14238         28255         67944         48065         8609         6977         54467         02416         21482         09980         1422           45307         95424         17664         96788         01289         13413         37732         46527         6156         33008         74354         17027         0244         25018         91737         95362         61323         6363         96118         79751           67512         61553         02595         55806         16182         32048         98061         1924         60659         39606         01572         27300         86075         23908         38819         88918         43049         24210         60559         39566         29923         26807         18533         24684         16924         36640         36650         91842         2901         23736         866269         74366         26259         26865         61605         34344         77662         50397         8281         13541         14238         81164         0425         84545         81612         944134         84545																				
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10959         25440         26269         40889         91641         78868         17601         76567         11357         01088         52233         21106         73798         90942         07779         42685         04186         61471         47687         20726           03784         41838         17267         04927         26719         30540         22557         33603         75689         04266         61592         18588         59135         95029         46711         01496         49891         22452         81489         62136           80949         08395         58909         64448         04736         07373         00130         08352         75058         58561         77656         67493         82480         03507         34742         82955         31274         17994         46276         01606           86038         76897         37132         46059         52260         76989         14728         683207         29811         111127         81957         79526         56240         35007         86620         23703         16099         46252           72451         18449         04444         30225         66543         30362         47162																				
03784         41838         17267         04927         26719         30540         22557         33603         75689         04266         61592         18588         59135         95029         46711         01496         49891         22452         81489         62136           80949         08395         58909         64448         04736         07373         00130         08352         75058         58561         77656         67493         82480         03507         34742         82955         31274         17994         46276         01606           86038         76897         37132         44871         85577         07205         03919         19347         17449         86832         46996         84847         15684         15187         33568         2b105         83358         15947         51285         01570           97916         32882         97441         26397         27173         46059         52260         76989         14728         68207         29811         111127         81957         79526         56240         35007         86620         23703         16099         46252           72451         18449         04444         30225         86543		25440			25038554067															
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72451         18449         04444         30225         86543         30362         47162         45784         29045         26513         76680         75923         79273         43684         96519         86541         10836         10778         08017         82954           12623         20526         27902         28596         69351         73214         67953         43725         71702         07781         99830         83847         18818         94296         60973         57960         91843         86460         93269         35636           13305         23464         16745         59406         10177         27227         47841         74838         65382         63736         47603         65176         20206         25929         51398         80379         75345         50304         60320         31904           78104         00194         87152         34571         74435         35395         18567         65386         93855         40642         01960         26232         19832         04214         61808         92899         24707         22758         18685         56996           13593         59272         95778         69866         72803	97916				200000000000000000000000000000000000000										30-3720-20					AMMINIST TO
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19602 77575 37169 65529 40604   17618 55960 21752 49454 15383   99010 99772 86920 32699 91168   32237 75433 93022 31898 72444					2000					C248-04-04-04-04-04-04-04-04-04-04-04-04-04-					RESERVE ALSO					
	19602	77575	37169	65529	40604	17618	55960	21752	49454	15383	99010	99772	86920	32699	91168	32237	75433	93022	31898	72444

Each digit in the table was generated by a process equally likely to give any one of the ten digits  $0, 1, 2, \ldots, 9$ . The digits have been grouped purely for convenience of reading.

Random digits can be used to simulate random samples from any probability distribution. First note that random numbers U from the continuous uniform distribution on (0:1) can be formed approximately by placing a decimal point in front of groups of, say, five random digits (again for ease of reading), thus: 0.02484, 0.88139, 0.31788, etc. These numbers may in turn be transformed to random numbers X from any continuous distribution with c.d.f. F(x) by solving the equation U = F(X) for X in terms of U — this may be accomplished using a graph of F(x) as

shown in the diagram. Random numbers from discrete distributions may be obtained by a similar graphical process or by finding the smallest X such that F(X) > U.



### Random numbers from normal distributions

					-									
0.5117	-0.6501	-0.0240	-0.0374	0.4650	0.6573	-0.8489	- 1.6237	0.9161	0.4286	2.1530	0.8024	0.6296	- 0.7431	0.2311
0.4219	-0.1946	-0.2223	0.8529	0.3829	1.3436	1.4955	0.5792	-1.1305	-0.3346	- 1.9110	1.4270	-1.7715	0.6190	1.3728
-0.3968	-2.0135	0.3052	1.4541	0.3063	0.0446	-2.1887	-0.2511	0.9978	-0.4531	-0.8269	-1.1302	-0.2418	0.1748	-0.2623
0.4687	-1.4781	-1.7345	0.7693	-0.9250	0.0144	0.7538	0.0476	-0.6648	1.0353	-1.9236	-0.0390	1.7233	-0.3012	-1.2579
0.6956	0.9457	-2.2365	-0.2212	-0.0329	1.3567	-1.0202	-0.6191	-1.5205	-2.4005	0.0528	-0.9080	-0.6263	0.6274	-0.1815
0.3644	1.5510	-0.4803	- 1.0094	0.4757	0.9914	0.5532	-0.7414	0.6996	0.4086	-0.7131	0.5659	0.5726	- 1.0370	0.6656
0.9069	-0.3967	0.6256	0.7654	0.6252	2.1284	1.2576	0.8842	0.3930	0.2474	-0.4700	0.5366	-0.7211	0.4170	-0.0039
-1.1476	-0.2261	-0.4645	0.3763	-1.5602	0.8831	1.4995	-0.5930	0.9010	0.5485	-0.8076	0.0739	1.8341	0.6792	-0.2652
0.6157	1.1829	-1.0711	-0.6905	0.2236	-0.4170	0.6114	0.0493	1.3242	1.0989	- 1.3245	-0.0253	0.3983	1.7539	0.7943
-0.0140	0.3773	-1.0443	0.3281	-0.1657	-0.5163	0.0572	-1.7496	0.6925	-0.9631	2.6746	0.1739	-0.2046	- 1.3770	-2.5394
0.6557	0.4607	-0.1899	1.4323	1.6818	-0.9194	-0.0812	-0.0136	0.5099	0.4716	0.4880	-1.2776	- 0.5492	-0.7707	0.2670
1.2269	2.4441	-2.5492	-0.7248	-1.5706	-0.3898	-0.6462	1.5392	0.4541	-0.2495	-0.5361	-1.2611	0.1790	0.7144	-0.3908
-2.0647	-0.1562	-0.2500	1,2900	1.1793	0.4379	-0.5050	-0.8679	-0.2687	1.0452	-0.5523	1.2387	-1.6821	1.0840	-0.8673
0.2633	1.0436	0.3264	0.1131	-1.9656	0.2444	-0.4575	0.1475	-0.9912	-0.0698	1.4027	-1.4261	-1.3690	1.1719	0.6424
0.1536	-0.2625	-0.4261	0.1458	0.1283	-0.0728	1.0004	0.2144	1.7433	0.4577	-0.7605	-0.8476	-1.1592	3.0920	0.8802
0.0288	0.0438	-0.1742	0.9610	-0.3768	-0.1367	0.0709	0.7607	-1.2500	0.5741	1.6103	-0.1116	-0.3716	- 1,3832	0.8992
-1.8426	-0.3121	-1.0415	0.5305	-0.9029	-0.9628	-0.3619	-0.9187	0.2634	-0.0089	-0.3599	0.8698	1.2590	-1.2478	-0.8828
-0.7422	-0.5728	0.6748	1.9620	-0.0364	0.3374	0.6351	1.7987	-0.0415	0.9141	-0.7215	-0.6227	1.1671	-1.0297	0.5019
-0.8158	1.6473	-2.0569	-0.5147	0.5564	-1.0821	-1.7388	0.0251	-1.3612	-2.2882	0.3054	-1.2463	1.3680	0.1380	1.5723
1.2816	0.4435	0.3760	-0.6307	0.9982	1.9737	-0.1486	0.5829	1.7779	0.8335	-0.4614	0.7387	-0.9224	1.4158	0.4807
0.3257	1.6609	1.5465	1.8711	0.4291	- 0.4098	- 0.9554	0.5928	0.6828	2.8234	0.7119	0.2455	-0.2270	-0.9025	0.1486
-0.5662	0.2938	-1.0305	0.4343	2.1240	1.5033	-0.5762	1.0887	-0.0615	-1.4243	0.9548	-1.2092	-0.1559	0.8749	-0.1916
-0.7432	0.6906	-1.9848	-0.2062	1.5273	1.1176	-0.4626	-1.7566	-0.2784	0.3495	-0.4353	-2.5354	-1.8229	-1.2539	-0.5565
0.0799	0.8198	-1.2491	0.4998	-0.0589	-0.6848	-0.9974	0.8797	-0.0676	1.0889	-0.5973	-3.1585	0.4271	0.6168	2.1738
0.7719	1.2595	-0.1923	-1.8775	1.2376	-0.4795	-0.6284	-0.0667	-0.5308	-0.2933	0.7285	-1.6920	-1.7669	0.5144	-0.5109

These random numbers are from the standard normal distribution, i.e. the normal distribution with mean 0 and standard deviation 1. They may be transformed to random numbers from any other normal distribution with mean  $\mu$  and standard deviation  $\sigma$  by multiplying them by  $\sigma$  and

adding  $\mu$ . For example to obtain a sample from the normal distribution with mean  $\mu=10$  and standard deviation  $\sigma=2$ , double the numbers and add 10, thus:  $2\times(0.5117)+10=11.0234, 2\times(-0.6501)+10=8.6998, 2\times(-0.0240)+10=9.9520$ , etc.

### Random numbers from exponential distributions

0.6193	1.8350	0.2285	1.5106	0.5024	2.3326	4.7123	0.9869	0.7543	0.1759	2.3678	0.1260	1.5913	0.1730	0.5110
0.0354	1.4300	1.6249	0.1402	0.8824	0.9866	0.2289	0.1741	1.3838	0.3772	1.5610	0.1928	0.6389	0.1052	0.4661
0.1258	0.2010	0.2728	0.5152	1.2431	0.3924	1.4429	0.5880	0.0941	1.9999	0.2395	2.6969	1.5680	3.7064	0.0875
2.0308	1.0043	0.1779	0.2475	0.2649	0.2800	5.0992	2.2468	2.2083	0.0988	0.0611	2.2454	0.9630	0.8355	4.0204
0.2145	2.5019	1.3019	1.6369	1,3499	0.6203	1.9118	0.1670	0.1949	1.3440	0.2005	1.5157	1.7353	0.9324	1.3523
1.1118	1.9728	0.6191	0.0149	0.5376	0.0046	0.6752	1.6281	0.2772	0.0556	0.4470	0.5266	0.8817	0.2427	1.1638
0.2432	0.7302	2.4396	0.0779	1.0151	0.4888	1.2114	0.3606	0.0234	1.9367	1.2689	2.1829	0.3569	1.4470	0.9422
0.6834	1.2602	0.0440	3.6550	0.1032	1.5326	4.1297	1.2753	0.1516	0.3470	0.9681	0.4149	1.5600	1.7575	0.5968
0.8743	0.5972	0.5226	0.6086	0.4820	0.8126	0.7244	2.8622	1.2995	0.1391	1.0467	0.3153	0.7654	0.0526	0.6286
1.8945	0.0828	0.6279	0.5823	1.7757	0.1087	0.6876	0.5346	0.6817	0.1436	0.6388	0.6211	0.8468	0.9272	0.8470
1.6711	0.2592	2.1458	0.0449	3.1336	0.5581	0.1607	0.4598	0.7907	0.5938	2.7818	1.8210	1.2763	1.2032	0.0126
0.5536	0.3020	0.2853	1.2290	0.4552	0.0068	1.5726	0.0027	0.0645	0.2775	3.1438	2.9250	0.8723	4.8510	1.2586
0.9866	0.9132	0.3053	0.3737	0.5469	0.0346	2.8317	0.2933	0.7938	0.2877	0.2119	0.8928	2.0636	0.5153	0.8829
1.3695	0.2366	1.7697	1.0209	0.7348	2.3026	0.0673	1.2728	0.5977	5.5840	1.0013	0.4362	0.4095	1.7154	0.0811
0.5208	0.6984	1.0987	0.1917	0.6229	2.1011	0.0072	1.4618	1.1227	0.6920	0.3934	1.3236	0.2127	0.1735	1.0092
2.2593	4.3931	1.4765	0.7746	2.6811	0.0104	0.4500	0.2286	0.1451	0.2324	0.6069	1.2613	1.9487	1.2471	1.3712
1.0490	0.5225	0.2698	0.6562	0.3095	0.7785	0.3197	0.6824	0.3432	0.4526	2.7164	1.0550	0.6933	1.8137	1.7805
0.0518	0.3456	0.1365	0.4320	4.4838	1.1652	0.0927	0.7937	0.0223	1.4675	0.1545	1.4515	0.8765	0.1045	0.2226
0.7941	0.3201	0.0899	1.6611	0.5771	0.2266	0.3686	0.0393	0.8588	0.4303	0.4266	0.3845	0.5723	2.6542	0.6612
0.4676	0.5834	2.3247	0.7372	2.4606	0.3932	0.1851	1.6538	1.7101	1.4550	0.4140	0.0591	0.8581	3.3141	0.4378
0.9766	0.8192	4.1140	0.5508	0.3703	2.3148	0.0545	1.3626	0.3847	2.1840	3.6072	0.1066	0.7252	1.3741	0.8290
1.2443	0.5925	2.2355	0.1753	0.4353	0.7177	3.4943	0.8487	3.9863	2.8398	2.2733	0.4179	0.5265	1.6294	0.4912
0.6793	0.3157	1.6361	0.7469	2.5568	0.2092	0.0555	2.0506	0.1296	1.9426	0.0250	0.9036	1.3022	0.4394	0.6579
0.2690	0.4206	0.9004	2.7633	0.2804	2.7984	2.5987	0.1178	0.5429	1.6306	3.0790	1.1955	0.0738	0.1938	2.0874
0.2610	0.1912	0.3160	1.1692	2.8068	0.2948	0.1969	1.3823	2.1179	0.3821	1.8986	1.3541	0.1657	4.3879	3.3662

These are random numbers from the exponential distribution with mean 1. They may be transformed to random numbers from any other exponential distribution with

mean  $\mu$  simply by multiplying them by  $\mu$ . Thus a sample from the exponential distribution with mean 10 is 6.193, 18.350, 2.285, . . . , etc.

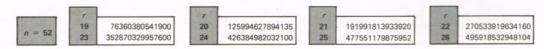
### Binomial coefficients

1	n\	1	( n )	n!	$n(n-1)\ldots(n-r+1)$
1	r	=	$\binom{n-r}{r}$	$= \frac{1}{r!(n-r)!}$	$=\frac{n(n-1)\ldots(n-r+1)}{r(r-1)\ldots 1}$

for n = 1 to 36 and 52 (for playing-card problems)

	0	1	2	3	4	5	6	7	8	9	10	11	4
1	1	1											T
2	1	2	1										
3	1	3	3	1									133
4	1	4	6	4	1								183
5	1	5	10	10	5	1							
6	1	6	15	20	15	6	1					17 9.7	100
7	1	7	21	35	35	21	7	1					188
8	1	8	28	56	70	56	28	8	1				100
9	1	9	36	84	126	126	84	36	9	1			100
10	1	10	45	120	210	252	210	120	45	10	1		
1	1	11	55	165	330	462	462	330	165	55	- 11	1	100
2	1	12	66	220	495	792	924	792	495	220	66	12	100
13	;	13	78	286	715	1287	1716	1716	1287	715	286	78	100
250000	1	14	91	364	1001	2002	3003	3432	3003	2002	2221	364	-
14	1	15	105	455	1365	3003	5005	6435	6435	5005	3003	1365	100
2	-			-		15.000.00.0151			3.000,000,000		With the same of t	700000	
6	1	16	120	560	1820	4368	8008	11440	12870	11440	8008	4368	100
7	1	17	136	680	2380	6188	12376	19448	24310	24310	19448	12376	13
8	1	18	153	816	3060	8568	18564	31824	43758	48620	43758	31824	100
9	1	19	171	969	3876	11628	27132	50388	75582	92378	92378	75582	
0	1	20	190	1140	4845	15504	38760	77520	125970	167960	184756	167960	1
1	1	21	210	1330	5985	20349	54264	116280	203490	293930	352716	352716	100
2	1	22	231	1540	7315	26334	74613	170544	319770	497420	646646	705432	
3	1	23	253	1771	8855	33649	100947	245157	490314	817190	1144066	1352078	100
4	1	24	276	2024	10626	42504	134596	346104	735471	1307504	1961256	2496144	
5	1	25	300	2300	12650	53130	177100	480700	1081575	2042975	3268760	4457400	
6	1	26	325	2600	14950	65780	230230	657800	1562275	3124550	5311735	7726160	
7	1	27	351	2925	17550	80730	296010	888030	2220075	4686825	8436285	13037895	
8	1	28	378	3276	20475	98280	376740	1184040	3108105	6906900	13123110	21474180	100
9	1	29	406	3654	23751	118755	475020	1560780	4292145	10015005	20030010	34597290	
0	1	30	435	4060	27405	142506	593775	2035800	5852925	14307150	30045015	54627300	
1	1	31	465	4495	31465	169911	736281	2629575	7888725	20160075	44352165	84672315	
2	1	32	496	4960	35960	201376	906192	3365856	10518300	28048800	64512240	129024480	100
3	1	33	528	5456	40920	237336	1107568	4272048	13884156	38567100	92561040	193536720	
	1	34	561	5984	46376	278256	1344904	5379616	18156204	52451256	131128140	286097760	
5	1	35	595	6545	52360	324632	1623160	6724520	23535820	70607460	183579396	417225900	
6	1	36	630	7140	58905	376992	1947792	8347680	30260340	94143280	254186856	600805296	
2	1	52	1326	22100	270725	2598960	20358520	133784560	752538150	3679075400	15820024220	60403728840	

\	12	13	14	15	16	17	18	1
12	1							12
13	13	1						13
14	91	14	1					14
15	455	105	15	1	191			15
16	1820	560	120	16	1	A THE		16
17	6188	2380	680	136	17	1		17
18	18564	8568	3060	816	153	18	1	18
19	50388	27132	11628	3876	969	171	19	19
20	125970	77520	38760	15504	4845	1140	190	20
21	293930	203490	116280	54264	20349	5985	1330	21
22	646646	497420	319770	170544	74613	26334	7315	22
23	1352078	1144066	817190	490314	245157	100947	33649	23
24	2704156	2496144	1961256	1307504	735471	346104	134596	24
25	5200300	5200300	4457400	3268760	2042975	1081575	480700	25
26	9657700	10400600	9657700	7726160	5311735	3124550	1562275	26
27	17383860	20058300	20058300	17383860	13037895	8436285	4686825	27
28	30421755	37442160	40116600	37442160	30421755	21474180	13123110	28
29	51895935	67863915	77558760	77558760	67863915	51895935	34597290	29
30	86493225	119759850	145422675	155117520	145422675	119759850	86493225	30
31	141120525	206253075	265182525	300540195	300540195	265182525	206253075	31
32	225792840	347373600	471435600	565722720	601080390	565722720	471435600	32
33	354817320	573166440	818809200	1037158320	1166803110	1166803110	1037158320	33
34	548354040	927983760	1391975640	1855967520	2203961430	2333606220	2203961430	34
35	834451800	1476337800	2319959400	3247943160	4059928950	4537567650	4537567650	35
36	1251677700	2310789600	3796297200	5567902560	7307872110	8597496600	9075135300	36
52	206379406870	635013559600	1768966344600	4481381406320	10363194502115	21945588357420	42671977361650	52



The binomial coefficient  $\binom{n}{r}$  gives the number of different groups of r objects which may be selected from a collection of n objects: e.g. there are  $\binom{4}{2} = 6$  different pairs of letters which may be selected from the four letters A, B, C, D; they are (A,B), (A,C), (A,D), (B,C),

(B,D) and (C,D). The order of selection is presumed immaterial, so (B,A) is regarded as the same as (A,B) etc. As a more substantial example, the number of different hands of five cards which may be dealt from a full pack of 52 cards is  $\binom{52}{5} = 2598960$ .

## Reciprocals, squares, square roots and their reciprocals, and factorials

n	1/n	n <sup>2</sup>	$\sqrt{n}$	√10n	1\v/n	1/√10n	n1
1	1.0000	1	1.0000	3.1623	1.000	.31623	1
2	.50000	4	1.4142	4.4721	.7071	.22361	2
3	.33333	9	1.7321	5.4772	.5774	.18257	6
4	.25000	16	2.0000	6.3246	.5000	.15811	24
5	.20000	25	2,2361	7.0711	.4472	.14142	120
6	.16667	36	2.4495	7.7460	.4082	.12910	720
7	.14286	49	2.6458	8.3666	.3780	.11952	5,040
8	.12500	64	2.8284	8.9443	.3536	.11180	40,320
9	.11111	81	3.0000	9.4868	.3333	.10541	362,880
10	.10000	100	3.1623	10.000	.3162	.10000	3,628,800
11	.09091	121	3.3166	10.488	.3015	.09535	39,916,800
12	.08333	144	3.4641	10.954	.2887	.09129	4.7900 x 10 <sup>8</sup>
13	.07692	169	3.6056	11.402	.2774	.08771	6.2270 × 109
14	.07143	196	3.7417	11.832	.2673	.08452	8.7178 × 10 <sup>10</sup>
15	.06667	225	3.8730	12.247	.2582	.08165	1.3077 x 10 <sup>12</sup>
16	.06250	256	4.0000	12.649	.2500	.07906	2.0923 × 10 <sup>13</sup>
17	.05882	289	4.1231	13.038	.2425	.07670	3.5569 × 10 <sup>14</sup>
18	.05556	324	4.2426	13.416	.2357	.07454	6.4024 × 10 <sup>15</sup>
19	.05263	361	4.3589	13.784	.2294	.07255	1.2165 x 1017
20	.05000	400	4.4721	14.142	.2236	.07071	2.4329 × 10 <sup>18</sup>
21	.04762	441	4.5826	14.491	.2182	.06901	5.1091 x 10 <sup>19</sup>
22	.04545	484	4.6904	14.832	.2132	.06742	1.1240 × 10 <sup>21</sup>
23	.04348	529	4.7958	15.166	.2085	.06594	2.5852 × 10 <sup>22</sup>
24	.04167	576	4.8990	15.492	.2041	.06455	6.2045 x 10 <sup>23</sup>
25	.04000	625	5.0000	15.811	.2000	.06325	1.5511 × 10 <sup>25</sup>
26	.03846	676	5.0990	16.125	.1961	.06202	$4.0329 \times 10^{26}$
27	.03704	729	5.1962	16.432	.1925	.06086	1.0889 × 10 <sup>28</sup>
28	.03571	784	5.2915	16.733	.1890	.05976	3.0489 × 10 <sup>29</sup>
29	.03448	841	5.3852	17.029	.1857	.05872	8.8418 × 10 <sup>30</sup>
30	.03333	900	5.4772	17.321	.1826	.05774	2.6525 × 10 <sup>32</sup>
31	.03226	961	5.5678	17.607	.1796	.05680	8.2228 × 10 <sup>33</sup>
32	.03125	1024	5.6569	17.889	.1768	.05590	2.6313 x 10 <sup>35</sup>
33	.03030	1089	5.7446	18.166	.1741	.05505	8.6833 x 10 <sup>36</sup>
34	.02941	1156	5.8310	18.439	.1715	.05423	2.9523 x 10 <sup>38</sup>
35	.02857	1225	5.9161	18.708	.1690	.05345	1.0333 × 10 <sup>40</sup>
36	.02778	1296	6.0000	18.974	.1667	.05270	$3.7199 \times 10^{41}$
37	.02703	1369	6.0828	19.235	.1644	.05199	1.3764 × 10 <sup>43</sup>
38	.02632	1444	6.1644	19.494	.1622	.05130	5.2302 × 10 <sup>44</sup>
39	.02564	1521	6.2450	19.748	.1601	.05064	2.0398 × 10 <sup>46</sup>
40	.02500	1600	6.3246	20.000	.1581	.05000	8.1592 × 10 <sup>47</sup>
41	.02439	1681	6.4031	20.248	.1562	.04939	3.3453 × 10 <sup>49</sup>
42	.02381	1764	6.4807	20.494	.1543	.04880	1.4050 × 10 <sup>51</sup>
43	.02326	1849	6.5574	20.736	.1525	.04822	6.0415 × 10 <sup>52</sup>
44	.02273	1936	6.6332	20.976	.1508	.04767	2.6583 × 10 <sup>54</sup>
45	.02222	2025	6.7082	21.213	.1491	.04714	1.1962 × 10 <sup>56</sup>
46	.02174	2116	6.7823	21.448	.1474	.04663	5.5026 × 10 <sup>57</sup>
47	.02128	2209	6.8557	21.679	.1459	.04613	2.5862 × 10 <sup>59</sup>
48	.02083	2304	6.9282	21.909	.1443	.04564	1.2414 × 10 <sup>61</sup>
49	.02041	2401	7.0000	22.136	.1429	.04518	6.0828 × 10 <sup>62</sup>
50	.02000	2500	7.0711	22.361	.1414	.04472	3.0414 × 10 <sup>64</sup>

n	1/n	n <sup>2</sup>	$\sqrt{n}$	$\sqrt{10n}$	1/√n	1/√10 <i>n</i>	nl
51	.01961	2601	7.1414	22.583	.1400	.04428	1.5511 × 10 <sup>66</sup>
52	.01923	2704	7.2111	22.804	.1387	.04385	8.0658 × 10 <sup>67</sup>
53	.01887	2809	7.2801	23.022	.1374	.04344	4.2749 × 10 <sup>69</sup>
54	.01852	2916	7.3485	23.238	.1361	.04303	2.3084 × 10 <sup>71</sup>
55	.01818	3025	7.4162	23.452	.1348	.04264	1.2696 × 10 <sup>73</sup>
56	.01786	3136	7.4833	23.664	.1336	.04226	7.1100 × 10 <sup>74</sup>
57	.01754	3249	7.5498	23.875	.1325	.04189	4.0527 × 10 <sup>76</sup>
58	.01724	3364	7.6158	24.083	.1313	.04152	2.3506 × 10 <sup>78</sup>
59	.01695	3481	7.6811	24.290	.1302	.04117	1.3868 × 10 <sup>80</sup>
60	.01667	3600	7.7460	24,495	.1291	.04082	8.3210 × 10 <sup>81</sup>
61	.01639	3721	7.8102	24.698	.1280	.04049	5.0758 × 10 <sup>83</sup>
62	.01613	3844	7.8740	24.900	.1270	.04016	3.1470 × 10 <sup>85</sup>
63	.01587	3969	7.9373	25.100	.1260	.03984	1.9826 × 10 <sup>87</sup>
64	.01563	4096	8.0000	25.298	.1250	.03953	1.2689 × 10 <sup>89</sup>
65	.01538	4225	8.0623	25.495	.1240	.03922	8.2477 × 10 <sup>90</sup>
66	.01515	4356	8.1240	25,690	.1231	.03892	5.4434 × 10 <sup>92</sup>
67	.01493	4489	8.1854	25.884	.1222	.03863	3.6471 × 10 <sup>94</sup>
68	.01471	4624	8.2462	26.077	.1213	.03835	2.4800 × 10 <sup>96</sup>
69	.01449	4761	8.3066	26.268	.1204	.03807	1.7112 × 10 <sup>98</sup>
70	.01429	4900	8.3666	26.458	.1195	.03780	1.1979 × 10 <sup>100</sup>
71	.01408	5041	8.4261	26.646	.1187	.03753	8.5048 × 10 <sup>101</sup>
72	.01389	5184	8.4853	26.833	.1179	.03727	6.1234 × 10 <sup>103</sup>
73	.01370	5329	8.5440	27.019	.1170	.03701	4.4701 × 10 <sup>105</sup>
74	.01351	5476	8.6023	27.203	.1162	.03676	3.3079 × 10 <sup>107</sup>
75	.01333	5625	8.6603	27.386	.1155	.03651	2.4809 × 10 <sup>109</sup>
76	.01316	5776	8.7178	27.568	.1147	.03627	1.8855 × 10 <sup>111</sup>
77	.01299	5929	8.7750	27.749	.1140	.03604	1.4518 × 10 <sup>113</sup>
78	.01282	6084	8.8318	27.928	.1132	.03581	1.1324 × 10 <sup>115</sup>
79	.01266	6241	8.8882	28.107	.1125	.03558	8.9462 × 10 <sup>116</sup>
80	.01250	6400	8.9443	28.284	.1118	.03536	7.1569 × 10 <sup>118</sup>
81	.01235	6561	9.0000	28.460	.1111	.03514	5.7971 × 10 <sup>120</sup>
82	.01220	6724	9.0554	28.636	.1104	.03492	4.7536 × 10 <sup>122</sup>
83	.01205	6889	9.1104	28.810	.1098	.03471	3.9455 × 10 <sup>124</sup>
84	.01190	7056	9.1652	28.983	.1091	.03450	3.3142 × 10 <sup>126</sup>
85	.01176	7225	9.2195	29.155	.1085	.03430	2.8171 × 10 <sup>128</sup>
86	.01163	7396	9.2736	29.326	.1078	.03410	2.4227 × 10 <sup>130</sup>
87	.01149	7569	9.3274	29.496	.1072	.03390	2.1078 × 10 <sup>132</sup>
88	.01136	7744	9.3808	29.665	.1066	.03371	1.8548 × 10 <sup>134</sup>
89	.01124	7921	9.4340	29.833	.1060	.03352	1.6508 × 10 <sup>136</sup>
90	.01111	8100	9.4868	30.000	.1054	.03333	1.4857 × 10 <sup>138</sup>
91	.01099	8281	9.5394	30.166	.1048	.03315	1.3520 × 10 <sup>140</sup>
92	.01087	8464	9.5917	30.332	.1043	.03297	1.2438 x 10 <sup>142</sup>
93	.01075	8649	9.6437	30.496	.1037	.03279	1.1568 x 10 <sup>144</sup>
94	.01064	8836	9.6954	30.659	.1031	.03262	1.0874 × 10 <sup>146</sup>
95	.01053	9025	9.7468	30.822	.1026	.03244	1.0330 × 10 <sup>148</sup>
96	.01042	9216	9.7980	30.984	.1021	.03227	9.9168 × 10 <sup>149</sup>
97	.01031	9409	9.8489	31.145	.1015	.03211	9.6193 x 10 <sup>151</sup>
98	.01020	9604	9.8995	31.305	.1010	.03194	9.4269 x 10 <sup>153</sup>
99	.01010	9801	9.9499	31.464	.1005	.03178	9.3326 x 10 <sup>155</sup>
100	.01000	10000	10.000	31.623	.1000	.03162	9.3326 x 10 <sup>157</sup>

### Useful constants

π	3.14159	26536
$\sqrt{\pi}$	1.77245	38509
е	2.71828	18285
log <sub>e</sub> 10	2.30258	50930
√2	1.41421	35624

1/π	0.31830	98862
1/√π	0.56418	95835
1/e	0.36787	94412
log <sub>10</sub> e	0.43429	44819
1/√2	0.70710	67812

π2	9.86960	44011
$\sqrt{2\pi}$	2.50662	82746
√e	1.64872	12707
log <sub>e</sub> π	1.14472	98858
$\sqrt{3}$	1.73205	08076

1/π²	0.10132 11836
1/√2π	0.39894 22804
1/√e	0.60653 06597
$\log_{10}\pi$	0.49714 98727
1/√3	0.57735 02692

# The negative exponential function: e-x

See	810.00   890.00   910.00   9	18	-		0	c	4		9	7	0	4	,		PR	PROPORTIONAL PARTS	IONA	L PAR			
9800         9804 <th< th=""><th>9800         9804         <th< th=""><th>L</th><th></th><th>-</th><th>7</th><th>2</th><th>7</th><th>0</th><th>0</th><th>,</th><th>00</th><th>5</th><th></th><th>2</th><th>2</th><th>4</th><th>9</th><th>9</th><th>1</th><th>80</th><th>6</th></th<></th></th<>	9800         9804 <th< th=""><th>L</th><th></th><th>-</th><th>7</th><th>2</th><th>7</th><th>0</th><th>0</th><th>,</th><th>00</th><th>5</th><th></th><th>2</th><th>2</th><th>4</th><th>9</th><th>9</th><th>1</th><th>80</th><th>6</th></th<>	L		-	7	2	7	0	0	,	00	5		2	2	4	9	9	1	80	6
8988         8781         8894         8781         8894         8781         8894         8897         8741         8742         8741         8743         8741 <th< td=""><td>  868   888   889   878   8694   867   857   847   858   878   878   874   875   874   875</td><td></td><td>1.0000</td><td>0066</td><td>9802</td><td>9704</td><td>8096</td><td>0</td><td></td><td></td><td>-</td><td></td><td>10</td><td>20</td><td>29</td><td>39</td><td>49</td><td>69</td><td>89</td><td>78</td><td>88</td></th<>	868   888   889   878   8694   867   857   847   858   878   878   874   875   874   875		1.0000	0066	9802	9704	8096	0			-		10	20	29	39	49	69	89	78	88
Heat	Heart   Hear		0.9048	8968	8869	8781	8694	9512	35	9324	9231	9139	0 0	13	28	35	44	23	65	74	79
1,10,	1734   7255   7255						0000	8607	8521	8437	8353	8270	00	17	25	34	42	20	29	67	9/
7334         7261         7180         7190         7191 <th< td=""><td>  1334   7261   7169   7118   7104  </td><td></td><td>0.8187</td><td>8106</td><td>8029</td><td>/945</td><td>1866</td><td>7788</td><td>7711</td><td>7634</td><td>75.60</td><td>7403</td><td>00 00</td><td>16</td><td>24</td><td>32</td><td>40</td><td>48</td><td>299</td><td>2 5</td><td>72</td></th<>	1334   7261   7169   7118   7104		0.8187	8106	8029	/945	1866	7788	7711	7634	75.60	7403	00 00	16	24	32	40	48	299	2 5	72
6005         6440         6871         6871         7 14         21         28         34         41         68         55           6005         6846         6846         6873         6771         7 13         20         28         34         41         68         56           6405         6846         6886         6873         679         6712         6866         6706         6712         19         25         31         37         44         50           6434         4888         8199         6771         3773         4724         4817         686         6706         6706         670         888         689         670         31         37         44         40         40         80         40 </td <td>  6937 6570 6566 6440   6376 6377 6907 6839 6771   7 14 21 29 34 41 68 55 66 65 646 6 647 6576 6313 6250 6188 6126 6 12 19 25 31 37 44 50 44 50 64 64 64 64 64 64 64 64 64 64 64 64 64</td> <td></td> <td>0.7408</td> <td>7334</td> <td>7261</td> <td>7189</td> <td>7118</td> <td>00//</td> <td></td> <td>1001</td> <td>0007</td> <td>1403</td> <td>7</td> <td>12</td> <td>22</td> <td>29</td> <td>36</td> <td>43</td> <td>51</td> <td>58</td> <td>8 8</td>	6937 6570 6566 6440   6376 6377 6907 6839 6771   7 14 21 29 34 41 68 55 66 65 646 6 647 6576 6313 6250 6188 6126 6 12 19 25 31 37 44 50 44 50 64 64 64 64 64 64 64 64 64 64 64 64 64		0.7408	7334	7261	7189	7118	00//		1001	0007	1403	7	12	22	29	36	43	51	58	8 8
6937         6506         6504         6507         6509         6507         6507         6509         6400         7         13         20         26         33         30         46         50         600         6005         5945         6507         6706         6706         6707	6537   6570   6506   6440							7047	7769	6907	6839	6771	7	14	21	28	34	41	48	22	62
Color   Colo	6005   5946   5886   5817   5786   5136   5250   6188   6126   6   12   19   25   31   37   44   50   56   56   56   56   56   56   56		0.6703	6637	6570	6505	6440						7	13	20	26	33	39	46	52	69
6006         5846         5886         5871         5786         5712         5656         5640         6 541         1         23         29         35         40         46           4916         4894         5836         5826         5726         5719         5117         5666         5016         6         1         1         2         2         3         40         46         440	6006         5846         5886         5871         5786         5712         5656         5659         5640         6 12         1         23         29         35         40         46           4916         4838         6526         5726         5720         5171         4524         457         4677							6376	6313	6250	6188	6126	9	12	19	25	31	37	44	20	99
6434         6379         6226         6710         6066         6016         6117         6066         6016         6117         6066         6016         6117         6066         6016         6117         6064         6016         6117         6064         6017         611         61	6434         6379         6279         6172         6774         6764         6016         6117         6064         6016         6117         6064         6016         6117         6064         6016         6117         6064         6016         6117         612         62         31         77         4449 </td <td></td> <td>0.6065</td> <td>6005</td> <td>5945</td> <td>5886</td> <td>5827</td> <td>5769</td> <td>5712</td> <td>5655</td> <td>5599</td> <td>5543</td> <td>9</td> <td>12</td> <td>17</td> <td>23</td> <td>29</td> <td>35</td> <td>40</td> <td>46</td> <td>52</td>		0.6065	6005	5945	5886	5827	5769	5712	5655	5599	5543	9	12	17	23	29	35	40	46	52
4916         4888         48119         4771         4724         4670         4680         4681         4771         4724         4670         4680         4681         4781         4774         4724         4670         4680         4681         471         1724         4274         4274         4274         4274         4274         4279         4178         4107         414         18         21         16         32         38           3842         3866         3466         3490         3466         3190         3104         3078         346         3104         3078         36         10         11         14         17         21         26         26         241         21         14         11         14         14         17         26         22         3882         3982         308	4916         4888         4819         4717         4724         4670         4680         4681         4691         4717         4724         4670         4680         4691         4717         4724         4670         4680         4694         4404         460         4370         4374         4274         4274         4274         4279         4149         4107         414         410         41         19         24         29         34           3842         3866         3466         3490         3466         3190         3781         3104         3073         348         316 <t< td=""><td></td><td>0.5488</td><td>5434</td><td>5379</td><td>5326</td><td>5273</td><td>5220</td><td>5169</td><td>5117</td><td>9909</td><td>5016</td><td>2</td><td>10</td><td>16</td><td>21</td><td>26</td><td>31</td><td>37</td><td>42</td><td>47</td></t<>		0.5488	5434	5379	5326	5273	5220	5169	5117	9909	5016	2	10	16	21	26	31	37	42	47
4449         4340         4350         4317         4274         4224         4100         4341         4101         4360         3340         3362         3791         3752         3716         4         9         11         14         12         25         28           3296         3366         3366         3366         3366         3366         3396         3396         3396         3367         3368         3296         2296         2296         2296         2296         2296         3296         3499         316 </td <td>4449         4404         4350         4317         4724         4224         4109         4148         4107         4 9         11         17         21         26         30           3642         3865         3867         3829         3791         3752         3716         4         9         11         14         17         21         26         37         31           2296         3263         3293         3894         3166         3136         3104         3073         3042         3         6         10         13         16         19         22         26           2286         2266         2367         241         271         241         271         241         271         241         4         9         13         14         17         21         20         22         26         26         9         11         14         17         23         28         27         21         23         26         8         10         13         14         17         11         11         11         11         11         11         11         11         11         11         11         11         11</td> <td></td> <td>0.4966</td> <td>4916</td> <td>4868</td> <td>4819</td> <td>4771</td> <td>4724</td> <td>4677</td> <td>4630</td> <td>4584</td> <td>4538</td> <td>5</td> <td>6</td> <td>14</td> <td>19</td> <td>24</td> <td>28</td> <td>33</td> <td>38</td> <td>43</td>	4449         4404         4350         4317         4724         4224         4109         4148         4107         4 9         11         17         21         26         30           3642         3865         3867         3829         3791         3752         3716         4         9         11         14         17         21         26         37         31           2296         3263         3293         3894         3166         3136         3104         3073         3042         3         6         10         13         16         19         22         26           2286         2266         2367         241         271         241         271         241         271         241         4         9         13         14         17         21         20         22         26         26         9         11         14         17         23         28         27         21         23         26         8         10         13         14         17         11         11         11         11         11         11         11         11         11         11         11         11         11		0.4966	4916	4868	4819	4771	4724	4677	4630	4584	4538	5	6	14	19	24	28	33	38	43
4025         3865         3864         3866         3867         3829         3791         3753         3716         4         8         12         16         19         23         27         31           3862         3866         3867         3856         3490         3466         3780         3782         4         7         11         14         18         21         25         28           2386         2862         2862         2867         2841         2761         2868         2969         11         14         17         20         23           2888         2862         2868         2867         2841         2761         2868         2969         1868         19         11         14         17         20         23           2898         2867         2868         2867         2867         2868         2780         2766         28         1	4025   3986   3946   3906   3867   3829   3791   3753   3716   4 8   12   16   19   23   27   31     3982   3962   3957   3958   3949   3465   3450   3365   349   3   3   6   10   11   14   18   12   12   25   28     2982   2952   2923   2984   2965   2847   2968   2784   2785   3   6   10   11   14   18   19   21     2988   2962   2923   2894   2965   2847   2968   2784   2785   3   6   10   11   14   17   20   23     2441   2417   2417   2418   2782   2269   2752   2269   2752   2784   2785   2785   2784   2785		0,4493	4449	4404	4360	4317	4274	4232	4190	4148	4107	4	6	13	17	21	26	30	8	39
3442         3459         3456         3450         3362         3469         3465         3459         3466         3367         3369         3362         4         7         11         14         18         21         25         25           2826         2263         2230         3186         3156         3157         3104         3073         3042         3         6         10         14         17         25         25           2882         2671         2646         2641         2516         2441         215         26         11         4         17         20         23           2898         2671         2646         2547         2546         2546         2547         2546         2546         2546         2546         2547         2546         2547         2547         2547         2547         2547         2547         2547         2547         2547         2548         2547         2548         2547         2548         2547         2548         2547         2547         2547         2547         2547         2547         2547         2547         2547         2547         2547         2547         2547         2547	3442         3469         3465         3430         3362         3362         3469         3465         3472         3369         3362         4         7         11         14         18         21         25         25           2826         2263         2230         3186         3166         3173         3104         3073         36         9         11         14         17         25		0.4066	4025	3985	3946	3906	3867	3829	3791	3753	3716	4	8	12	16	19	23	27	31	32
3298         3263         3284         3188         3166         3135         3104         3073         3042         3         6         10         11         14         17         20         23           2898         2891         2862         2864         2886         2834         2868         2834         2868         2837         2808         2766         276         276         3         6         9         11         14         17         20         23         2898         2898         2898         10         13         16         19         20         23         2898         2896         2897         2808         2766         289         11         13         16         19         19         10         11         19         14         16         19         19         10         11         19         14         18         11         19         11         13         11         11         13         11         11         13         14         11         2         3         4         6         9         11         1         1         1         1         1         1         1         1         1         1<	2326         2363         2364         2368         2363         3364         2368         2363         3364         2368         2363         3364         2368         2363         2364         2368         2363         2364         2368         2363         2364         2368         2364         2368         2367         2368         2368         2369         2367         2368         2368         2369         2367         2368         2368         2369         2376         2368         2369         2376         2368         2369         2376         2368         2369         2376         2368         2369         2376         2368         2369         2376         2369         2376         2369         2376         2369         2376         2369         2376         2369         2376         2369         2376         2369 <th< td=""><td></td><td>0.3679</td><td>3642</td><td>3606</td><td>3570</td><td>3535</td><td>3499</td><td>3465</td><td>3430</td><td>3336</td><td>3362</td><td>4</td><td>7</td><td>:</td><td>14</td><td>18</td><td>21</td><td>25</td><td>28</td><td>32</td></th<>		0.3679	3642	3606	3570	3535	3499	3465	3430	3336	3362	4	7	:	14	18	21	25	28	32
2982         2984         2886         2894         2886         2897         2989         2778         2789         2789         2789         2789         2789         2889         2887         2884         2886         2887         2884         2887         2881         2582         2884         2887         2884         2887         2884         2887         2884         2887         2884         2887         2884         2887         2884         2882         2884         2882         2884         2882         2884         2882         2884         2882         2884         2882         2884         2882         2884         2882         2884         2882         2884         2885         2884         2885         2884         2885         2884         2885         2884         2885         2884         2885         2884         2885         2884         2885         2884         2885         2884         2885         2884         2885         2884         2885         2884         2885         2885         2886         2885         2885         2885         2886         2885         2885         2885         2885         2885         2885         2885         2885 <th< td=""><td>2982         2984         2886         2894         2886         2894         2886         2894         2886         2894         2886         2894         2886         2894         2886         2894         2886         2894         2886         2894         2886         2894         2886         2894         2886         2894         2886         2894         2886         2894         2886         2894         2886         2894         2882         2894         2882         2894         2882         2894         2882         2894         2882         2894         2882         2894         2882         2894         2894         2882         2894         2894         2895         2894         2894         2895         2894         2895         2894         2895         2894         2895         2894         2895         2894         2895         2895         2894         2895         2895         2894         2895         2895         2895         2895         2895         2895         2895         2895         2895         2895         2895         2895         2895         2895         2895         2895         2895         2895         2896         2896         2896         <th< td=""><td>-</td><td>0.3329</td><td>3296</td><td>3263</td><td>3230</td><td>3198</td><td>3166</td><td>3135</td><td>3104</td><td>3073</td><td>3042</td><td>m</td><td>9</td><td>10</td><td>13</td><td>16</td><td>19</td><td>22</td><td>25</td><td>29</td></th<></td></th<>	2982         2984         2886         2894         2886         2894         2886         2894         2886         2894         2886         2894         2886         2894         2886         2894         2886         2894         2886         2894         2886         2894         2886         2894         2886         2894         2886         2894         2886         2894         2886         2894         2886         2894         2882         2894         2882         2894         2882         2894         2882         2894         2882         2894         2882         2894         2882         2894         2894         2882         2894         2894         2895         2894         2894         2895         2894         2895         2894         2895         2894         2895         2894         2895         2894         2895         2895         2894         2895         2895         2894         2895         2895         2895         2895         2895         2895         2895         2895         2895         2895         2895         2895         2895         2895         2895         2895         2895         2895         2896         2896         2896 <th< td=""><td>-</td><td>0.3329</td><td>3296</td><td>3263</td><td>3230</td><td>3198</td><td>3166</td><td>3135</td><td>3104</td><td>3073</td><td>3042</td><td>m</td><td>9</td><td>10</td><td>13</td><td>16</td><td>19</td><td>22</td><td>25</td><td>29</td></th<>	-	0.3329	3296	3263	3230	3198	3166	3135	3104	3073	3042	m	9	10	13	16	19	22	25	29
2441         2456         2561         2562         2567         2561         2561         2561         2561         2561         2562         2567         2561         2561         2561         2562         2562         2563         2576         2564         26         8         10         13         16         19           2009         2187         2166         2144         2122         2101         2000         2000         2000         2         4         6         8         10         12         14         16         1         13         15         15         1         2         3         4         6         8         1         1         1         1         1         1         1         1         1 <td>2688         2671         2646         2681         2682         2681         2782         2268         2787         2841         2341         2342         2362         2367         2841         2546         2249         2376         2269         2276         2269         2276         2269         2376         2342         2369         2346         2322         2299         2276         2341         182         182         182         183         182         182         183         182         184         188         &lt;</td> <td></td> <td>0.3012</td> <td>2982</td> <td>2962</td> <td>2923</td> <td>2894</td> <td>2865</td> <td>2837</td> <td>2808</td> <td>2780</td> <td>2753</td> <td>3</td> <td>9</td> <td>6</td> <td>11</td> <td>14</td> <td>17</td> <td>20</td> <td>23</td> <td>26</td>	2688         2671         2646         2681         2682         2681         2782         2268         2787         2841         2341         2342         2362         2367         2841         2546         2249         2376         2269         2276         2269         2276         2269         2376         2342         2369         2346         2322         2299         2276         2341         182         182         182         183         182         182         183         182         184         188         <		0.3012	2982	2962	2923	2894	2865	2837	2808	2780	2753	3	9	6	11	14	17	20	23	26
2441         2417         2393         2366         2346         2322         2299         2276         2254         2         5         7         9         12         14         16         19           2209         2187         2165         2144         2122         2101         2080         2060         2039         2         4         6         9         11         13         15           1899         1940         1791         1773         1765         1781         1703         1886         1670         2         4         6         9         11         13         15         14         19         10         12         14         19         10         12         14         19         10         12         14         19         10         12         14         19         10         12         14         14         13         13         14         14         15         15         15         15         15         14         14         13         14         14         14         13         14         14         14         14         14         14         14         14         14         14         14<	2441         2417         2393         2366         2346         2322         2299         2276         2254         2         5         7         9         10         11         16         19           2209         1887         2187         2165         144         2122         2101         2080         2060         2039         2         4         6         9         11         13         15         17           1989         1791         1775         1756         1738         1736         1861         1865         16         9         10         12         14           1899         1791         1775         1567         1541         1526         1511         2         3         5         6         9         11         13         15         17         14         17         14         17         14         17         16         17         17         17         17         17         17         17         17         17         17         17         17         17         17         17         17         17         17         17         18         18         18         18         18         18		0.2725	2698	2671	2645	2618	2592	2567	2541	2516	2491	e	2	80	10	13	16	18	21	23
2209         1180         1180         200         200         203         2         4         6         9         11         13         15         17           1999         1991         1940         1920         1901         1882         1864         1845         2         4         6         9         11         13         15         17           1987         1791         1791         1970         1901         1882         1864         1845         2         4         6         8         10         12         14         14         14         15         1572         1501         1882         1864         1866         160         9         11         13         15         17         16         11         13         18         1409         190         10         11         11         13         14         14         1409         1386         1381         1367         17         18         14         18         14         1         1         2         4         6         7         9         10         11         11         13         11         13         11         13         14         4         6 </td <td>2209         1180         1212         2101         2080         2060         2039         2         4         6         9         11         13         15         17           1999         1991         1940         1901         1882         1864         1845         2         4         6         8         10         12         13         15         17         1901         1882         1864         1806         1601         1801         1882         1864         1806         1601         1801         1882         1864         1806         1601         1801</td> <td></td> <td>0.2466</td> <td>2441</td> <td>2417</td> <td>2393</td> <td>2369</td> <td>2346</td> <td>2322</td> <td>2299</td> <td>2276</td> <td>2254</td> <td>2</td> <td>2</td> <td>7</td> <td>6</td> <td>12</td> <td>14</td> <td>16</td> <td>19</td> <td>21</td>	2209         1180         1212         2101         2080         2060         2039         2         4         6         9         11         13         15         17           1999         1991         1940         1901         1882         1864         1845         2         4         6         8         10         12         13         15         17         1901         1882         1864         1806         1601         1801         1882         1864         1806         1601         1801         1882         1864         1806         1601         1801		0.2466	2441	2417	2393	2369	2346	2322	2299	2276	2254	2	2	7	6	12	14	16	19	21
1999         1979         1959         1940         1920         1901         1882         1864         1845         2         4         6         8         10         12         13         15           1899         1979         1971         1773         1862         1804         187         173         188         1720         1703         1868         187         1         2         3         5         7         9         10         11         1481         1467         1468         1472         1472         1575         1541         1526         1518         1472         157 <td>1999         1979         1959         1940         1920         1901         1882         1864         1845         2         4         6         8         10         12         13         15           1899         1979         1973         1959         1970         1973         1886         1846         1         2         3         5         7         9         10         12         14           1481         1467         1620         1620         1541         1526         1511         3         4         6         7         9         10         11         13           1481         1466         1451         1472         1526         1518         1381         1367         1         3         4         6         7         9         10         11         11         13         11         13         11         13         11         13         14&lt;</td> <td></td> <td>0.2231</td> <td>2209</td> <td>2187</td> <td>2165</td> <td>2144</td> <td>2122</td> <td>2101</td> <td>2080</td> <td>2060</td> <td>2039</td> <td>2</td> <td>4</td> <td>9</td> <td>6</td> <td>=</td> <td>13</td> <td>15</td> <td>17</td> <td>19</td>	1999         1979         1959         1940         1920         1901         1882         1864         1845         2         4         6         8         10         12         13         15           1899         1979         1973         1959         1970         1973         1886         1846         1         2         3         5         7         9         10         12         14           1481         1467         1620         1620         1541         1526         1511         3         4         6         7         9         10         11         13           1481         1466         1451         1472         1526         1518         1381         1367         1         3         4         6         7         9         10         11         11         13         11         13         11         13         11         13         14<		0.2231	2209	2187	2165	2144	2122	2101	2080	2060	2039	2	4	9	6	=	13	15	17	19
1630         1791         1773         1756         1738         1750         1703         1686         1670         2         3         5         6         8         10         12         14           1481         1462         1620         1604         1586         152         157         1451         156         18         9         10         11         13         4         6         8         9         10         11         13         4         6         8         9         10         11         13         14         6         8         9         10         11         13         4         6         6         8         9         10         11         13         14         13         14         13         14	1630   1791   1773   1756   1738   1750   1703   1686   1670   2 3 5 5 6 8 9 10   12 144   1481   1486   1481   1437   1432		0.2019	1999	1979	1959	1940	1920	1901	1882	1864	1845	2	4	9	80	10	12	13	15	17
1437         1820         1604         1588         1572         1567         1541         1526         1511         13         1         13         1486         1457         1466         1469         1381         1367         1367         1541         1526         1381         1367         1468         1467         1468         1381         1367         1468         1381         1367         1468         1381         1367         1423         1440         1367         1448         1448         1442         1441         1367         1448         1448         1448         1442         1448         1448         1449         1448         1448         1449         1444 </td <td>1487         1820         1694         1588         1572         1567         1541         1526         1511         2         3         6         8         9         11         13         1481         1466         1451         1423         1469         1381         1361         1361         1381         1367         1469         1386         1381         1367         1469         1462         1429         1275         1429         1275         1469         1381         1367         1469         1381         1367         1469         1861         1381         1377         146         172         146         166         7         9         10         11         1         2         6         6         7         9         10         11         1         2         6         6         7         9         10         11         11         13         14</td> <td></td> <td>0.1827</td> <td>1809</td> <td>1791</td> <td>1773</td> <td>1755</td> <td>1738</td> <td>1720</td> <td>1703</td> <td>1686</td> <td>1670</td> <td>2</td> <td>e</td> <td>2</td> <td>7</td> <td>6</td> <td>10</td> <td>12</td> <td>14</td> <td>16</td>	1487         1820         1694         1588         1572         1567         1541         1526         1511         2         3         6         8         9         11         13         1481         1466         1451         1423         1469         1381         1361         1361         1381         1367         1469         1386         1381         1367         1469         1462         1429         1275         1429         1275         1469         1381         1367         1469         1381         1367         1469         1861         1381         1377         146         172         146         166         7         9         10         11         1         2         6         6         7         9         10         11         1         2         6         6         7         9         10         11         11         13         14		0.1827	1809	1791	1773	1755	1738	1720	1703	1686	1670	2	e	2	7	6	10	12	14	16
1481   1466   1451   1437   1423   1409   1395   1381   1387   1   3   4   6   7   9   10   11   11   11   11   12   1300   1787   1275   1262   1249   1237   1   3   4   6   7   9   10   11   11   12   1300   1787   1275   1262   1249   1237   1   3   4   6   6   6   8   9   10   11   12   1300   1388   1388   1398   13	1461   1466   1451   1437   1423   1409   1395   1381   1367   1   3   4   6   7   9   10   11   11   11   11   11   11		0.1653	1637	1620	1604	1588	1572	1557	1541	1526	1511	2	m	S	9	80	6	Ξ	13	14
1340   1327   1313   1300   1287   1275   1262   1249   1237   1 3 4 5 6 8 8 9 10 10 10 11 12   1700   1188   1177   1165   1152   1130   1119   1 1 2 4 5 6 8 7 8 9 10 10 10 10 10 10 10 10 10 10 10 10 10	1340   1327   1313   1300   1287   1275   1262   1249   1237   1 3 4 5 6 6 8 9 10 10 10 11 12   1300   1388   1177   1165   1152   1130   1119   1 2 4 5 6 6 7 8 9 10 10 10 10 10 10 10 10 10 10 10 10 10		0.1496	1481	1466	1451	1437	1423	1409	1395	1381	1367	-	3	4	9	7	6	10	=	13
1037         1188         1177         1165         1153         1142         1130         1119         1         2         4         5         6         7         8         9           1097         1086         1056         1054         1044         1033         1033         113         2         3         4         5         6         7         8         9           0993         0983         0983         0984         0944         0944         0846         0846         0847         0846         0847         0846         0847         0846         0847         0846         0849         0878         0773         0768         0778         0778         0778         0778         0778         0778         0769         0879         0789         0779         0778         0778         0769         0789         0779         0779         0769         0769         0769         0769         0769         0779         0769         0767         0769         0769         0769         0769         0769         0769         0769         0769         0769         0769         0769         0769         0769         0769         0769         0769         0769	1037         1188         1177         1165         1153         1142         1130         1119         1         2         4         5         6         7         8         9         1           0993         10983         10983         10983         10983         10933         1033         11         2         3         4         5         6         7         8         9           0993         0983         0983         0984         0944         0846         0846         0849         0846         0849         0849         0859         0859         0859         0859         0859         0878         0750         0741         0773         0766         0789         0750         1         2         3         4         5         6         7         8         9         9           0645         0787         0781         0773         0766         0780         0750         1         1         2         3         4         6         7         8         9         9         9         9         9         9         9         9         9         9         9         9         9         9         9         9		0.1353	1340	1327	1313	1300	1287	1275	1262	1249	1237	-	3	4	5	9	80	6	10	12
1097         1086         1075         1066         1054         1044         1033         1073         1013         11         2         3         4         5         6         7         8           0989         0889         0889         0884         0895         0844         0846         0845         0846         0847         0846         0849         0846         0847         0846         0847         0846         0849         084	1087         1086         1075         1066         1054         1044         1033         1073         1013         1         2         3         4         6         7         8           0989         0889         0889         0889         0894         0894         0894         0895         0896         0896         0897         8         4         6         7         8           0813         0889         0889         0896         0897         0781         0773         0786         0786         0789         0789         0879         1         2         3         4         6         7         8           06813         0728         0721         0774         0899         0693         0686         0799         1         2         2         3         4         6         7         8           0685         0580         0589         0683         0687         0670         0699         0693         0686         0799         1         1         2         2         3         4         4         6         7         8           0685         0599         0693         0693         0693         0686		0.1225	1212	1200	1188	1177	1165	1153	1142	1130	1119	-	2	4	2	9	7	8	6	10
0983         09843         09973         09663         09644         0944         09456         09496         0949         0949         0949         0949         0944         0946         0849         0949         0949         0949         0949         0949         0949         0949         0949         0949         0949         0970         0899         0969	0983         0984         0995         0944         0955         0956         0946         0944         0956         0949         074         0849         0744         0846         0850         0959         1         2         3         4         5         6         7         8           0681         0880         0890         0797         0794         0846         0787         0750         1         2         3         4         4         6         7         8           0735         0728         0772         0797         0899         0787         0890         0893         0880         0893         0896         0787         4         4         4         6         6         7         8           0665         0659         0592         0646         0693         0683         0687         0661         1         1         2         3         4         4         6         6         7         8           0665         0659         0593         0687         0667         0661         0660         0663         1         1         1         2         3         4         4         6         6		0.1108	1097	1086	1075	1065	1054	1044	1033	1023	1013	-	2	3	4	2	9	1	80	6
0818         082 <td>0898         0890         0872         0863         0854         0846         0837         0829         1         2         3         4         5         6         7           0813         0805         0797         0798         0781         0773         0765         0786         0750         1         2         3         4         5         6         6         7           0735         0724         0797         0899         0829         0850         0679         1         1         2         2         3         4         5         6         6         6         6         7         9         6         6         6         6         6         6         7         8         6         6         6         6         6         6         6         6         6         6         6         6         6         7         8         6         6         7         8         6         6         6         7         8         7         8         6         6         6         7         8         7         8         6         6         7         8         7         8         7         8</td> <td></td> <td>0.1003</td> <td>0993</td> <td>0983</td> <td>0973</td> <td>0963</td> <td>0954</td> <td>0944</td> <td>0935</td> <td>0926</td> <td>9160</td> <td>-</td> <td>2</td> <td>3</td> <td>4</td> <td>2</td> <td>9</td> <td>7</td> <td>00</td> <td>6</td>	0898         0890         0872         0863         0854         0846         0837         0829         1         2         3         4         5         6         7           0813         0805         0797         0798         0781         0773         0765         0786         0750         1         2         3         4         5         6         6         7           0735         0724         0797         0899         0829         0850         0679         1         1         2         2         3         4         5         6         6         6         6         7         9         6         6         6         6         6         6         7         8         6         6         6         6         6         6         6         6         6         6         6         6         6         7         8         6         6         7         8         6         6         6         7         8         7         8         6         6         6         7         8         7         8         6         6         7         8         7         8         7         8		0.1003	0993	0983	0973	0963	0954	0944	0935	0926	9160	-	2	3	4	2	9	7	00	6
0813         0805         0797         0789         0781         0773         0766         0768         0759         1         2         2         3         4         5         6           0665         0653         0523         0533         0633         0689         0699         1         2         2         3         4         5         6           0665         0659         0659         0633         0633         0633         0634         1         1         2         3         4         4         5         6           0602         0569         0659         0633         0686         0667         1         1         2         2         3         4         4         5         6           0645         0639         0636         0646         0647         0640         0646         0647         0741         1         2         2         3         4         4         5         6           0440         0480         0484         0460         0464         0460         0464         0460         0463         0474         0460         0464         0460         0464         0460         0464 <th< td=""><td>0813         0805         0797         0789         0781         0773         0766         0766         0769         071         2         2         3         4         6         6           0665         0653         0721         0794         0899         0693         0689         0679         1         2         2         3         4         6         6           0665         0665         0663         0678         0573         0673         0667         0670         1         1         2         3         4         6         6           0645         0659         0684         0678         0673         0667         0667         1         1         2         2         3         4         6         6           0645         0630         0684         0678         0673         0667         0667         0670         0671         1         1         2         2         3         4         4         5         6           0442         0442         0442         0443         0443         0443         0446         0446         0446         0446         0446         0446         0446         0446</td><td>-27</td><td>0.0907</td><td>8680</td><td>6880</td><td>0880</td><td>0872</td><td>0863</td><td>0854</td><td>0846</td><td>0837</td><td>0829</td><td>-</td><td>2</td><td>69</td><td>m</td><td>4</td><td>10</td><td>9</td><td>1</td><td>00</td></th<>	0813         0805         0797         0789         0781         0773         0766         0766         0769         071         2         2         3         4         6         6           0665         0653         0721         0794         0899         0693         0689         0679         1         2         2         3         4         6         6           0665         0665         0663         0678         0573         0673         0667         0670         1         1         2         3         4         6         6           0645         0659         0684         0678         0673         0667         0667         1         1         2         2         3         4         6         6           0645         0630         0684         0678         0673         0667         0667         0670         0671         1         1         2         2         3         4         4         5         6           0442         0442         0442         0443         0443         0443         0446         0446         0446         0446         0446         0446         0446         0446	-27	0.0907	8680	6880	0880	0872	0863	0854	0846	0837	0829	-	2	69	m	4	10	9	1	00
0.935         0.728         0.721         0.744         0.707         0.689         0.683         0.686         0.679         1         1         2         3         4         4         5         6           0.665         0.656         0.654         0.633         0.623         0.637         0.657         0.640         0.640         0.644         1         1         2         3         3         4         4         5         6           0.645         0.659         0.653         0.651         0.651         0.667         0.641         1         1         2         2         3         3         4         4         5         6           0.645         0.659         0.653         0.651         0.667         0.667         0.667         1         1         2         2         3         3         4         4         5         6           0.483         0.648         0.648         0.646         0.667         0.646         0.646         0.646         0.646         0.646         0.646         0.646         0.646         0.646         0.646         0.646         0.646         0.646         0.646         0.646         0.646         0.	0735         0728         0721         0707         0899         0693         0686         0679         1         1         2         3         4         4         5         6           0665         0665         0662         0663         0673         0673         0673         0673         0673         0673         0673         0673         0674         1         1         2         3         3         4         4         5         6           0645         0659         0684         0673         0673         0673         0673         1         1         2         2         3         3         4         4         6           0445         0486         0687         0673         0673         0673         071         1         1         2         2         3         3         4         4         6         6           0446         0478         0673         0674         0476         0476         0476         0476         0476         0477         07         1         1         2         2         3         3         4         4         6         6         07         1         1         1	-	0.0821	0813	0805	1610	6820	0781	0773	0765	0758	0220	-	2	2	m	4	15	25	9	7
0665         0659         0652         0646         0639         0633         0627         0620         0614         1         2         3         3         4         6           0626         0659         0659         0657         0657         0657         0657         0656         1         1         2         2         3         4         6           0646         0659         0530         0561         0667         0667         0667         0667         0667         0667         0667         0667         0667         0667         0667         0667         0668	Q665         O659         O652         O646         O639         G637         O627         O620         O614         1         2         3         3         4         6           O607         O669         O659         O657         O667         O667         O667         O667         O667         O668         C6         2         3         3         4         6           O446         O653         O653         O667         O667         O667         O669         O668         O67         3         3         3         4         4         6           O446         O429         O629         O424         O420         O464         O460         O466         O466         O676         O         1         1         2         2         3         3         4         4         6           O446         O440         O429         O444         O460         O466         O466 <td></td> <td>0.0743</td> <td>0735</td> <td>0728</td> <td>0721</td> <td>0714</td> <td>0707</td> <td>6690</td> <td>2690</td> <td>9890</td> <td>6290</td> <td>-</td> <td>-</td> <td>2</td> <td>m</td> <td>4</td> <td>4</td> <td>2</td> <td>9</td> <td>9</td>		0.0743	0735	0728	0721	0714	0707	6690	2690	9890	6290	-	-	2	m	4	4	2	9	9
0652 0596 0594 0678 0573 0567 0561 0565 1 1 1 2 2 2 3 3 4 4 5 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6	0652 0596 0594 0678 0573 0567 0561 0565 1 1 1 2 2 2 3 3 4 4 5 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6		0.0672	9990	6990	0652	0646	0639	0633	0627	0620	0614	-	-	2	m	es	4	4	9	9
0445 0634 0634 0629 0623 0518 0613 0608 0603 1 1 2 2 3 3 4 4 4 4 4 0490 0482 0483 0478 0494 0460 0465 0465 041 041 0 2 2 3 3 3 4 4 4 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0445 0539 0534 0529 0523 0518 0513 0508 0503 1 1 2 2 3 3 4 4 4 4 4 0440 0482 0437 0432 0437 0432 0437 0433 0429 0444 0460 0465 0465 041 041 041 041 041 041 041 041 041 041	900	0.0608	0602	9690	0690	0584	0578	0573	0567	0561	9990	-	-	2	2	m	e	4	2	15
0493         0488         0487         0478         0469         0464         0460         0455         0         1         1         2         2         3         3         4           0404         0445         0447         0469         0446         0460         0467         0         1         1         2         2         3         3         4           0404         0400         0386         0384         0420         0416         0412         0         1         1         2         2         2         3         3         3           0366         0386         0384         0361         0347         0344         0340         0343         0         1         1         2         2         2         3         3         3           0396         0387         0324         0347         0344         0340         0337         0         1         1         2         2         2         3	0493         0488         0483         0478         0474         0469         0464         0460         0465         0         1         1         2         2         3         3         4           0446         0442         0432         0432         0432         0432         0434         0420         0416         0412         0         1         1         2         2         3         3         4           0440         0432         0429         0424         0420         0316         0317         0         1         1         2         2         3	4	0.0550	0545	0539	0534	0529	0623	0518	0513	8090	0503	-	-	2	2	m	8	4	4	5
0446         0442         0437         0433         0429         0424         0420         0416         0412         0         1         1         2         2         3         3         3         3           0404         0400         0396         0392         0384         0384         03876         0375         0         1         1         2         2         2         3         3         3           0350         0324         0384         0384         0344         0344         0344         0344         0344         0341         1         1         2         2         2         3         3         3           0330         0324         0334         0344         0344         0344         0344         0341         1         1         1         2         2         2         3         3         3           0326         0326         0347         0344         0346         0356         0356         0356         0356         0356         0356         0356         0356         0356         0356         0356         0356         0356         0356         0356         0356         0356         0356         0356<	0.446	789	0.0498	0493	0488	0483	0478	0474	0469	0464	0460	0455	0	-	-	2	2	3	3	4	4
0404   0400   0396   0398   0384   0389   0376   0373   0   1   2   2   2   2   3   3   3   3   3   3	0404 0400 0396 0398 0384 0381 0387 0380 0376 0373 0 1 1 2 2 2 2 3 3 3 3 0 0365 0385 0386 0384 0381 0387 0344 0340 0337 0 1 1 1 2 2 2 2 3 3 0 037 0320 0327 0324 0321 0347 0344 0340 0331 0311 0308 0305 0 1 1 1 1 2 2 2 2 3 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	SSC.	0.0450	0446	0445	0437	0433	0429	0424	0420	0416	0412	0	-	-	2	2	es	3	es	4
Q365         Q386         Q386         Q356         Q356         Q356         Q356         Q356         Q356         Q357         Q344         Q340         Q337         Q         1         1         2         2         2         3           Q330         Q326         Q327         Q346         Q321         Q366         Q367         Q366         Q376         Q37         Q	Q386         Q387         Q384         Q384         Q384         Q384         Q384         Q386         Q386         Q386         Q387         Q384         Q381         Q386         Q386         Q387         Q384         Q386         Q386 <th< td=""><td></td><td>0.0408</td><td>0404</td><td>0400</td><td>9620</td><td>0392</td><td>0388</td><td>0384</td><td>0380</td><td>0376</td><td>0373</td><td>0</td><td>-</td><td>-</td><td>2</td><td>2</td><td>2</td><td>3</td><td>en</td><td>e</td></th<>		0.0408	0404	0400	9620	0392	0388	0384	0380	0376	0373	0	-	-	2	2	2	3	en	e
0330 0327 0324 0321 0317 0314 0311 0308 0305 0 1 1 1 2 2 2 2 3 3 0299 0296 0296 0296 0298 0298 0287 0287 0287 0282 0279 0275 0 0 1 1 1 1 2 2 2 2 2 0 0271 0286 0285 0285 0285 0285 0285 0285 0285 0285	0330         0327         0324         0321         0317         0314         0311         0308         0305         0         1         1         2         2         3         3           0299         0296         0267         0284         0282         0279         0276         0         1         1         1         2         1 <td< td=""><td></td><td>0.0369</td><td>0365</td><td>0362</td><td>0358</td><td>0354</td><td>0351</td><td>0347</td><td>0344</td><td>0340</td><td>0337</td><td>0</td><td>-</td><td>-</td><td>-</td><td>2</td><td>2</td><td>2</td><td>3</td><td>63</td></td<>		0.0369	0365	0362	0358	0354	0351	0347	0344	0340	0337	0	-	-	-	2	2	2	3	63
0299         0296         U.293         0280         0284         0282         0287         0284         0282         0287         0284         0287         0289         0287         0286         0287         0286         0287         0286         0287         0286         0287         0286         0287         0286         0287         0286         0287         0286         0287         0286         0287         0286         0287         0286         0287         0286         0287         0286         0287         0286         0287         0286         0287         0286         0287         0286         0287         0286         0287         0287         0288         0287 <t< td=""><td>0299         0296         0.293         0290         0287         0284         0282         0279         0275         0         1         1         1         2         1</td><td>59</td><td>0.0334</td><td>0330</td><td>0327</td><td>0324</td><td>0321</td><td>0317</td><td>0314</td><td>0311</td><td>0308</td><td>9000</td><td>0</td><td>-</td><td>-</td><td>-</td><td>2</td><td>2</td><td>7</td><td>3</td><td>65</td></t<>	0299         0296         0.293         0290         0287         0284         0282         0279         0275         0         1         1         1         2         1	59	0.0334	0330	0327	0324	0321	0317	0314	0311	0308	9000	0	-	-	-	2	2	7	3	65
0271 0268 0265 0263 0260 0267 0255 0252 0250 0 1 1 1 1 2 2 2 2 0240 0248 0242 0240 0238 0238 0233 0231 0229 0207 0204 0 0 1 1 1 1 1 1 2 2 0 0221 0219 0217 0219 0217 0219 0191 0119 0187 0185 0 0 1 1 1 1 1 1 1 2 0 000 0198 0196 0194 0193 0191 0199 0187 0198 0197 0198 0198 0198 0198 0198 0198 0198 0198	Q271         Q268         Q265         Q267         Q265         Q266         Q276         Q276 <td< td=""><td></td><td>0.0302</td><td>0299</td><td>0296</td><td>v293</td><td>0530</td><td>0287</td><td>0284</td><td>0282</td><td>0279</td><td>0276</td><td>0</td><td>-</td><td>-</td><td>-</td><td>-</td><td>2</td><td>2</td><td>2</td><td>3</td></td<>		0.0302	0299	0296	v293	0530	0287	0284	0282	0279	0276	0	-	-	-	-	2	2	2	3
0245 0242 0240 0238 0235 0233 0231 0228 0226 0 0 1 1 1 1 2 2 2 0221 0221 0219 0217 0219 0219 0219 0219 0219 0219 0219 0219	0245 0242 0240 0238 0235 0233 0231 0228 0226 0 0 1 1 1 1 1 2 2 2 0221 0219 0217 0215 0213 0211 0209 0207 0204 0 0 1 1 1 1 1 1 1 2 2 0200 0219 0319 0194 0193 0191 0189 0187 0185 0 0 1 1 1 1 1 1 1 2 2 1 1 1 1 1 1 1 1 1		0.0273	0271	0268	0265	0263	0560	0257	0255	0252	0220	0	-	-	-	-	2	2	2	2
0221 0219 0217 0215 0213 0211 0209 0207 0204 0 0 1 1 1 1 1 1 2 0200 0200 0308 0198 0198 0199 0193 0191 0189 0187 0185 0 0 1 1 1 1 1 1 1 2 1 2 3 4 5 6 7 8	0221 0219 0217 0215 0213 0211 0209 0207 0204 0 0 1 1 1 1 1 1 2 0200 0200 0308 0196 0194 0193 0191 0189 0187 0185 0 0 1 1 1 1 1 1 1 2 1 2 1 2 3 4 5 6 7 8 9 1 2 3 4 5 6 7 8 8 9 1 2 3 4 5 6 7 8 1 2 3 8 4 5 6 7 8 8 9 1 2 3 4 5 6 7 8 8 9 1 2 3 8 8 9 7 8 8 9 7 8 8 9 7 8 8 9 7 8 8 9 7 8 8 9 7 8 8 9 7 8 8 9 7 8 8 9 7 8 8 9 7 8 8 9 7 8 8 9 7 8 8 9 7 8 8 9 7 8 8 9 7 8 8 9 7 8 8 9 7 8 8 9 7 8 8 9 7 8 9 9 7 8 9 9 7 8 9 9 7 8 9 9 7 8 9 9 7 8 9 9 7 8 9 9 7 8 9 9 7 8 9 9 7 8 9 9 9 7 8 9 9 7 8 9 9 9 7 8 9 9 9 7 8 9 9 9 9		0.0247	0245	0242	0240	0238	0235	0233	0231	0228	0226	0	0	-	-	-	-	2	2	2
0200         0198         0196         0193         0191         0189         0187         0185         0         0         1         1         1         1         1         2           1         2         3         4         5         6         7         8         9         1         2         3         4         5         6         7         8	0200 0198 0196 0194 0193 0191 0189 0187 0185 0 0 1 1 1 1 1 1 2 1 2 8 1 2 3 4 5 6 7 8 8 1 2 3 4 5 6 7 8 8 1 8 1 8 1 8 1 8 1 8 1 8 1 8 1 8 1		0.0224	0221	0219	0217	0215	0213	0211	0200	0207	0204	0	0	-		-		-	2	
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1.2461         1.2866         1.2712         1.2940           1.3771         1.2866         1.2712         1.2860           1.5220         1.5373         1.5627         1.4191           1.5220         1.5731         1.5627         1.56383           2.0544         2.0751         2.0999         2.1170           2.2706         2.2033         2.3164         2.3867           2.2706         2.2634         2.5600         2.5867           2.7732         2.8011         2.8292         2.3170           2.7732         2.8011         2.8292         2.3857           3.0649         3.0687         3.1288         3.1882           3.7434         3.7810         3.1882         3.1882           3.3872         4.1787         4.2007         4.2631           4.1371         4.1787         4.2007         4.2631           6.810         6.2339         6.2469         5.938           6.811         6.8895         6.2869         6.3589           6.811         6.2339         6.2469         7.0281           1.1743         1.1580         11.154         11.154           1.1746         1.1359         11.413 <td< th=""><th>1,2214 1,3499 1,4918 1,6487 1,8221 2,0138 2,2255 2,4596</th><th>1.0101</th><th>1.0202</th><th>1.0305</th><th>1.0408</th><th>1.0513</th><th>1.0618</th><th></th><th>1.0725</th></td<>	1,2214 1,3499 1,4918 1,6487 1,8221 2,0138 2,2255 2,4596	1.0101	1.0202	1.0305	1.0408	1.0513	1.0618		1.0725
1,5068         1,5220         1,5373         1,5627         1,5683           1,6653         1,6850         1,5889         1,7160         1,7333           1,8404         1,8889         1,7160         1,7333           2,2479         2,2705         2,2933         2,3164         2,3366           2,2479         2,2706         2,2933         2,3164         2,3366           2,7466         2,7732         2,8011         2,8292         2,1170           2,7466         2,7732         2,8011         2,8292         2,170           3,7662         3,7434         3,7810         3,468         3,1582           3,7662         3,7434         3,7810         3,8190         2,1867           4,7527         4,572         4,6646         4,7116           5,0028         5,0331         5,193         5,1946         3,1867           6,179         6,2339         6,2966         6,3686         5,7546           6,179         6,2339         6,2968         6,3688         7,7279           7,4653         7,5294         4,7187         1,7690         7,7729           8,2482         8,5407         8,5846         6,7640         6,3680	1.4918 1.6487 1.8221 2.0138 2.2255 2.4596	1.2337	1.2461	1.2586	1.2712	1.2840	1.2969		1.3100
16653         16820         15889         1,7160         1,733           1,8404         1,8689         1,8776         1,8965         1,9155           2,0340         2,0340         2,0346         2,3366         2,1155           2,0443         2,2693         2,3164         2,3366         2,1170           2,4483         2,2693         2,3600         2,5867         2,3366           2,0466         2,7732         2,8011         2,8292         2,1364         2,3366           3,0545         3,7843         3,7810         3,8656         3,4903         3,1862         3,4903           3,0546         3,7812         3,7810         3,8696         3,4903         3,8674         4,7171         4,777         4,777         4,7787         4,207         4,2631         5,796         5,596         5,596         5,8945         5,796<	1.6487 1.8221 2.0138 2.2255 2.4596	1.5068	1.5220	1.5373	1.5527	1.5683	1.5841	- 1	1.6000
2.0340         2.0544         2.0751         2.0969         2.1170           2.0349         2.22705         2.2933         2.3164         2.3396           2.4843         2.2705         2.2933         2.3164         2.3396           2.7456         2.7732         2.8041         2.3396         2.3166           3.0344         3.0849         3.0867         3.4867         2.8877           3.0544         3.0849         3.1268         3.1862         3.3867           3.0546         3.7734         4.1787         4.2607         4.5877           4.5060         4.3711         4.1787         4.2207         4.5817           5.0028         5.0531         5.1039         5.1562         5.2010           5.5020         5.8445         5.407         4.5868         7.0887           6.7531         6.8210         6.8396         6.3588         7.0887           6.7531         6.8210         6.8396         6.3588         7.0887           6.7531         6.8210         6.8399         9.3333         9.4877           10.074         10.76         10.278         10.381         10.486           11.34         11.246         11.359         11.473<	2.2255	1.6653	1.8589	1.6989	1,7160	1.7333	1.7507		1.7683
2.2479         2.2205         2.2933         2.3164         2.3396           2.74843         2.5083         2.5346         2.5367         2.3396           2.7484         2.5083         2.5345         2.5600         2.5857           3.0344         3.0849         3.0871         3.4865         3.4802           3.0548         3.0849         3.0873         3.4866         3.4802           3.0567         3.7434         3.7817         4.2607         4.2877           4.0960         4.1371         4.1787         4.2207         4.2867           5.0228         5.0531         5.1039         5.1582         5.7846           6.7531         6.8210         6.8396         6.2968         7.7879           8.2482         8.3311         8.4149         8.4994         8.5499           8.7482         8.3311         8.4149         8.4994         8.5499           8.7482         8.3311         8.4149         8.4994         8.5499           8.7482         8.3311         8.4149         8.4994         8.5499           8.7482         8.3311         8.4149         8.4994         8.5499           8.7482         8.3311         8.4149         8.55	2.2255	2.0340	2.0544	2.0751	2.0959	2.1170	2.1383		2.1598
2.7456         2.7732         2.8011         2.8292         2.8577           3.0344         3.0649         3.0945         3.1288         3.1882           3.0556         3.3656         3.4956         3.1288         3.1882           3.7062         3.7434         4.1787         4.2631         4.2631           4.0567         4.5172         4.6182         4.6646         4.7115           5.0028         5.0531         5.1039         5.1852         5.2070           5.5290         5.8845         5.6407         5.6958         6.3588           6.1104         6.1719         6.2339         6.2965         6.3588           6.104         6.1719         6.2339         6.2965         6.3588           6.107         6.8170         6.8866         6.9688         7.0887           7.4633         7.5383         7.6189         7.0887           1.0074         10.176         10.278         10.381         11.588           1.134         11.2429         12.549         12.489         14.618           1.1359         13.736         12.894         14.013         14.164           1.134         12.205         12.284         12.368         12.368 </td <td></td> <td>2.2479</td> <td>2.2705</td> <td>2.2933</td> <td>2.3164</td> <td>2.5857</td> <td>2.3632</td> <td></td> <td>2.3869</td>		2.2479	2.2705	2.2933	2.3164	2.5857	2.3632		2.3869
3,0344         3,0649         3,0649         3,1268         3,1268           3,0555         3,7812         3,4566         3,1682         3,4656         3,1682           4,0600         4,1371         4,1787         4,2691         4,2631         4,7645         4,7645         4,7646         4,7165         4,6666         4,7115         6,2339         6,2368         6,2368         6,3568         6,3568         6,3568         6,3586         6,3586         6,3586         6,3586         6,3586         6,3586         6,3586         6,3586         6,3588	2,7183	2.7456	2.7732	2,8011	2.8292	2.8577	2.8864		2.9154
3,7062         3,4817         3,4950         3,5874           4,0960         4,1371         4,1787         4,5950         3,5874           4,0960         4,1371         4,1787         4,207         4,2631         3,5846           6,0028         6,0531         5,1039         5,1852         5,2070         5,2893           5,5290         5,6847         5,1952         5,1852         5,2070         5,2893           6,7331         6,1719         6,2339         6,2965         6,3986         6,4377           6,7831         6,1719         6,2339         6,2965         6,3686         6,4377           6,7831         6,1719         6,2339         6,2965         6,3686         6,4237           6,7831         7,1714         7,6906         7,7679         7,8460         7,993           7,4653         7,5823         7,6449         8,4994         8,5487         9,5811           10,74         10,176         10,278         10,381         11,705         11,705           11,34         11,249         12,499         14,491         14,491         11,706           15,206         12,249         11,280         11,403         11,106         11,206	3.0042	3.0344	3.0649	3.0957	3.1268	3.1582	3.1899		3.2220
4,5267         4,5722         4,6182         4,6646         4,7113         4,090           4,5267         4,5722         4,6182         4,6464         4,7113         4,060           6,5290         5,6393         5,1562         5,2070         5,2563           6,5290         6,5895         6,2896         6,3588         6,4237           6,7531         6,8210         6,8895         6,2896         6,3588         6,4237           6,7633         7,5141         7,6906         7,7679         7,0923           7,4633         7,5141         7,6906         7,7679         7,8460           8,2482         8,3311         8,4149         8,4994         8,5497         9,5831           1,0074         10,776         10,278         10,381         10,486         10,581           11,134         11,246         11,359         11,473         11,588         11,705           11,134         11,246         11,359         11,473         11,588         11,705           11,134         11,246         11,359         11,473         11,588         11,705           11,359         13,473         14,184         14,184         14,186         10,381           11	3,3201	3.3535	3.3872	3.4212	3,4556	3.4903	3.5254		3.5609
4,5267         4,5722         4,6182         4,6646         4,7116         4,7588           5,0028         5,0231         5,1039         5,1562         5,2070         5,2893           6,1104         6,1719         6,2339         6,2868         6,32070         5,2893           6,1104         6,1719         6,2339         6,2868         7,0287         7,0933           7,653         7,5287         7,0287         7,0933         7,0483         7,0287         7,0933           8,2482         8,3311         8,4449         8,5849         8,5849         8,5711         9,8871         9,8871           9,1157         9,2073         9,2999         9,3833         9,4877         9,8871         9,8871           10,074         10,176         10,278         10,381         10,486         10,591           11,134         11,246         11,359         11,473         11,589         11,705           11,236         13,736         13,874         14,013         14,184         14,286           16,519         15,180         15,333         15,487         15,800         17,462           16,510         12,254         12,584         14,186         17,462	4.0552	4.0960	4.1371	4.1787	4.2207	4.2631	4.3060	, 4	4.3492
5,0028         5,0531         5,1562         5,2070         5,2833           6,7231         6,1039         6,1562         5,2070         5,2833           6,1104         6,1719         6,2836         6,2868         6,7546         6,8124           6,1104         6,1719         6,2836         6,2868         7,0287         7,0933           7,4633         7,583         7,6141         7,6906         7,7679         7,2460           8,2482         8,8311         8,4149         8,4994         8,85849         8,6711           9,1157         10,176         10,278         10,381         10,486         10,591           11,344         11,246         11,359         11,473         11,588         11,705           11,349         11,249         12,884         14,154         14,296           11,340         11,246         11,384         14,154         14,296           11,340         11,246         11,3874         14,154         14,296           15,029         15,180         15,387         14,114         14,296           16,10         16,777         16,945         17,116         17,288         17,462           18,347         2,2486	4.4817	4.5267	4.5722	4.6182	4.6646	4.7115	4.7588	4	4.8066
6.7531         6.81049         5.0947         5.0945         6.3598         6.4237           6.7531         6.8210         6.8895         6.2896         6.3598         6.4237           6.7531         6.8210         6.8895         6.2896         7.7679         7.0923           7.4633         7.5383         7.6141         7.6906         7.7679         7.8460           8.2482         8.3311         8.4149         8.4994         8.5849         8.5711           9.1157         10.776         10.278         10.281         10.281         10.281         10.281           11.134         11.246         11.359         11.473         11.588         11.705           12.006         12.487         12.887         12.386         10.281           15.029         13.484         14.013         14.154         14.296           15.029         13.746         11.359         11.473         14.264         14.296           15.029         13.487         14.154         14.296         17.462           15.029         13.487         14.154         14.296         17.462           15.029         13.481         17.16         17.288         17.462	4.9530	5.0028	5.0531	5.1039	5.1552	5.2070	5,2593	47	5.3122
6.751 6.810 6.8895 6.988 70287 70997 70897 70893 74633 75383 75144 76906 777679 708460 77679 708460 82482 83311 8.4449 8.4894 8.8849 8.8711 91.0074 10.074 10.278 10.278 10.281 10.486 10.591 11.34 11.246 11.359 11.473 11.588 11.705 11.3599 13.359 12.554 12.880 12.807 12.366 13.378 13.874 14.013 11.4154 11.296 13.378 13.874 14.013 11.4154 17.296 13.378 13.479 15.320 12.5421 12.206 12.2874 23.104 23.336 23.351 22.4779 25.602 22.874 23.104 23.336 23.571 22.4779 25.602 22.874 23.104 23.336 23.351 24.779 25.602 25.2874 23.104 25.730 26.502 25.544 23.336 25.7385 25.2874 24.2986 25.2874 24.2986 25.387 28.219 26.503 28.789 26.504 25.544 25.790 26.504 25.544 25.790 26.505 26.504 25.544 25.790 26.504 25.544 25.790 26.504 25.544 25.790 26.504 25.544 25.790 26.504 25.544 25.790 26.504 25.544 25.790 26.504 25.791 26.504 27.791 27.791 27.	5,4739	6 1104	5,5845	5.5407	5.69/3	6.3500	5.8124	ຜ	5.8709
7.4633         7.5141         7.6906         7.7679         7.8460           8.2482         8.3311         8.4149         8.4994         8.849         8.6711           9.1073         9.2999         9.3833         9.4877         9.5831           10.074         10.176         10.278         10.381         10.486         10.581           11.34         11.246         11.359         11.473         11.588         11.705           12.305         12.429         12.554         12.880         12.306         12.366           15.029         13.359         14.013         14.154         14.296           15.029         13.359         11.473         11.588         11.406           16.510         16.777         16.945         17.116         17.286         17.462           16.510         16.777         16.945         17.116         19.106         19.298           20.287         2.646         2.2874         22.045         22.874         23.304         23.336         23.571           24.779         2.6028         2.2874         22.095         22.534         26.790         26.783           27.385         2.766         2.7.938         22.219 <t< td=""><td>6.6859</td><td>6.7531</td><td>6.8210</td><td>6.8895</td><td>6.9588</td><td>7.0287</td><td>7.0993</td><td>0 1</td><td>7.1707</td></t<>	6.6859	6.7531	6.8210	6.8895	6.9588	7.0287	7.0993	0 1	7.1707
8.2482         8.3311         8.4449         8.4984         8.5849         8.5711           9.0175         9.2073         9.2999         9.3833         9.4877         9.5831           10.074         10.176         10.278         10.486         10.581         10.486         10.581           11.34         11.246         11.259         11.473         11.588         11.705           15.259         12.534         12.584         12.807         12.366           15.259         15.376         13.874         14.013         14.154         14.296           15.259         15.376         15.333         15.487         15.802         15.802           16.777         16.577         16.547         16.278         17.16         17.286         17.456           20.287         18.547         18.546         17.487         15.643         15.802         18.516         19.106         19.286           20.287         18.547         18.547         18.547         22.328         22.336         23.517           20.287         20.569         22.834         22.196         25.34         26.78           20.286         20.288         22.284         25.79         26.78 <td>7,3891</td> <td>7.4633</td> <td>7,5383</td> <td>7,6141</td> <td>7.6906</td> <td>7.7679</td> <td>7.8460</td> <td>1</td> <td>7.9248</td>	7,3891	7.4633	7,5383	7,6141	7.6906	7.7679	7.8460	1	7.9248
9,157         9,2073         9,2899         9,3833         9,4877         9,4877           11,154         11,246         11,249         11,248         11,048         10,591           11,134         11,246         11,249         11,249         11,249         11,249         11,249           12,359         13,359         13,374         14,013         14,154         14,296           15,029         15,376         15,387         15,487         15,487         15,890           16,510         16,777         16,547         16,403         14,154         14,296           16,510         16,777         16,548         17,488         17,462           20,287         20,481         20,905         21,116         19,296           20,287         20,481         20,905         21,116         21,328           20,287         20,481         20,905         21,116         21,328           20,287         20,484         22,336         28,739         26,790           21,385         27,560         27,938         28,219         28,530         26,789           21,386         27,586         27,938         28,219         28,789         38,181           3	8.1662	8.2482	8.3311	8,4149	8.4994	8.5849	8.6711	8	8.7583
1,2,2,4	9.0250	9.1157	9.2073	9.2999	9.3933	9.4877	9.5831	9.	9.6794
12,306   12,429   12,554   12,880   12,807   12,336   13,356   13,376   13,374   14,013   14,154   14,296   15,029   15,180   15,333   15,487   15,643   15,800   16,510   16,777   16,545   15,487   15,643   15,800   16,510   19,106   19,298   17,455   18,541   18,728   18,916   19,106   19,298   17,289   17,288   18,288   18,288   18,288   18,288   18,288   18,288   18,288   18,288   18,288   18,288   17,289   17,288   1	11.023	11.134	11,246	11,359	11.473	11.588	11,705	2 =	11.822
13.569   13.736   13.874   14.013   14.154   14.266   15.029   15.033   15.487   15.643   15.800   16.5100   15.333   15.487   15.643   15.800   16.5100   16.577   16.545   17.288   17.465   19.208   17.289   17.288   17.288   17.288   17.288   17.288   17.288   17.288   17.288   17.288   17.288   17.288   17.288   17.288   17.289   17.288	12.182	12.305	12,429	12,554	12.680	12.807	12,936	13	13.066
15,024   15,180   15,333   15,807   15,6043	13,464	13.599	13.736	13.874	14.013	14.154	14.296	14	14,440
18.357   18.471   18.728   18.116   19.106   19.208   1	14.880	15.029	15.180	15,333	15.487	15,643	15.800	15	15.959
20.287         20.491         20.697         20.905         21.115         21.328           22.471         22.646         22.874         23.104         23.336         23.571           24.779         2.6028         25.280         25.534         25.530         26.050           27.385         27.660         27.938         28.219         26.050         26.050           27.386         30.569         30.877         31.187         31.500         31.817           33.448         33.784         34.124         34.467         34.813         35.163           36.966         41.264         41.579         42.088         42.521         42.948           40.894         41.264         41.679         42.088         42.521         42.948           45.150         46.063         46.525         46.893         47.465           49.899         50.400         50.907         51.419         51.335         57.974           60.347         66.347         66.408         62.803         63.434         64.077           77.478         77.478         77.478         77.478         78.267	18.174	18.357	18.541	18.728	18,916	19.106	19.298	19	19,492
22,421         22,646         22,874         23,104         23,336         23,571           24,779         27,060         25,280         25,534         25,790         26,050           27,385         27,366         27,938         28,19         28,503         28,189           30,265         30,569         30,877         31,187         31,500         31,817           33,448         33,784         34,124         34,467         34,813         35,163           40,864         41,264         41,579         42,082         42,521         42,948           45,150         46,564         46,063         46,525         46,983         47,466           49,899         50,401         56,261         56,261         51,419         51,397         57,974           60,347         56,501         66,178         62,803         63,437         64,072           67,357         66,347         66,408         70,166         70,810           77,478         75,344         76,748         78,257           86,377         86,408         77,478         78,267           72,444         75,944         76,708         77,478         78,267           86,444         7	20.086	20.287	20.491	20,697	20.905	21.115	21.328	21	21.542
20,718         20,008         20,509         20,509         20,509         20,509         20,509         20,109<	22.198	22.421	22.646	22.874	23.104	23,336	23.571	23	23.807
30.265 30.569 30.877 31.187 31.500 31.817 33.448 33.784 34.124 34.467 34.813 35.163 36.966 37.338 37.713 38.092 38.475 39.861 40.884 41.284 41.679 42.098 42.521 42.948 45.150 46.063 46.063 46.525 46.993 47.465 49.899 60.400 50.907 51.419 51.939 57.974 60.347 61.559 62.178 62.803 63.434 64.072 67.357 68.033 68.777 69.408 77.478 78.257 82.289 82.399 75.944 88.2289 77.478 78.257	27.113	27.385	27.660	27.938	28 219	28 503	28.050	26	26.311
33.448 33.784 34.124 34.467 34.813 35.163 36.066 37.338 37.713 38.092 38.475 38.861 46.150 46.564 41.579 42.098 42.521 42.948 45.150 46.564 46.063 46.525 46.393 47.465 49.899 50.400 50.307 51.419 51.395 52.447 55.147 55.701 56.281 56.826 457.397 57.394 60.347 66.343 68.717 69.408 76.105 70.810 74.440 75.189 75.344 76.708 77.478 78.267 82.269 83.096 83.391 84.775 86.488	29.964	30.265	30.569	30.877	31.187	31.500	31.817	32.	32.137
36,966         37,338         37,713         38,092         38,475         38,881           40,854         41,264         41,679         42,088         42,521         42,948           46,864         46,604         46,603         46,525         46,933         47,465           49,889         50,400         50,907         51,419         51,935         52,457           66,947         61,569         62,178         62,803         63,434         64,072           67,357         68,033         68,717         66,408         76,106         70,810           74,440         75,189         75,944         76,704         76,704         78,267           82,269         83,066         83,391         86,775         86,577         86,488	33.115	33.448	33.784	34.124	34.467	34.813	35.163	35.	35,517
40.854 41.264 41.679 4.2088 42.551 42.948 42.150 42.948 42.150 45.604 45.604 45.605 46.525 46.995 47.465 46.899 50.400 50.907 51.419 51.395 52.457 55.701 56.201 56.826 45.7397 57.397 67.397 67.397 67.397 67.397 67.397 68.337 68.777 69.408 77.378 78.257 88.289 83.066 83.391 84.775 85.77 86.488	36.598	36.966	37.338	37.713	38.092	38.475	38.861	39,252	52
49.190 45.004 46.003 46.225 46.935 47.485 49.899 50.400 50.907 51.419 51.335 52.457 55.701 56.261 65.826 457.397 57.374 60.947 61.559 62.178 62.803 63.434 64.072 74.440 75.189 75.944 76.708 77.478 78.267 82.269 83.066 83.391 84.775 85.277 86.488	40,447	40.854	41.264	41.679	42.098	42.521	42.948	43,380	380
55.147         56.701         56.261         56.826         457.397         57.974           60.947         61.559         62.178         62.803         63.434         64.072           67.357         68.033         68.177         66.408         70.105         70.810           74.440         75.944         76.704         76.708         77.478         78.267           82.269         83.096         83.931         84.775         86.488	49.402	49.899	50.400	50.907	46.525 51.419	51.935	47.465 52.457	52.	47.942 52.985
60.947 61.559 62.178 62.803 63.434 64.072 67.357 68.033 68.177 66.408 70.105 70.810 77.478 78.257 78.259 83.096 83.931 84.775 85.627 86.488	54.598	55.147	55.701	56.261	56.826	457.397	57.974	58.	58.557
67.357 68.033 68.177 69.408 70.105 70.810 74.40 75.189 75.944 76.708 77.478 78.257 82.269 83.066 83.931 84.775 85.627 86.488	60.340	60.947	61,559	62.178	62.803	63,434	64.072	64	64.715
75,189 75,944 76,708 77,478 78,257 82,269 83,096 83,931 84,775 85,627 86,488	989.99	67.357	68.033	68.717	69.408	70.105	70.810	71.	71.522
	81.451	82.269	83.096	83.931	84.775	85.627	78.257	87.	79.044
	99.484	100,48	101.49	102.51	103.54	104.58	105.64	10	106.70
100.48 101.49 102.51 103.54 104.58 105.64	109.95	111.05	112.17	113.30	114.43	115.58	116.75	11	117.92
100.48 101.49 102.51 103.54 104.58 105.64 111.05 112.17 113.30 114.43 115.58 116.75	121.51	122.73	123.97	125.21	126.47	127.74	129.02	130	130.32
100.48 101.49 102.51 103.54 104.58 105.64 111.05 112.17 113.30 114.43 115.58 116.75 122.73 123.97 155.21 126.47 129.02	67.401	+0.00.	137,000	138.38	139.77	141.17	142.59	14	144.03
100.48 101.49 102.51 103.54 104.58 105.64 111.05 112.17 113.30 114.43 115.58 116.75 122.73 123.97 125.21 126.47 127.74 129.02 135.64 137.00 138.38 139.77 141.17 142.59	403 43	164.02	181.27	200,34	221.41	244.69	270.43	296	298.87
100.48 101.49 102.51 103.54 104.58 105.64 111.05 112.77 113.30 114.43 115.58 116.75 122.73 123.97 125.21 126.47 127.74 129.02 135.64 137.00 138.38 139.77 141.17 142.59 164.02 181.27 200.34 223.141 244.69 270.43	1096.6	1212.0	1339 4	1480.3	1636.0	1808.14	1998 2	220	14.
100.48   101.49   102.51   103.54   104.58   105.64   110.05   112.77   113.30   114.43   115.58   116.75   1	2981.0	3294.5	3641.0	4023.9	4447.1	4914.8	5431.7	909	6002.9
100.48   101.49   102.51   103.54   104.58   105.64   111.05   112.77   113.30   114.43   115.58   116.75   116.75   112.73   115.64   129.02   128.64   137.00   138.38   139.77   141.17   142.59   164.02   181.27   200.34   221.41   244.69   270.43   245.68   492.75   544.57   601.85   665.14   735.10   1212.0   1339.4   1480.3   1636.0   1908.0   1998.2   2394.5   364.10   4023.9   4447.1   4914.8   5431.7	8103.1	8955.3	1,7686	10938	12088	13360	14765	163	16318
100.48	22026	24343	26903	29733	32860	36316	40135	44356	99

.007447 .002739 .001008 .0<sup>3</sup> 3707 .0<sup>4</sup> 5017 .0<sup>4</sup> 1364

.003028 .003028 .001114 .0<sup>3</sup>4097 .0<sup>3</sup>1507 .0<sup>4</sup>5545

.009095 .003346 .001231 .0<sup>3</sup>4528 .0<sup>3</sup> 1666 .0<sup>4</sup> 6128

.010052 .003698 .001360 .0<sup>3</sup> 5005 .0<sup>3</sup> 1841 .0<sup>4</sup> 6773

.004087 .004087 .001503 .0<sup>3</sup>5531 .0<sup>3</sup>2035 .0<sup>4</sup>7485

.004517 .004517 .001662 .0<sup>3</sup> 6113 .0<sup>4</sup> 8272 .0<sup>4</sup> 8272

.013569 .004992 .001836 .0<sup>3</sup> 6755 .0<sup>3</sup> 2485 .0<sup>4</sup> 9142

.014996 .005517 .002029 .0<sup>3</sup>7466 .0<sup>3</sup>2747 .0<sup>3</sup>1010

.016573 .006097 .002243 .0<sup>3</sup>8251 .0<sup>3</sup>3035 .0<sup>4</sup>1117

0.0018316 0.006738 0.002479 0.0.<sup>3</sup>9119 0.0.<sup>3</sup>3355 0.0.<sup>3</sup>1234 0.0.<sup>4</sup>4540

## Natural logarithms: logex or lnx

l		20 1	5.2	5.3	2	5.6	D.	5,8	6.0	6.1	6.3	6.4	6.6	6.7	6.8	7.0	7.1	7.2	7.4	7.5	7.6	7.7	7.8	8.0	8,1	8.2	8.4	8.5	8.6	8.7	8.9	9.0	9.1	2.8	9.4	9.5	9.6	9.8	9.9
1	6					m	10.0	m =		- 10		0		~ .	- 10	_		_		T.,	_				_										_		_	_	_
ı	8	10000		77 27								5 52		48		222		38		1			32			28		1000		24		AT /	22			1 20			18
1	7 8	2000	2 77					2 2		1 51		45		43		10155			33 4				28			25				21		20		2 20			71	16	16
I		9	9 9	9 1	n in	'n	10	4 4	46	44	4	39	3 8	3 3	7 %	8	8 8	30	28 28	27	26	25	24	23	22	22	20	20	10	9 8	18	17	17	16	16	15	15	14	14
	9	59	23 28	51	47	45	44	41	33	38	38	35	33	32	3 8	29	28	28	25	24	23	22	20 20	20	19	20 20	17	17	16	16	15	15	14	4 4	5	13	13	12	12
ı	10	49	45	43	39	38	36	34 34				29				24	23	22	20	20	19	18	17	16	16	15 15	15	14	14	13	13	12	12	12	=	=	= :	2	10
	4	39	37	34	3 5	30	29	27	26	25	24	23	22	21	20	20	19	17 8	16	16	15	12	14	13	13	12	12	Ξ	= :	1 01	0	10	2 0	0 0	6	a	6 0	0 00	80
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	2	20	18	17	16	15	15	14	13	13	12	12	Ξ	= 5	2 2	0	6 6	n 0	0 00	00	00	~ 1	1	1	9	9 9	9	9	S I	o co	2	2	u ou	מומ	4	4	4 4	4	4
	-	10	0 0	000	0 00	80	- 1		7	9 9	9	9 9	20	n n	വ	ın	φ. 4	4 4	4	4	4	4 .	4 W	m	m (	m m	m	m	m (	77 (7)	6	2	2 2	7 7	2	2	2 0	2 4	2
	6		0862	1740	2546		3293	3988		4637	5247	5822		6366	6881	7372	7839	8286	9123	9517	9895	0260	0953	1282	1600	1909	2499	2782	3056	3524	3838	4085	4327	4793	5019	5239	5454	5872	6074
	8		0770	1655	2469		3221	3920		4574	5188	5766		6313	6831	7324	7793	8242 8671	9083	9478	9858	0225	0978	1249	1569	2179	2470	2754	3029	3558	3813	4061	4303	4770	4996	5217	5433	5851	6054
	1		0677	1570	2390		3148	3853		4511	5128	5710		6229	6780	7275	7747	8198	9042	9439	9821	0188	0886	1217	1537	2149	2442	2726	3002	3533	3788	4036	4279	4748	4974	5195	5412	5831	6034
	9		0583	1484	2311		3075	3784		4447	8909	5653		9029	6229	7227	7701	8154	9002	9400	9783	0152	0808	1184	1506	2119	2413	2698	2975	3507	3762	4012	4255	4725	4951	5173	5390	5810	6014
	5		0488	1398	2231		3001	3716		4383	9009	5596		6152	8299	7178	7655	8109	1968	9361	9746	0116	0818	1151	1474	2090	2384	2669	2947	3481	3737	3987	4231	4702	4929	5151	5369	6730	5994
	4	0392	1310	2151	1017	2927	0000	3646	4318	4947	Ì	5539	8609	7693	1700	7129	7608	8065	8920	9322	9708	0080	0784	1119	1442	1756	2355	2641	2920	3455	3712	3962	4207	4679	4907	5129	5347	6929	5974
	3	0296	1222	0206	2010	2852	200	35//	4253	4886	200	5481	6043	GE7E	0.00	7080	7561	8020	8879	9282	9670	0043	0750	1086	1410	2030	2326	2613	2892	3429	3686	3938	4183	4656	4884	5107	5326	5748	5963
	2	0198	1133	1080	000	2776	2503	3207	4187	4824		5423	5988	6622	0000	7031	7514	8416	8838	9243	9632	9000	0716	1053	1378	2000	2296	2585	2865	3403	3661	3913	4159	4633	4861	5085	5304	5728	5933
-	-	0100	1044	1006	000	2700	24.30	3430	4121	4762		5365	5933	6471	5	6981	7467	8372	8796	9203	9594	8966	0682	1019	1346	1969	2267	2556	2837	3376	3635	3888	4134	4609	4839	5063	5497	5707	5913
	0	0.0000	0.0953	0.1823	0.1043	0.2624	30000	0.3305	0.4055	0.4700		0.5306	0.5878	0.6419		0.6931	0.7419	0.8329	0.8755	0.9163	0.9555	1 0000	1.0647	1.0986	1.1314	1,1939	1.2238	1.2528	1.2809	1,3350	1.3610	1.3863	1.4110	1.4586	1.4816	1.5041	1.5261	1,5686	1.5892
	*	1.0	1.1	1.2		1,3		*	1.5	1.6		1.7	1.8	9		2.0	1.7	2.3	2.4	2.5	2.6	200	2.9	3.0	3.1	3.3	3.4	3.5	3.6	3.8	3.9	4.0	4.1	4.3	4.4	5.5	2.0	80	6.9

*	0	1	2	2	4	5	9	7	80	6	-	2 3	4	9	9	1	80	6
6.0	1.6094	6114	6134	6154	6174	6194	6214	6233	6253	6273	2	4 6	-	1	12	14	16	18
5.1	1.6292	6312	6332	6351	6371	6390	6409	6429	6448	6467	2	4	8	10	12	14	16	17
5.2	1.6487	9099	6525	6544	6563	6582	6601	6620	6639	8999	2	4			1	13	15	17
5.3	1.6677	9699	6715	6734	6752	6771	6790	8089	6827	6845	2			6	=	13	15	17
9.4	1.5864	6882	6901	6918	6938	9569	6974	6993	7011	7029	2	4 6			11	13	15	17
5,5	1.7047	9902	7084	7102	7120	7138	7156	7174	7192	7210	2	4 5	7	6	11	13	14	16
9.6	1.7228	7246	7263	7281	7299	7317	7334	7352	7370	7387	2	4 5	7	6	:	12	14	16
6.7	1.7405	7422	7440	7457	7475	7492	7509	7527	7544	7561	2	3 5	_	6	10	12	14	16
8.0	1.7579	7596	7613	7630	7647	7664	7681	7699	7716	7733	2		7	6	10	12	14	15
6.9	1.7750	7766	7783	7800	7817	7834	7851	7867	7884	7901	2	3 5	_	00	10	12	13	15
6.0	1 7918	7934	7951	7967	7004	1000	00017	*600	0000	2200		0	-	0	9		:	1
6.1	1 8083	0000	2110	1961	1304	1000	2000	8034	0608	9000	N 0	5 0		00 0	2 5	12	2	9
	1,000	8800	0110	8132	8148	8165	1818	818/	8213	8228	7	20 10 10 10 10 10 10 10 10 10 10 10 10 10	-		10	=	3	15
2.6	1.0245	7978	8778	8294	8310	8326	8342	8328	8374	8390	2	3 2			0	11	13	14
6.3	1.8405	8421	8437	8453	8469	8485	8200	8516	8532	8547	2	3 5	9	00	6	=	13	14
8.4	1,8563	8579	8594	8610	8625	8641	8656	8672	8687	8703	2	3 5	9	8	6	Ξ	12	14
6.5	1.8718	8733	8749	8764	8779	8795	8810	8825	8840	8856	2	3 5		α	a	1	12	14
6.6	1.8871	RRRR	8001	8016	0021	0000	0000	2200	0000	9000	, ,		0 0		0 0	:	4 5	:
6.7	1.9021	9036	9051	9006	9081	9006	0110	9126	0140	9156		3 6			0	101	2 4	
8 8	1 9169	0104	0010	0000	0000	0000	0 00	0210	00000	0000				. 1	0 0	2 !	7	2 !
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2	01000	9990	2044	9339	93/3	3387	3402	2410	9430	9445	-	5	٥	-	n	10	12	3
2.0	1.9459	9473	9488	9502	9516	9530	9544	9559	9573	9587	-	3 4	9	1	6	10	=	13
7.1	1.9601	9615	9629	9643	9657	9671	9685	6696	9713	9727	-	3 4	9	1	8	10	=	13
7.2	1.9741	9755	6926	9782	9626	9810	9824	9838	9851	9865	-	3 4	9	7	8	10	11	12
7.3	1,9879	9892	9066	9920	9933	9947	9961	9974	8866	0001	-	3 4	ı.	7	00	10	=	12
7.4	2.0015	0028	0042	9900	6900	0082	9600	0109	0122	0136	-	3 4	- CO	7	00	6	=	12
7.5	2 0149	0162	0176	0100	2000	2100	0000	0.000	2000	0000				,	0		:	1
7.8	2 0281	0205	0300	0201	0202	0247	0220	2470	0000	0000	- ,	, ,	חו	- 1	0 0	ם ת	= 5	7
7.7	20412	0426	0000	0.022	9000	0347	0390	03/3	0386	0388		9 0	۵ ۱	-	20 0	5 (	10	12
30	2.0412	0240	0438	1040	0464	04//	0490	0503	0516	0528	-	9	ם מ	9	00	on .	10	12
9 1	2.0541	0224	0267	0280	0592	9090	0618	0631	0643	9990	-	3 4	2	9	8	6	10	=
6.7	2.0669	0681	0694	0202	0719	0732	0744	0757	6920	0782	-	3 4	2	9	8	6	10	Ξ
8.0	2.0794	0807	0819	0832	0844	0857	6980	0882	0894	9060	-	2 4	10	9	7	6	10	1
8.1	2.0919	0931	0943	9360	8960	0860	0992	1005	1017	1029	-	2 4	100	4	7	σ	10	:
8.2	2.1041	1054	1066	1078	1090	1102	1114	1126	1138	1150		2 4	14	0	7	α	10	:
8.3	2,1163	1175	1187	1199	1211	1223	1235	1247	1258	1270		0	) ц	0		0 0	2 5	:
8.4	2.1282	1294	1306	1318	1330	1342	1353	1365	1377	1389		2 0	9 4	0 (	. 1	ο α	0	: :
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6.0	2.1401	1412	1424	1436	1448	1459	1471	1483	1494	1506	-	2 4	25.50	9	1	00	6	=
0.0	2.1518	1529	1541	1552	1564	1576	1587	1599	1610	1622	-			9	7	œ	θ	10
8.7	2.1633	1645	1656	1668	1679	1691	1702	1713	1725	1736	-	2 3	n n	9	1	00	6	10
8.8	2.1748	1759	1770	1782	1793	1804	1815	1827	1838	1849	-			9	7	80	6	10
6.9	2.1861	1872	1883	1894	1905	1917	1928	1939	1950	1961	-	-0.0	4	9	1	80	6	10
0.6	2.1972	1983	1994	2006	2017	2028	2039	2050	2061	2072	-	2 3	4	45	7	00	0	10
9.1	2.2083	2094	2105	2116	2127	2138	2148	2159	2170	2181		2	4	u	7	α	0	0
9.2	2.2192	2203	2214	2225	2235	2246	2257	2268	97.79	2289			4	o u	. 4	0	0	9 9
9.3	2.2300	2311	2322	2332	2343	2354	2364	2375	2386	2396			Ψ.	n u	0 4	2 1	0	2 5
9.4	2.2407	2418	2428	2439	2450	2460	2471	2481	2402	2502		0 0		o u	0 15		0 0	2 9
-	0.0000	0000			-									2			,	2
0 0	2,2513	5262	2554	2544	2555	2565	2576	2586	2597	2607	-		4	S)	9	7	00	6
0 1	2.2618	8797	2638	2649	2659	2670	2680	2690	2701	2711	-		4	ດ	9	1	00	6
9.7	2.2721	2732	2742	2752	2762	2773	2783	2793	2803	2814	-		4	2	9	7	80	6
9.8	2.2824	2834	2844	2854	2865	2875	2885	2895	2905	2915	-	2 3	4	ß	9	7	00	6
6.	2.2925	2935	2946	2956	2966	2976	2986	2996	3006	3016	-	2 3	4	2	9	7	00	6
×	0																	
	2		2	3	4	9	9	1	8	6	-	2 3	4	ď	8	7	00	C

×	log <sub>e</sub> 10°
10	24,9741
6	21.2767
60	19.5793
1	17.8819
9	14,1845
9	12,4871
4	10.7897
69	7.0922
2	5,3948
-	3.6974
×	loge 10"x

×	1	7	2	4	9	9	,	80	6	10
loge 10°	2,3026	4.6052	6.9078	9.2103	11,5129	13,8155	16,1181	18,4207	20.7233	23.0259

## Common logarithms: log 10 X

1	×	10	=	12	13	14		15	16	17	18	19		20 17	22	24 23	25	26	28	30	37	33	50	36	37	39	40	42	4 43	45	46	48	49	×
1   2   3   4   5   5   6   6   7   7   7   7   7   7   7   7		1000	2021/2												3,00					100	-										1000			ALC: NO.
1	0																																	0
1	1																																	1
1	2																																	2
1	3	0128	0531	6680	1239	1553		1847	2122	2380	2625	2856		3075	3483	3674	4031	4362	4518	4814	4955	5224	0202	5599	5717	5944	6053	6263	6365	6561	6656	6839	8269	3
Color   Colo	4	0170	6990	0934	1271	1584		1875	2148	2405	2648	2878		3304	3502	3692	4048	4216	4533	4829	4969	5237	0300	5611	5729	5955	6064	6274	6375	6571	6665	6848	6937	4
1, 10, 10, 11, 11, 11, 11, 11, 11, 11,	10	0100	2120	0969		1303	1614	1903	100	2175	2430	2672	2900	3324	3522	3892	4065	4232	4548	4843	4983	5250	52/6	5623	5740	9969	6075	6284	6484	6580	6675	6857	6946	2
1, 10, 10, 10, 10, 10, 10, 10, 10, 10,	9	-	0645	1004		1335	1644	1931	.000	2201	2017	2695	2923	3345	3541	3729	4082	4249	4564	4857	4997	5263	5331	5635	5752	5977	6085	6294	6395	6590	6684	9//9	6955	9
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7324         7324         7340         7348         7356         7354         7347         7349         7356         7346         7347         7348         7346         7447         7447         7447         7443         7441         7451         7450         7448         7446         7447         7448         7451         7450         7564         7450         7564         7657         7664         7657         7664         7657         7664         7657         7664         7657         7664         7657         7664         7657         7664         7657         7664         7657         7664         7657         7664         7657         7664         7657         7664         7657         7664         7657         7664         7664         7657         7664         7677         7664         7677         7664         7677         7664         7677         7664         7677         7664         7677         7664         7677         7664         7677         7676         7774           7702         7702         7714         7723         7731         7732         7745         7745         7764         7701           7702         7702         7702         7702<	7324         7324         7324         7324         7324         7324         7324         7324         7324         7324         7324         7324         7324         7435         743         7451         7451         7466         7474         7472         7482         7482         7482         7482         7482         7482         7482         7482         7484         7701           7703         7716         7716         7723         7731         7734         7745         7762         7764         7701         7774         7774         7774         7701         7774         7774         7701         7774         7774         7701         7774         7774         7701         7774         7701         7774         7774         778	7324         7332         7340         7348         7356         7354         7357         7349         7349         7349         7356         7349         7357         7349         7349         7349         7349         7349         7349         7349         7349         7349         7349         7349         7349         7349         7349         7349         7349         7349         7349         7344         7449         7449         7449         7444         7449         7449         7449         7449         7449         7449         7449         7449         7449         7449         7449         7449         7449         7449         7449         7449         7449         7449         7449         7444         8440         860         880         8	7324 7332 7404 7412 7492 7490 7534 7645 7709 7716 7709 7716 8000 8000 8126 8207 8451 8457 8451 8457 8451 8457 8639 8639 8692 8638 8751 8756 8808 8814 8868 8814 8869 8894 8976 8987 8976 8987 8976 8987 8976 8987 8976 8987 8976 8987 8977 8977 8977 8977 8977 8977 8978 8987 8978 8987	7259	7267	7275	7284	7292	7300	7308	7316			2 2	2 2		3 2 3 2	3 3 4 5 5	2 3 4 5 6
7404         7412         7419         7427         7435         7436         7443         7451         7456         7456         7445         7456         7467 <th< td=""><td>7404         7412         7419         7427         7435         7443         7451         7451         7436         7444         7451         7450         7450         7450         7450         7450         7450         7450         7450         7450         7450         7450         7451         7450         7450         7451         <th< td=""><td>7404         7412         7419         7427         7435         7443         7461         7461         7414         7417         7419         7414         7411         7419         7411         7421         7436         7520         7528         7526         7526         7526         7526         7526         7527         7520         7527         7520         7527         7520         7527         7520         7527         7520         7527         7520         7527         7520         7527         7520         <th< td=""><td>740.4 741.2 740.7 741.2 748.2 749.0 753.4 764.2 770.9 771.6 770.4 771.6 770.4 771.6 770.4 771.6 770.7</td><td>7340</td><td>7348</td><td>7356</td><td>7364</td><td>7372</td><td>7380</td><td>7388</td><td>7396</td><td>-</td><td></td><td>2</td><td></td><td>2</td><td>2 3 4</td><td>2 3 4 5</td><td>2 3 4 5 6</td></th<></td></th<></td></th<>	7404         7412         7419         7427         7435         7443         7451         7451         7436         7444         7451         7450         7450         7450         7450         7450         7450         7450         7450         7450         7450         7450         7451         7450         7450         7451 <th< td=""><td>7404         7412         7419         7427         7435         7443         7461         7461         7414         7417         7419         7414         7411         7419         7411         7421         7436         7520         7528         7526         7526         7526         7526         7526         7527         7520         7527         7520         7527         7520         7527         7520         7527         7520         7527         7520         7527         7520         7527         7520         <th< td=""><td>740.4 741.2 740.7 741.2 748.2 749.0 753.4 764.2 770.9 771.6 770.4 771.6 770.4 771.6 770.4 771.6 770.7</td><td>7340</td><td>7348</td><td>7356</td><td>7364</td><td>7372</td><td>7380</td><td>7388</td><td>7396</td><td>-</td><td></td><td>2</td><td></td><td>2</td><td>2 3 4</td><td>2 3 4 5</td><td>2 3 4 5 6</td></th<></td></th<>	7404         7412         7419         7427         7435         7443         7461         7461         7414         7417         7419         7414         7411         7419         7411         7421         7436         7520         7528         7526         7526         7526         7526         7526         7527         7520         7527         7520         7527         7520         7527         7520         7527         7520         7527         7520         7527         7520         7527         7520 <th< td=""><td>740.4 741.2 740.7 741.2 748.2 749.0 753.4 764.2 770.9 771.6 770.4 771.6 770.4 771.6 770.4 771.6 770.7</td><td>7340</td><td>7348</td><td>7356</td><td>7364</td><td>7372</td><td>7380</td><td>7388</td><td>7396</td><td>-</td><td></td><td>2</td><td></td><td>2</td><td>2 3 4</td><td>2 3 4 5</td><td>2 3 4 5 6</td></th<>	740.4 741.2 740.7 741.2 748.2 749.0 753.4 764.2 770.9 771.6 770.4 771.6 770.4 771.6 770.4 771.6 770.7	7340	7348	7356	7364	7372	7380	7388	7396	-		2		2	2 3 4	2 3 4 5	2 3 4 5 6
748.2         748.0         750.5         750.8         750.7         750.8         750.7         750.4         750.7         750.4         750.7         750.4         750.7         750.4         750.7         750.4         750.7         760.4         760.7         760.4 <th< td=""><td>748.2         748.0         749.1         750.5         751.3         752.0         752.8         752.9         752.0         752.8         752.0         752.8         752.0         752.0         752.0         752.0         752.0         752.0         752.0         752.0         752.0         752.0         752.0         752.0         752.0         772.1         <th< td=""><td>748.2         748.0         749.1         752.0         752.8         755.8         755.4         755.1           765.9         756.0         756.7         760.4         757.7         760.4         757.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760</td><td>7482 7490 7482 7490 7709 7716 7709 7</td><td>7419</td><td>7427</td><td>7435</td><td>7443</td><td>7451</td><td>7459</td><td>7466</td><td>7474</td><td>-</td><td></td><td>2</td><td>2 2</td><td>2</td><td>2 3 4</td><td>2 3 4 5</td><td>2 3 4 5 5</td></th<></td></th<>	748.2         748.0         749.1         750.5         751.3         752.0         752.8         752.9         752.0         752.8         752.0         752.8         752.0         752.0         752.0         752.0         752.0         752.0         752.0         752.0         752.0         752.0         752.0         752.0         752.0         772.1 <th< td=""><td>748.2         748.0         749.1         752.0         752.8         755.8         755.4         755.1           765.9         756.0         756.7         760.4         757.7         760.4         757.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760</td><td>7482 7490 7482 7490 7709 7716 7709 7</td><td>7419</td><td>7427</td><td>7435</td><td>7443</td><td>7451</td><td>7459</td><td>7466</td><td>7474</td><td>-</td><td></td><td>2</td><td>2 2</td><td>2</td><td>2 3 4</td><td>2 3 4 5</td><td>2 3 4 5 5</td></th<>	748.2         748.0         749.1         752.0         752.8         755.8         755.4         755.1           765.9         756.0         756.7         760.4         757.7         760.4         757.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760.4         767.7         760	7482 7490 7482 7490 7709 7716 7709 7	7419	7427	7435	7443	7451	7459	7466	7474	-		2	2 2	2	2 3 4	2 3 4 5	2 3 4 5 5
7634         7764         767         7679         7885         7694         7771         7779         7779         7779         7779         7779         7779         7779         7774	7634         7642         7643         7674         7679         7684         7677         7679         7784         771           7709         7716         7723         7731         7731         7734         7745         7760         7764         7774           7709         7716         7723         7731         7734         7734         7774         7774           7785         7860         7862         7862         7863         7866         787         7893         7846           7863         7860         7862         7862         7863         7866         787         7893         7846         7701           7924         7860         8062         8004         8014         8021         8048         8056         8041         8048         8056           8126         8062         8062         8062         8062         8041         8048         8056         8048         8056         8048         8056         8048         8056         8048         8056         8048         8056         8048         8056         8041         8049         8048         8056         8041         8049         8056         8041         8049 <t< td=""><td>7634         7642         7643         7647         7679         7684         7677         7679         7716         7714           7709         7716         7723         7731         7731         7734         7745         7760         7774         7774           7709         7716         7723         7731         7733         7731         7733         7746         7774         7774           7785         7786         7860         7867         7862         7866         7973         7890         7810         7774           7853         7860         7867         7869         7866         7873         7891         7917           7853         7860         7867         7869         7866         8973         8978         8968         8968         8968         8968         8968         8968         8968         8968         8968         8968         8968         8968         8968         8968         8969         8819         8969         8819         8869         8869         8869         8869         8869         8869         8869         8869         8869         8869         8869         8869         8869         8869         8869</td><td>7634 7642 7709 7716 7709 7716 7789 7789 7789 7860 7924 7931 8000 8002 8069 8136 8136 8131 8267 8261 8457 8451 8457 8853 8639 8873 8579 8873 8579 8873 8579 8874 8957 8976 8987 8976 8987 8976 8987 9976 9987 99876 9987</td><td>7574</td><td>7582</td><td>7513</td><td>7520</td><td>7528</td><td>7536</td><td>7543</td><td>7551</td><td></td><td></td><td>2 6</td><td></td><td></td><td>3 3</td><td>2 3 4 5</td><td>2 3 4 5</td></t<>	7634         7642         7643         7647         7679         7684         7677         7679         7716         7714           7709         7716         7723         7731         7731         7734         7745         7760         7774         7774           7709         7716         7723         7731         7733         7731         7733         7746         7774         7774           7785         7786         7860         7867         7862         7866         7973         7890         7810         7774           7853         7860         7867         7869         7866         7873         7891         7917           7853         7860         7867         7869         7866         8973         8978         8968         8968         8968         8968         8968         8968         8968         8968         8968         8968         8968         8968         8968         8968         8969         8819         8969         8819         8869         8869         8869         8869         8869         8869         8869         8869         8869         8869         8869         8869         8869         8869         8869	7634 7642 7709 7716 7709 7716 7789 7789 7789 7860 7924 7931 8000 8002 8069 8136 8136 8131 8267 8261 8457 8451 8457 8853 8639 8873 8579 8873 8579 8873 8579 8874 8957 8976 8987 8976 8987 8976 8987 9976 9987 99876 9987	7574	7582	7513	7520	7528	7536	7543	7551			2 6			3 3	2 3 4 5	2 3 4 5
7709         7716         7723         7731         7738         7745         7750         7774         7774           7782         7782         7789         780         7810         7810         782         7832         7833         7846           7853         7860         780         7882         7865         783         7893         7846           7953         8000         8007         8014         8021         8028         7865         7873         7890         7897           7993         8000         8007         8014         8021         8028         8035         8041         8048         8055           8062         8069         8172         8178         8178         8178         8178         8189         8065         8041         8055         8065         8041         8055         8066         8065         8066         8066	7709         7716         7723         7731         7738         7745         7750         7774         7774           7782         7789         7780         7810         7810         7810         782         7837         7839         7846           7853         7860         7867         7882         7865         7837         7893         7846           7983         8000         8007         8014         8021         8028         7865         7873         7893         7846           7993         8000         8007         8014         8021         8028         8035         8041         8016         8116	7709         7716         7723         7731         7738         7745         7752         7787         7778         7779         7774         7774         7774         7774         7774         7774         7774         7774         7774         7774         7774         7774         7774         7774         7774         7774         7774         7777         7774         7774 <th< td=""><td>7709 7716 7782 7789 7883 7860 7984 7931 7993 8000 8062 8069 8129 8136 8195 8202 8261 8267 8261 8457 8451 8659 8653 8659 8652 8668 8751 8756 8697 8976 8978 9978 8978 9978</td><td>7649</td><td>7657</td><td>7664</td><td>7672</td><td>7679</td><td>7686</td><td>7694</td><td>7701</td><td>-</td><td></td><td>٠ -</td><td>1 2</td><td>2</td><td>2 3 4</td><td>2 3 4 4</td><td>2 3 4 4 5 5</td></th<>	7709 7716 7782 7789 7883 7860 7984 7931 7993 8000 8062 8069 8129 8136 8195 8202 8261 8267 8261 8457 8451 8659 8653 8659 8652 8668 8751 8756 8697 8976 8978 9978 8978 9978	7649	7657	7664	7672	7679	7686	7694	7701	-		٠ -	1 2	2	2 3 4	2 3 4 4	2 3 4 4 5 5
7782         7782         7783         7784         7893         7894         7895         8895         8896         8897         8896 <th< td=""><td>7782         7789         7789         7780         7890         7890         7890         7880         8880         <th< td=""><td>7782         7782         7783         7782         7782         7883         7885         7882         7883         7885         7884         7885         7885         7885         7885         7885         7885         7885         7885         7885         7885         7885         7885         7886         7885         7885         7885         7885         7886         8886         <th< td=""><td>7782 7789 7853 7860 7993 8000 8062 8069 8129 8136 8195 8267 8261 8267 8275 8331 8388 8395 8632 8638 8632 8638 8751 8756 88632 8698 8751 8756 88632 8698 8975 8698 8975 8977 8975 8977 8976 8982 9081 9036 9138 9191 9196 9284 9299</td><td>7723</td><td>7731</td><td>7738</td><td>7745</td><td>7752</td><td>7760</td><td>7767</td><td>7774</td><td>-</td><td></td><td>-</td><td>1 2</td><td></td><td></td><td>3 4 4</td><td>3 4 4 5</td></th<></td></th<></td></th<>	7782         7789         7789         7780         7890         7890         7890         7880         8880 <th< td=""><td>7782         7782         7783         7782         7782         7883         7885         7882         7883         7885         7884         7885         7885         7885         7885         7885         7885         7885         7885         7885         7885         7885         7885         7886         7885         7885         7885         7885         7886         8886         <th< td=""><td>7782 7789 7853 7860 7993 8000 8062 8069 8129 8136 8195 8267 8261 8267 8275 8331 8388 8395 8632 8638 8632 8638 8751 8756 88632 8698 8751 8756 88632 8698 8975 8698 8975 8977 8975 8977 8976 8982 9081 9036 9138 9191 9196 9284 9299</td><td>7723</td><td>7731</td><td>7738</td><td>7745</td><td>7752</td><td>7760</td><td>7767</td><td>7774</td><td>-</td><td></td><td>-</td><td>1 2</td><td></td><td></td><td>3 4 4</td><td>3 4 4 5</td></th<></td></th<>	7782         7782         7783         7782         7782         7883         7885         7882         7883         7885         7884         7885         7885         7885         7885         7885         7885         7885         7885         7885         7885         7885         7885         7886         7885         7885         7885         7885         7886         8886 <th< td=""><td>7782 7789 7853 7860 7993 8000 8062 8069 8129 8136 8195 8267 8261 8267 8275 8331 8388 8395 8632 8638 8632 8638 8751 8756 88632 8698 8751 8756 88632 8698 8975 8698 8975 8977 8975 8977 8976 8982 9081 9036 9138 9191 9196 9284 9299</td><td>7723</td><td>7731</td><td>7738</td><td>7745</td><td>7752</td><td>7760</td><td>7767</td><td>7774</td><td>-</td><td></td><td>-</td><td>1 2</td><td></td><td></td><td>3 4 4</td><td>3 4 4 5</td></th<>	7782 7789 7853 7860 7993 8000 8062 8069 8129 8136 8195 8267 8261 8267 8275 8331 8388 8395 8632 8638 8632 8638 8751 8756 88632 8698 8751 8756 88632 8698 8975 8698 8975 8977 8975 8977 8976 8982 9081 9036 9138 9191 9196 9284 9299	7723	7731	7738	7745	7752	7760	7767	7774	-		-	1 2			3 4 4	3 4 4 5
786.3         786.0         786.3         786.4         788.9         789.6         790.3         791.0 <th< td=""><td>786.3         786.0         786.3         786.0         787.1         787.1         787.1         787.1         787.1         787.1         787.1         787.2         788.9         788.6         788.0         787.2         788.9         788.6         787.2         787.2         789.6         789.6         787.3         789.0         787.1         789.0         789.1         789.7         789.0         789.1         789.1         789.1         789.1         889.2         <th< td=""><td>785.3         786.0         786.4         788.9         789.6         790.3         791.0         891.0         <th< td=""><td>7863 7860 79924 7931 7993 8006 8122 8069 8129 8136 8195 8267 8267 8331 8375 8331 8451 8457 8451 8457 8451 8457 8451 8619 8632 8698 8751 8756 8808 8814 8808 8814 8808 8814 8907 8927 9031 9036 9138 9191 9196 9244 9299 9244 9299</td><td>7796</td><td>7803</td><td>7810</td><td>7818</td><td>7825</td><td>7832</td><td>7839</td><td>7846</td><td>-</td><td></td><td>_</td><td>1 2</td><td></td><td></td><td>3 4 4</td><td>3 4 4 5</td></th<></td></th<></td></th<>	786.3         786.0         786.3         786.0         787.1         787.1         787.1         787.1         787.1         787.1         787.1         787.2         788.9         788.6         788.0         787.2         788.9         788.6         787.2         787.2         789.6         789.6         787.3         789.0         787.1         789.0         789.1         789.7         789.0         789.1         789.1         789.1         789.1         889.2 <th< td=""><td>785.3         786.0         786.4         788.9         789.6         790.3         791.0         891.0         <th< td=""><td>7863 7860 79924 7931 7993 8006 8122 8069 8129 8136 8195 8267 8267 8331 8375 8331 8451 8457 8451 8457 8451 8457 8451 8619 8632 8698 8751 8756 8808 8814 8808 8814 8808 8814 8907 8927 9031 9036 9138 9191 9196 9244 9299 9244 9299</td><td>7796</td><td>7803</td><td>7810</td><td>7818</td><td>7825</td><td>7832</td><td>7839</td><td>7846</td><td>-</td><td></td><td>_</td><td>1 2</td><td></td><td></td><td>3 4 4</td><td>3 4 4 5</td></th<></td></th<>	785.3         786.0         786.4         788.9         789.6         790.3         791.0         891.0 <th< td=""><td>7863 7860 79924 7931 7993 8006 8122 8069 8129 8136 8195 8267 8267 8331 8375 8331 8451 8457 8451 8457 8451 8457 8451 8619 8632 8698 8751 8756 8808 8814 8808 8814 8808 8814 8907 8927 9031 9036 9138 9191 9196 9244 9299 9244 9299</td><td>7796</td><td>7803</td><td>7810</td><td>7818</td><td>7825</td><td>7832</td><td>7839</td><td>7846</td><td>-</td><td></td><td>_</td><td>1 2</td><td></td><td></td><td>3 4 4</td><td>3 4 4 5</td></th<>	7863 7860 79924 7931 7993 8006 8122 8069 8129 8136 8195 8267 8267 8331 8375 8331 8451 8457 8451 8457 8451 8457 8451 8619 8632 8698 8751 8756 8808 8814 8808 8814 8808 8814 8907 8927 9031 9036 9138 9191 9196 9244 9299 9244 9299	7796	7803	7810	7818	7825	7832	7839	7846	-		_	1 2			3 4 4	3 4 4 5
7924         7921         7930         7940         7950         7960         800	7924         7921         7924         7921         7924         7921         7924         7921         7924         7921         7924         8924 <th< td=""><td>7924         7931         7930         7940         7950         8950         8950         8970         <th< td=""><td>  7993   7993   7993   8006   8006   8006   8126   8136   8385   8395   8457   8457   8692   8693   8692   8692   8692   8692   8692   8692   8906   8914   8957   8906   9138   9191   9196   9244   9299   9244   9244   9299   9244   9299   9244   9299   9244   9299   9244   9299   9244   9299  </td><td>7868</td><td>7875</td><td>7882</td><td>7889</td><td>7896</td><td>7903</td><td>7910</td><td>7917</td><td></td><td></td><td>_</td><td>2</td><td></td><td>e (</td><td>4 (</td><td>4 4</td></th<></td></th<>	7924         7931         7930         7940         7950         8950         8950         8970 <th< td=""><td>  7993   7993   7993   8006   8006   8006   8126   8136   8385   8395   8457   8457   8692   8693   8692   8692   8692   8692   8692   8692   8906   8914   8957   8906   9138   9191   9196   9244   9299   9244   9244   9299   9244   9299   9244   9299   9244   9299   9244   9299   9244   9299  </td><td>7868</td><td>7875</td><td>7882</td><td>7889</td><td>7896</td><td>7903</td><td>7910</td><td>7917</td><td></td><td></td><td>_</td><td>2</td><td></td><td>e (</td><td>4 (</td><td>4 4</td></th<>	7993   7993   7993   8006   8006   8006   8126   8136   8385   8395   8457   8457   8692   8693   8692   8692   8692   8692   8692   8692   8906   8914   8957   8906   9138   9191   9196   9244   9299   9244   9244   9299   9244   9299   9244   9299   9244   9299   9244   9299   9244   9299	7868	7875	7882	7889	7896	7903	7910	7917			_	2		e (	4 (	4 4
8062         8069         8076         8102 <th< td=""><td>8662         8669         876         876         876         876         876         876         876         876         876         876         876         876         876         876         876         876         876         876         877         877         877         877         877         877         878         878         878         877         877         877         877         877         877         877         878         878         878         877         877         878         888<!--</td--><td>8062         8069         8076         8106         8102         <th< td=""><td>8062 8069 8129 8136 8126 8267 8325 8331 8388 8395 8451 8457 8451 8679 8673 8679 8632 8638 8692 8698 8751 8756 8897 8987 8896 8814 8865 8871 8906 8914 8971 9036 9031 9036 9131 9196 9148 9248 9248</td><td>8007</td><td>8014</td><td>/952 8021</td><td>8028</td><td>7900</td><td>/9/3</td><td>7980</td><td>7987</td><td></td><td></td><td></td><td>2 6</td><td>2 6</td><td>n ~</td><td>2 C</td><td>3 4</td></th<></td></td></th<>	8662         8669         876         876         876         876         876         876         876         876         876         876         876         876         876         876         876         876         876         876         877         877         877         877         877         877         878         878         878         877         877         877         877         877         877         877         878         878         878         877         877         878         888 </td <td>8062         8069         8076         8106         8102         <th< td=""><td>8062 8069 8129 8136 8126 8267 8325 8331 8388 8395 8451 8457 8451 8679 8673 8679 8632 8638 8692 8698 8751 8756 8897 8987 8896 8814 8865 8871 8906 8914 8971 9036 9031 9036 9131 9196 9148 9248 9248</td><td>8007</td><td>8014</td><td>/952 8021</td><td>8028</td><td>7900</td><td>/9/3</td><td>7980</td><td>7987</td><td></td><td></td><td></td><td>2 6</td><td>2 6</td><td>n ~</td><td>2 C</td><td>3 4</td></th<></td>	8062         8069         8076         8106         8102 <th< td=""><td>8062 8069 8129 8136 8126 8267 8325 8331 8388 8395 8451 8457 8451 8679 8673 8679 8632 8638 8692 8698 8751 8756 8897 8987 8896 8814 8865 8871 8906 8914 8971 9036 9031 9036 9131 9196 9148 9248 9248</td><td>8007</td><td>8014</td><td>/952 8021</td><td>8028</td><td>7900</td><td>/9/3</td><td>7980</td><td>7987</td><td></td><td></td><td></td><td>2 6</td><td>2 6</td><td>n ~</td><td>2 C</td><td>3 4</td></th<>	8062 8069 8129 8136 8126 8267 8325 8331 8388 8395 8451 8457 8451 8679 8673 8679 8632 8638 8692 8698 8751 8756 8897 8987 8896 8814 8865 8871 8906 8914 8971 9036 9031 9036 9131 9196 9148 9248 9248	8007	8014	/952 8021	8028	7900	/9/3	7980	7987				2 6	2 6	n ~	2 C	3 4
8129         8136         8142         8156         8156         8156         8156         8156         8156         8156         8156         8156         8156         8156         8158 <th< td=""><td>8129         8136         8142         8156         8156         8156         8156         8156         8156         8156         8156         8158         8136         8189         <th< td=""><td>8129         8136         8142         8156         8156         8156         8156         8156         8156         8156         8156         8158         8189         <th< td=""><td>8129 8136 8195 8202 8261 8267 8388 8395 8451 8457 8451 8659 8653 8659 86632 8698 8751 8756 88692 8698 8751 8756 8800 8814 8806 8814 8906 8871 8907 9036 9031 9036 9138 9191 9196 9243 9248</td><td>8075</td><td>8082</td><td>8089</td><td>9608</td><td>8102</td><td>8109</td><td>8116</td><td>8122</td><td>-</td><td>-</td><td></td><td>2 2</td><td></td><td></td><td>3 0 0</td><td>n m</td></th<></td></th<></td></th<>	8129         8136         8142         8156         8156         8156         8156         8156         8156         8156         8156         8158         8136         8189 <th< td=""><td>8129         8136         8142         8156         8156         8156         8156         8156         8156         8156         8156         8158         8189         <th< td=""><td>8129 8136 8195 8202 8261 8267 8388 8395 8451 8457 8451 8659 8653 8659 86632 8698 8751 8756 88692 8698 8751 8756 8800 8814 8806 8814 8906 8871 8907 9036 9031 9036 9138 9191 9196 9243 9248</td><td>8075</td><td>8082</td><td>8089</td><td>9608</td><td>8102</td><td>8109</td><td>8116</td><td>8122</td><td>-</td><td>-</td><td></td><td>2 2</td><td></td><td></td><td>3 0 0</td><td>n m</td></th<></td></th<>	8129         8136         8142         8156         8156         8156         8156         8156         8156         8156         8156         8158         8189 <th< td=""><td>8129 8136 8195 8202 8261 8267 8388 8395 8451 8457 8451 8659 8653 8659 86632 8698 8751 8756 88692 8698 8751 8756 8800 8814 8806 8814 8906 8871 8907 9036 9031 9036 9138 9191 9196 9243 9248</td><td>8075</td><td>8082</td><td>8089</td><td>9608</td><td>8102</td><td>8109</td><td>8116</td><td>8122</td><td>-</td><td>-</td><td></td><td>2 2</td><td></td><td></td><td>3 0 0</td><td>n m</td></th<>	8129 8136 8195 8202 8261 8267 8388 8395 8451 8457 8451 8659 8653 8659 86632 8698 8751 8756 88692 8698 8751 8756 8800 8814 8806 8814 8906 8871 8907 9036 9031 9036 9138 9191 9196 9243 9248	8075	8082	8089	9608	8102	8109	8116	8122	-	-		2 2			3 0 0	n m
8195         8202         8202         8222         8232         8234         8244         8254           8261         8274         8280         8292         8293         8293         8293         8293         8294         8254         8254         8254         8254         8254         8254         8252         8293         8293         8293         8293         8344         8351         8342         8342         8343         8343         8343         8343         8343         8343         8343         8343         8343         8343         8345         8445         8465         8645         86	8195         8202         8202         8221         8223         8234         8241         8246         8254         8240         8241         8240         8241         8240         8241         8241         8240         8241         8242         8243         8245         8245         8243         8245         8245         8245         8245         8245         8245         8243         8245         8245         8243         8243         8243         8243         8243         8243         8243         8244         8245         8245         8244         8244         8245         8244         8244         8244         8244         8244         8244         8244         8244         8244         8244         8244 <th< td=""><td>8195         82002         82016         8215         8222         8235         8241         8248         8254           8261         8274         8280         8287         8293         8293         8293         8312         8319         8312         8319         8318         8348</td><td>8451 8267 8328 8338 8451 8457 8451 8457 8451 8679 8632 8638 8632 8638 8751 8756 8802 8814 8808 8814 8806 8814 8806 8871 8907 9036 9031 9036 9131 9196 9181 9196 9243 9248</td><td>8142</td><td>8149</td><td>8156</td><td>8162</td><td>8169</td><td>8176</td><td>8182</td><td>8189</td><td>-</td><td>-</td><td></td><td>2</td><td></td><td></td><td>3 3 4</td><td>8</td></th<>	8195         82002         82016         8215         8222         8235         8241         8248         8254           8261         8274         8280         8287         8293         8293         8293         8312         8319         8312         8319         8318         8348	8451 8267 8328 8338 8451 8457 8451 8457 8451 8679 8632 8638 8632 8638 8751 8756 8802 8814 8808 8814 8806 8814 8806 8871 8907 9036 9031 9036 9131 9196 9181 9196 9243 9248	8142	8149	8156	8162	8169	8176	8182	8189	-	-		2			3 3 4	8
8261         8267         8274         8280         8281         8393         8299         8290         8312         8319           8325         8331         8338         8346         8341         8361         8357         8376         8376         8376         8376         8376         8376         8378         8392         8392         8392         8392         8345         8485         8445         8450         8461         8647         8445         8647         86	8261         8267         8274         8280         8281         8281         8281         8282         8393         8399         8306         8312         8319         8311         8314 <th< td=""><td>8761         8267         8274         8280         8281         8312         8319           8326         8331         8346         8346         8357         8353         8399         8306         8312         8319           8326         8331         8401         8407         8414         8357         8356         8356         8485           8451         8457         8482         8436         8446         8600         8606         8607         8607         8608         8616         8667<td>8261 8267 8381 8385 8451 8457 8573 8579 8673 8679 8692 8698 8692 8698 8751 8756 8806 8814 8806 8814 8806 8814 8807 8971 9985 9090 9138 9143 9085 9090 9138 9143 9244 9299</td><td>8209</td><td>8215</td><td>8222</td><td>8228</td><td>8235</td><td>8241</td><td>8248</td><td>8254</td><td>-</td><td>-</td><td></td><td>2</td><td>-</td><td>က</td><td>3 3 4</td><td>3 3 4 5</td></td></th<>	8761         8267         8274         8280         8281         8312         8319           8326         8331         8346         8346         8357         8353         8399         8306         8312         8319           8326         8331         8401         8407         8414         8357         8356         8356         8485           8451         8457         8482         8436         8446         8600         8606         8607         8607         8608         8616         8667 <td>8261 8267 8381 8385 8451 8457 8573 8579 8673 8679 8692 8698 8692 8698 8751 8756 8806 8814 8806 8814 8806 8814 8807 8971 9985 9090 9138 9143 9085 9090 9138 9143 9244 9299</td> <td>8209</td> <td>8215</td> <td>8222</td> <td>8228</td> <td>8235</td> <td>8241</td> <td>8248</td> <td>8254</td> <td>-</td> <td>-</td> <td></td> <td>2</td> <td>-</td> <td>က</td> <td>3 3 4</td> <td>3 3 4 5</td>	8261 8267 8381 8385 8451 8457 8573 8579 8673 8679 8692 8698 8692 8698 8751 8756 8806 8814 8806 8814 8806 8814 8807 8971 9985 9090 9138 9143 9085 9090 9138 9143 9244 9299	8209	8215	8222	8228	8235	8241	8248	8254	-	-		2	-	က	3 3 4	3 3 4 5
8451         8452         8454         8450         8451         8450         8451         8450         8451         8851         8851         8851         8851         8851         8851         8851         8851         8851         8852 <th< td=""><td>8451         8452         8451         8445         8451         8851         8851         8851         8851         8851         8851         8851         8852         8851         8852         <th< td=""><td>8451         8452         8451         8651         8651         8651         8651         8651         8652         8651         8652         8651         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         <th< td=""><td>8328 8395 8451 8457 8513 8519 8632 8633 8662 8638 8751 8756 8802 8814 8808 8814 8808 8814 8801 8927 8976 8982 9031 9036 9085 9090 9193 9193 9243 9248</td><td>8274</td><td>8280</td><td>8287</td><td>8293</td><td>8299</td><td>8306</td><td>8312</td><td>8319</td><td></td><td><b>.</b></td><td></td><td>2</td><td>******</td><td>en e</td><td>e c</td><td>2 4</td></th<></td></th<></td></th<>	8451         8452         8451         8445         8451         8851         8851         8851         8851         8851         8851         8851         8852         8851         8852 <th< td=""><td>8451         8452         8451         8651         8651         8651         8651         8651         8652         8651         8652         8651         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         <th< td=""><td>8328 8395 8451 8457 8513 8519 8632 8633 8662 8638 8751 8756 8802 8814 8808 8814 8808 8814 8801 8927 8976 8982 9031 9036 9085 9090 9193 9193 9243 9248</td><td>8274</td><td>8280</td><td>8287</td><td>8293</td><td>8299</td><td>8306</td><td>8312</td><td>8319</td><td></td><td><b>.</b></td><td></td><td>2</td><td>******</td><td>en e</td><td>e c</td><td>2 4</td></th<></td></th<>	8451         8452         8451         8651         8651         8651         8651         8651         8652         8651         8652         8651         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652         8651         8652 <th< td=""><td>8328 8395 8451 8457 8513 8519 8632 8633 8662 8638 8751 8756 8802 8814 8808 8814 8808 8814 8801 8927 8976 8982 9031 9036 9085 9090 9193 9193 9243 9248</td><td>8274</td><td>8280</td><td>8287</td><td>8293</td><td>8299</td><td>8306</td><td>8312</td><td>8319</td><td></td><td><b>.</b></td><td></td><td>2</td><td>******</td><td>en e</td><td>e c</td><td>2 4</td></th<>	8328 8395 8451 8457 8513 8519 8632 8633 8662 8638 8751 8756 8802 8814 8808 8814 8808 8814 8801 8927 8976 8982 9031 9036 9085 9090 9193 9193 9243 9248	8274	8280	8287	8293	8299	8306	8312	8319		<b>.</b>		2	******	en e	e c	2 4
8451         8457         8462         8482         8488         8484         8656         8650         8650         8651         8657         1         1           8573         8553         8543         8543         8549         8656         8651         8667         1         1           8673         8639         8645         8656         8651         8667         1         1           8632         8645         8646         8669         8615         8667         1         1           8692         86868         8704         8710         875         872         873         8745         1         1           8908         8704         8710         878         872         872         872         8745         1         1           8908         8804         8863         8894         8874         8848         8854         8859         1         1           8906         8814         8867         8843         8949         8904         8904         8904         8904         8904         8904         9904         9904         9904         9904         9904         9904         9904         9904         99	8451         8457         8463         8482         8488         8484         8656         8650         8566         8661         8667         1         1           8573         8553         8543         8543         8549         8656         8661         8667         1         1           8673         8639         8645         8656         8661         8667         1         1           8632         8645         8656         8667         8667         8667         867         1         1           8692         8688         8704         8716         872         872         872         873         8745         1         1           8866         8704         876         867         8842         8848         8854         8859         1         1         1           8866         871         878         877         878         8874         8848         8854         8859         887         1         1           8908         881         8843         8843         8894         8964         8964         8964         8964         8964         8964         8964         8964         8964         8964	8451         8457         8462         8482         8484         8484         8656         8650         8506         1         1           8513         8525         8521         8537         8543         8549         8656         8651         8667         1         1           8673         8659         8651         8657         8663         8665         8661         8667         1         1           8632         8639         8645         8651         8663         8665         8661         8667         1         1           8692         8689         8704         8716         8779         8737         8739         8745         1         1           8806         8714         8719         8785         8727         8737         8739         8745         1         1           8806         8814         8820         8824         8842         8848         8859         8890         8904         8906         8907         1         1           8906         8817         8827         8837         8842         8848         8854         8859         8901         1         1         1         1         1	8451 8457 8573 8579 8632 8639 8632 8639 8751 8756 8751 8756 8871 8927 8976 8982 9031 9036 9085 9090 9138 9143 9191 9196 9243 9248 9244 9299	8401	8407	8414	8420	8426	8432	8439	8445			4		n m		2 m	າ ຕ
8513         8549         8654         8656         8661         8667         1         1           8573         8553         8543         8543         8549         8656         8667         8667         867         1         1           8637         8638         8646         8657         8663         8669         8615         8627         1         1           8692         8698         8746         8776         8737         8733         8739         8745         1         1           8908         8746         8776         8772         8737         8737         8739         8746         1         1           8908         8814         8820         8874         8842         8848         8854         8859         1         1         1           8906         8814         882         8843         8943         8944         8969         8964         8969         8964         8969         8964         8969         8964         8969         8964         8969         8964         8969         8964         8969         8964         8969         8964         8969         8964         8969         8964         8969	8513         8519         8526         8531         8543         8549         8656         8667         8667         8671         8673         8674         8656         8667         8667         8667         8671         8673         8673         8673         8673         8673         8674         8671         8673         8673         8673         8673         8673         8745         1         1           8692         8698         8704         8710         8772         8727         8723         8739         8745         1         1           8808         8704         8704         872         872         8727         <	8513         8549         8543         8549         8656         8667         8671         1         1           8573         8559         8651         8657         8651         8657         1         1         1           8632         8659         8651         8663         8663         8663         8663         8667         8671         875         1         1           8692         8683         874         877         873         873         873         8745         1         1           8808         874         867         874         873         872         872         875         874         1         1           8808         874         867         882         884         884         885         885         1         1         1           8808         881         882         883         889         894         8964         8964         8964         8967         1         1           8908         881         883         889         896         8904         8969         8904         8964         8964         8964         8964         8964         8964         8964         8964	8513 8519 8573 8579 8632 8638 8682 8638 8751 8751 8756 8802 8814 8821 8927 8976 8982 9031 9036 9085 9090 9143 9191 9191 9196 9243 9248 9244 9299	8463	8470	8476	8482	8488	8494	8500	8506	-	-	10	+	-	2	2	2
8579         8565         8591         8597         8603         8615         8671         8673         8671         8671         8671         8671         8671         8671         8671         8671         8671         8671         8671         8672         8673         8673         8673         8673         8673         8687         1         1         1           868         876         871         872         872         873         8739         8745         1         1         1           876         876         877         872         873         873         873         874         1         1           8814         8876         887         883         884         884         886         1         1         1           887         887         883         8943         8949         8964         896         897         1         1           887         8887         8887         8943         8969         8904         891         1         1           887         887         8943         8969         8904         891         1         1           892         8948         8949	8579         8565         8571         8693         8675         8671         8671         8671         8671         8671         8671         8671         8671         8671         8671         8671         8671         8671         8671         8671         8672         8672         8682         8675         8673         8673         8673         8673         8673         8673         8673         8673         8673         8673         8674         8772         8772         8772         8772         8773         7773         7773         7773         7773         7773         7773         7773         7773         7773         7773         8773         8773         8773         8773         8773         8773         8773         8773         8773         8773         8773         8773         8773         8774         8773         8774         8773         8774         8773 <th< td=""><td>8579         8585         8591         8597         8603         8609         8615         8621         8627         1         1           8638         8645         8651         8657         8663         8669         8675         8681         8666         1         1           8689         8704         8772         8722         8733         8739         8745         1         1           8756         8762         8762         8774         8773         8787         8897         8894         8744         8779         8788         8894         8964         8910</td><td>8579 8639 8638 8756 8814 8877 8927 8982 9036 9036 9148 9148 9248</td><td>8525</td><td>8531</td><td>8537</td><td>8543</td><td>8549</td><td>8555</td><td>8561</td><td>8567</td><td>-</td><td>-</td><td>2</td><td>_</td><td>2</td><td>2 3 4</td><td></td><td>3 4 4</td></th<>	8579         8585         8591         8597         8603         8609         8615         8621         8627         1         1           8638         8645         8651         8657         8663         8669         8675         8681         8666         1         1           8689         8704         8772         8722         8733         8739         8745         1         1           8756         8762         8762         8774         8773         8787         8897         8894         8744         8779         8788         8894         8964         8910	8579 8639 8638 8756 8814 8877 8927 8982 9036 9036 9148 9148 9248	8525	8531	8537	8543	8549	8555	8561	8567	-	-	2	_	2	2 3 4		3 4 4
865.3         865.3         864.5         865.1         865.3         866.9         867.5         868.1         868.6         1         1           8692         8686         870.4         871.0         871.6         872.2         872.7         873.2         873.9         874.5         1         1           875.1         875.6         876.2         877.2         872.7         873.2         873.7         884.2         884.8         885.9         1         1           880.6         881.1         887.6         887.8         884.2         884.8         885.4         885.0         1         1           886.6         887.1         887.6         889.3         884.9         884.8         885.4         885.0         1         1           897.1         897.1         889.3         894.9         896.4         896.0         890.6         890.7         1         1           897.8         894.3         896.9         900.4         901.0         901.6         901.7         907.9         1         1           903.1         902.9         904.9         904.9         904.9         904.9         907.9         1         1         1 <tr< td=""><td>8653         8645         8645         8657         8663         8667         867         867         867         867         867         867         867         867         867         867         867         868         868         1         1           8751         8756         8776         8772         8772         8773         878         878         878         878         878         878         878         878         878         889         889         889         889         889         889         889         889         890         891         891         891         892         890         891         891         891         892         890         891         891         892         890         891         891         892         890         891         891         891         891         891         891         891         891         891         892         890         891         891         892         890         891         891         891         892         890         901         902         902         902         902         902         902         902         902         902         902         902         9</td><td>8653         8645         8651         8653         8669         8675         8681         8686         8675         8681         8686         8675         8732         8732         8737         8733         8739         8746         8747         8772         8773         8783         8749         8772         8773         8784         8854         8859         1         1           8808         8871         8875         8874         8896         8904<td>8633 8639 8632 8698 8751 8756 8806 8814 8927 8927 8976 8982 9031 9036 9085 9090 9138 9143 9191 9196 9243 9248 9244 9299</td><td>8585</td><td>8591</td><td>8597</td><td>8603</td><td>8609</td><td>8615</td><td>8621</td><td>8627</td><td>-</td><td>-</td><td>2</td><td>_</td><td>2</td><td></td><td></td><td>3 4 4</td></td></tr<>	8653         8645         8645         8657         8663         8667         867         867         867         867         867         867         867         867         867         867         867         868         868         1         1           8751         8756         8776         8772         8772         8773         878         878         878         878         878         878         878         878         878         889         889         889         889         889         889         889         889         890         891         891         891         892         890         891         891         891         892         890         891         891         892         890         891         891         892         890         891         891         891         891         891         891         891         891         891         892         890         891         891         892         890         891         891         891         892         890         901         902         902         902         902         902         902         902         902         902         902         902         9	8653         8645         8651         8653         8669         8675         8681         8686         8675         8681         8686         8675         8732         8732         8737         8733         8739         8746         8747         8772         8773         8783         8749         8772         8773         8784         8854         8859         1         1           8808         8871         8875         8874         8896         8904 <td>8633 8639 8632 8698 8751 8756 8806 8814 8927 8927 8976 8982 9031 9036 9085 9090 9138 9143 9191 9196 9243 9248 9244 9299</td> <td>8585</td> <td>8591</td> <td>8597</td> <td>8603</td> <td>8609</td> <td>8615</td> <td>8621</td> <td>8627</td> <td>-</td> <td>-</td> <td>2</td> <td>_</td> <td>2</td> <td></td> <td></td> <td>3 4 4</td>	8633 8639 8632 8698 8751 8756 8806 8814 8927 8927 8976 8982 9031 9036 9085 9090 9138 9143 9191 9196 9243 9248 9244 9299	8585	8591	8597	8603	8609	8615	8621	8627	-	-	2	_	2			3 4 4
8751         8756         8757 <th< td=""><td>8751         8756         8757         <th< td=""><td>8751         8756         8774         8779         8774         8777         8779         8774         8777         8779         8774         8777         8779         8774         8779         8774         8779         8774         8779         8774         8779         8774         8779         8774         8779         8777         8779         8777         8771         8772         8772         8772         8772         8772         8772         8772         8772         8772         8772         8772         8772         8772         8772         8772         8772         8772         8772         8772         8774         8772         8772         8772         8772         8772         <th< td=""><td>8751 8756 8808 8814 8856 8871 8927 8927 8976 8982 9031 9036 9085 9090 9138 9143 9191 9196 9243 9248 9249 9299 9346 9350</td><td>8645</td><td>8651</td><td>8657</td><td>8663</td><td>8727</td><td>8675</td><td>8681</td><td>8686</td><td></td><td></td><td>2 0</td><td>_</td><td>2 6</td><td>2 3 4</td><td></td><td></td></th<></td></th<></td></th<>	8751         8756         8757 <th< td=""><td>8751         8756         8774         8779         8774         8777         8779         8774         8777         8779         8774         8777         8779         8774         8779         8774         8779         8774         8779         8774         8779         8774         8779         8774         8779         8777         8779         8777         8771         8772         8772         8772         8772         8772         8772         8772         8772         8772         8772         8772         8772         8772         8772         8772         8772         8772         8772         8772         8774         8772         8772         8772         8772         8772         <th< td=""><td>8751 8756 8808 8814 8856 8871 8927 8927 8976 8982 9031 9036 9085 9090 9138 9143 9191 9196 9243 9248 9249 9299 9346 9350</td><td>8645</td><td>8651</td><td>8657</td><td>8663</td><td>8727</td><td>8675</td><td>8681</td><td>8686</td><td></td><td></td><td>2 0</td><td>_</td><td>2 6</td><td>2 3 4</td><td></td><td></td></th<></td></th<>	8751         8756         8774         8779         8774         8777         8779         8774         8777         8779         8774         8777         8779         8774         8779         8774         8779         8774         8779         8774         8779         8774         8779         8774         8779         8777         8779         8777         8771         8772         8772         8772         8772         8772         8772         8772         8772         8772         8772         8772         8772         8772         8772         8772         8772         8772         8772         8772         8774         8772         8772         8772         8772         8772 <th< td=""><td>8751 8756 8808 8814 8856 8871 8927 8927 8976 8982 9031 9036 9085 9090 9138 9143 9191 9196 9243 9248 9249 9299 9346 9350</td><td>8645</td><td>8651</td><td>8657</td><td>8663</td><td>8727</td><td>8675</td><td>8681</td><td>8686</td><td></td><td></td><td>2 0</td><td>_</td><td>2 6</td><td>2 3 4</td><td></td><td></td></th<>	8751 8756 8808 8814 8856 8871 8927 8927 8976 8982 9031 9036 9085 9090 9138 9143 9191 9196 9243 9248 9249 9299 9346 9350	8645	8651	8657	8663	8727	8675	8681	8686			2 0	_	2 6	2 3 4		
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ADD PROPORTIONAL PARTS

### Glossary of symbols

		Main page			
		references			
A	factor for action limits on $\vec{X}$ -chart	41	S	the sign test statistic	28-29, 35
$a_1$	lower action limit on R-chart is $a_1\overline{R}$	41	S	unadjusted sample standard deviation:	,
$a_2$	upper action limit on R-chart is $a_2 \overline{R}$	41	-	$S = \{ \sum (X - \bar{X})^2 / n \}^{1/2}$	
c	$= \sigma/E\{R\} = 1/d_1$ ; conversion factor for		$\bar{S}$	average value of S in pilot samples	41
	estimating $\sigma$ from sample range	41	S	adjusted sample standard deviation,	**
c.d.f.	cumulative distribution function:	7.1		satisfying $E\{s^2\} = \sigma^2$ (but not $E\{s\} = \sigma$ )	
	Prob $(X \leq x)$			satisfying $E(s) = 0$ (but not $E(s) = 0$ )	1311/2
D			-	with single sample, $s = {\sum (X - \bar{X})^2/(n - \bar{X})^2}$	
D	Kolmogorov—Smirnov two-sample test statistic	20 25	S 2 2	average value of s in pilot samples	41
$D^*$		28, 35	$s^2, s_1^2,$	[[[[[]]]]]	
$D^2$	$= n_A n_B D$	28, 31	T	the Wilcoxon signed-rank test statistic	
	sum of squares of rank differences	35, 40	t	'Student' t statistic, test or distribution	20
$D_n$	test statistic for Kolmogorov-Smirnov		U	random variable having uniform	
-+	goodness-of-fit test or test for normalit			distribution on (0:1)	42
	one-sided versions of $D_n$	_ 26-27	U	the Mann-Whitney test statistic	28, 30, 35
$d_1$	= $E\{R\}/\sigma$ ; conversion factor from $\sigma$ to	R 41	$U_A$	$=R_A - \frac{1}{2}n_A(n_A + 1)$	28
$d_2$	$= E\{R\}/E\{S\}$ ; conversion factor from		$U_{B}$	$=R_B-\frac{1}{2}n_B(n_B+1)$	28
	S to R	41	W	factor for warning limits on $\bar{X}$ -chart	41
$d_3$	= $E\{R\}/E\{s\}$ ; conversion factor from		$w_1$	lower warning limit on R-chart is $w_1 \overline{R}$	41
	$\bar{s}$ to $\bar{R}$	41	W2	upper warning limit on R-chart is $w_2 \overline{R}$	41
$E\{ \}$	expected, i.e. long-term mean, value of		X	random variable	
e	= 2.718 28; base of natural logarithms	18, 46	x	value of X	
F	(Snedecor) F statistic, test or distribution			$\overline{X}_2, \overline{Y}$ sample means	
$F_0(x)$			$\overline{\overline{X}}$	average of sample means in pilot sample	. 41
	distribution	26		average of sample means in pilot sample	s 41
$F_n(x)$	sample (empirical) c.d.f.; proportion of		(X, Y)	matched-pair or bivariate (two-variable)	
ne-,	sample values which are $\leq x$	26	1/	quantity	28, 35
f	sample fraction; number of occurrences		Y	random variable	
,	divided by sample size	10-13	y	value of Y	
$f_1$	lower critical value for $f$ , or confidence	10-13	Z	random variable having standard normal	
J 1		10 12 22		distribution	18 - 20
c	limit using F distribution	10-13, 22	z	value of Z	18-20
$f_2$	upper critical value for f, or confidence		z, z(r),	$z(\rho)$ values obtained using Fisher's	
	limit using F distribution	10-13, 22		z-transformation	35-37
H	Kruskal-Wallis test statistic	28,32-35	1277		
$H_0$	null hypothesis (usually of status quo		α	sometimes used in place of $\alpha_2$ if	222
	or no difference)			one-sided test non-existent	28
$H_1$	alternative hypothesis (what a test is		$\alpha_1$	significance level for one-sided test	20
	designed to detect)		$\alpha f$	significance level for left-hand tail	
k	number of regression variables	22		one-sided test	20
k	number of samples	28, 32-35	$\alpha_1^R$	significance level for right-hand tail	
ln )	logarithm to base e (natural logarithm),			one-sided test	20
log <sub>e</sub>	such that if $\log_e x = y$ then $e^y = x$	45, 47	$\alpha_2$	significance level for two-sided test	20
log <sub>10</sub>	logarithm to base 10 (common	,	γ	confidence level for confidence intervals	
- 010	logarithm), such that if $\log_{10} x = y$		$\mu, \mu_1, \mu_2$		
	then $10^y = x$	45, 48		distributions; $\mu = E\{X\}$	,
M	Friedman's test statistic	28, 34–35	$\nu, \nu_1, \nu_2$		nd
	maximum (largest) value of		-,-1,-2	F distributions)	20-25
N		26	$\pi$	mathematical constant, = 3.141 59	18, 45
	total number of observations	28,32-33			
$N_C$	number of concordant pairs, i.e.		ρ	population linear correlation coefficient	35-39
	$(X_1, Y_1), (X_2, Y_2)$ with		$\rho_0$	(null) hypothesised value of $\rho$	35
	$(X_1 - X_2)(Y_1 - Y_2) + ve$	35, 40	Σ	summation, e.g.	
$N_D$	number of discordant pairs, i.e.			$\Sigma X = \Sigma X_i = X_1 + X_2 + X_3 + \dots$	
	$(X_1, Y_1), (X_2, Y_2)$ with		$\sigma$ , $\sigma_1$ , $\sigma$		
	$(X_1 - X_2)(Y_1 - Y_2) - ve$	35, 40		standard deviations of probability	
	$n_A, n_B, n_i$ sample sizes			distributions; $\sigma = (E\{(X-\mu)^2\})^{1/2}$	
n	common sample size of equal-size sample	es 28, 34	$\sigma^2$	population variance; variance of probabil	ity
n	binomial coefficient; number of possible			distribution; $\sigma^2 = E\{(X - \mu)^2\}$	21
	groups of $r$ objects out of $n$	4, 44	$\tau$	the Kendall rank correlation coefficient	35, 40
	binomial parameter; probability of event		Φ	c.d.f. of the standard normal	,
	happening at any trial of experiment	0.000			18-20, 27
n	(ault) because of any that of experiment		φ	ordinate of the standard normal curve	18-19
P <sub>0</sub>	(null) hypothesised value of p	10-11	$\chi^2$	chi-squared statistic, test or distribution	21
	probability of			emisquared statistic, test or distinuation	21
	quantile; the number x such that			is less than	
and the second	$\operatorname{Prob}\left(X\leqslant x\right)=q$	20		is less than or equal to	
	multiple correlation coefficient	22	>	is greater than	
	sample range:		≥	is greater than or equal to	
_	maximum value - minimum value	41		is not equal to	
	average range in pilot samples	41		positive (>0)	
	rank sums of samples A and B	28		negative (< 0)	
	sample linear correlation coefficient	35-39	11	modulus, absolute value, ignore minus sig	m if —w
	lower and upper critical values for r	35			
	the Spearman rank correlation coefficier			integer part; $[x]$ is the largest integer $\leq x$	
3		55, 40		factorial, e.g. $4! = 4 \times 3 \times 2 \times 1 = 24$	44-45
			1	integral	

These tables have been carefully prepared for the many users of statistical analysis at an introductory level. The enthusiastic reception accorded to the author's *Statistics Tables* (1978) by specialist statisticians highlighted the need for a briefer set of tables to be tailored to the requirements of students who have to use statistical analysis but with no greater commitment to it than is represented by a basic and often brief introductory course.

Both the coverage and the presentation of this set of tables have been determined with great care. In contrast with competing sets at this level, the content should match closely the requirements of users, who need have little mathematical background. The book is a positive teaching and learning aid, not just a stark and impenetrable reference item. Most of the tables are accompanied by fully explanatory introductory text and by some examples of use. Each table has been designed and laid out carefully for maximum clarity and ease of use, features which the large page size should also reinforce. There are many new or improved tables, some being much more extensive than in competing books. In view of the increasing recognition of nonparametric tests for their convenience, ease of use and wide application, the tables covering these tests should prove especially valuable.

The tables should serve the needs of all users of elementary techniques of statistical analysis, from engineers and technicians to geographers and social scientists. All students taking first courses in statistical analysis will find them an invaluable aid.

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ROUTLEDGE

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